

Modeling Prompt Atmospheric lepton fluxes with Intrinsic Charm contribution

Diksha Garg¹

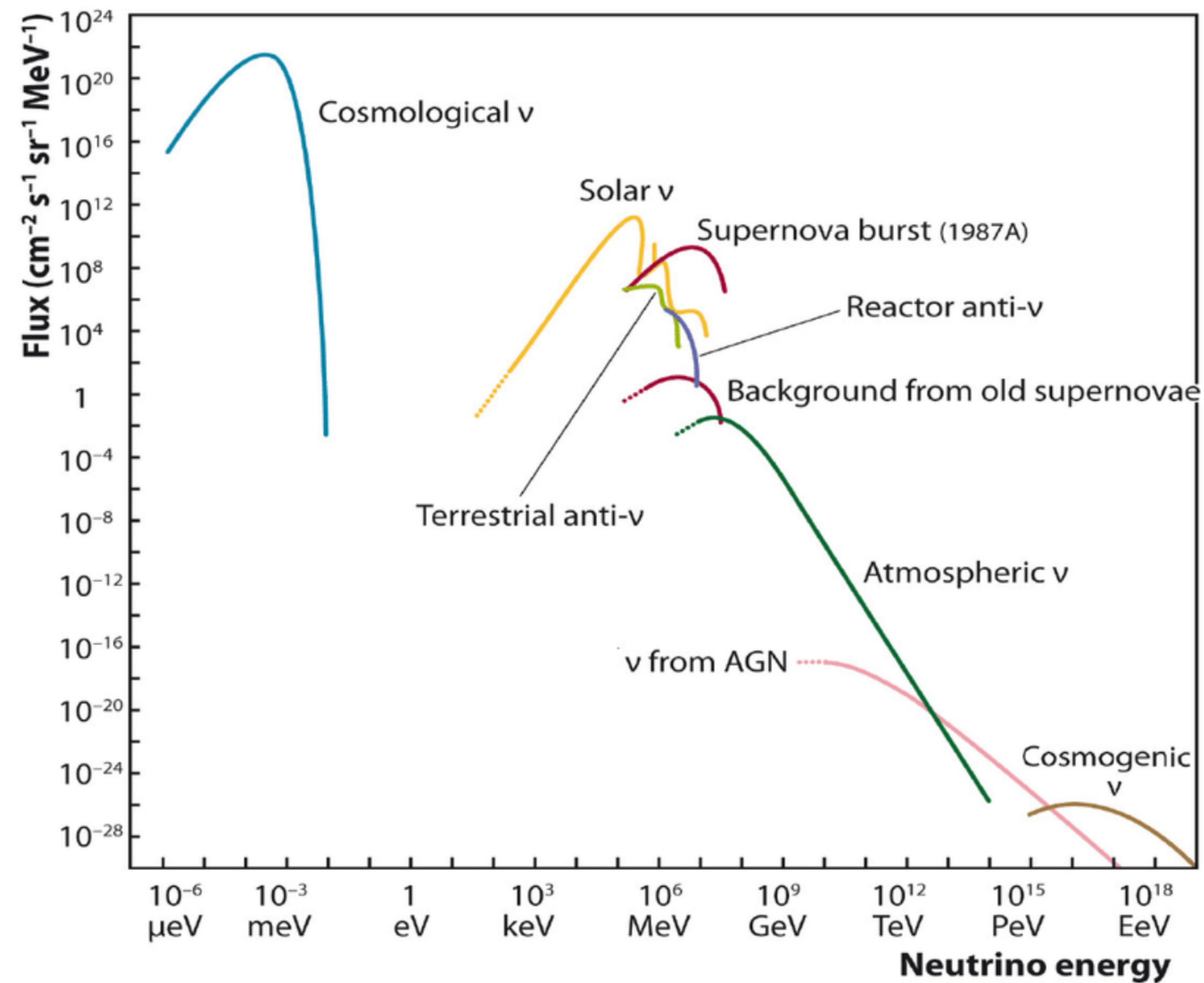
Work in progress with L P Das¹, M V Garzelli², M H Reno¹, G Sigl²

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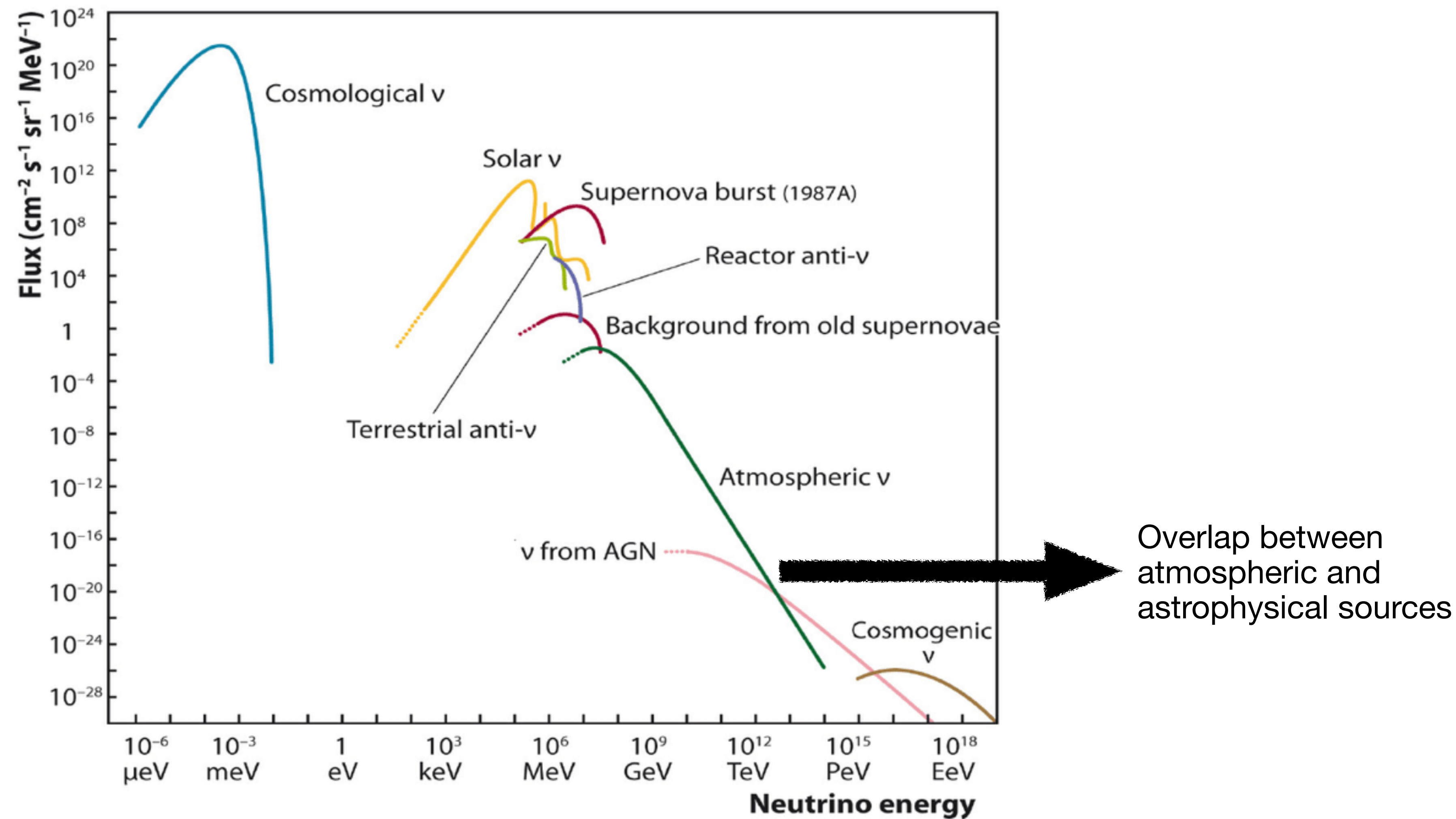
CETUP* Workshop - Neutrino session

July 11, 2025

Neutrino Flux

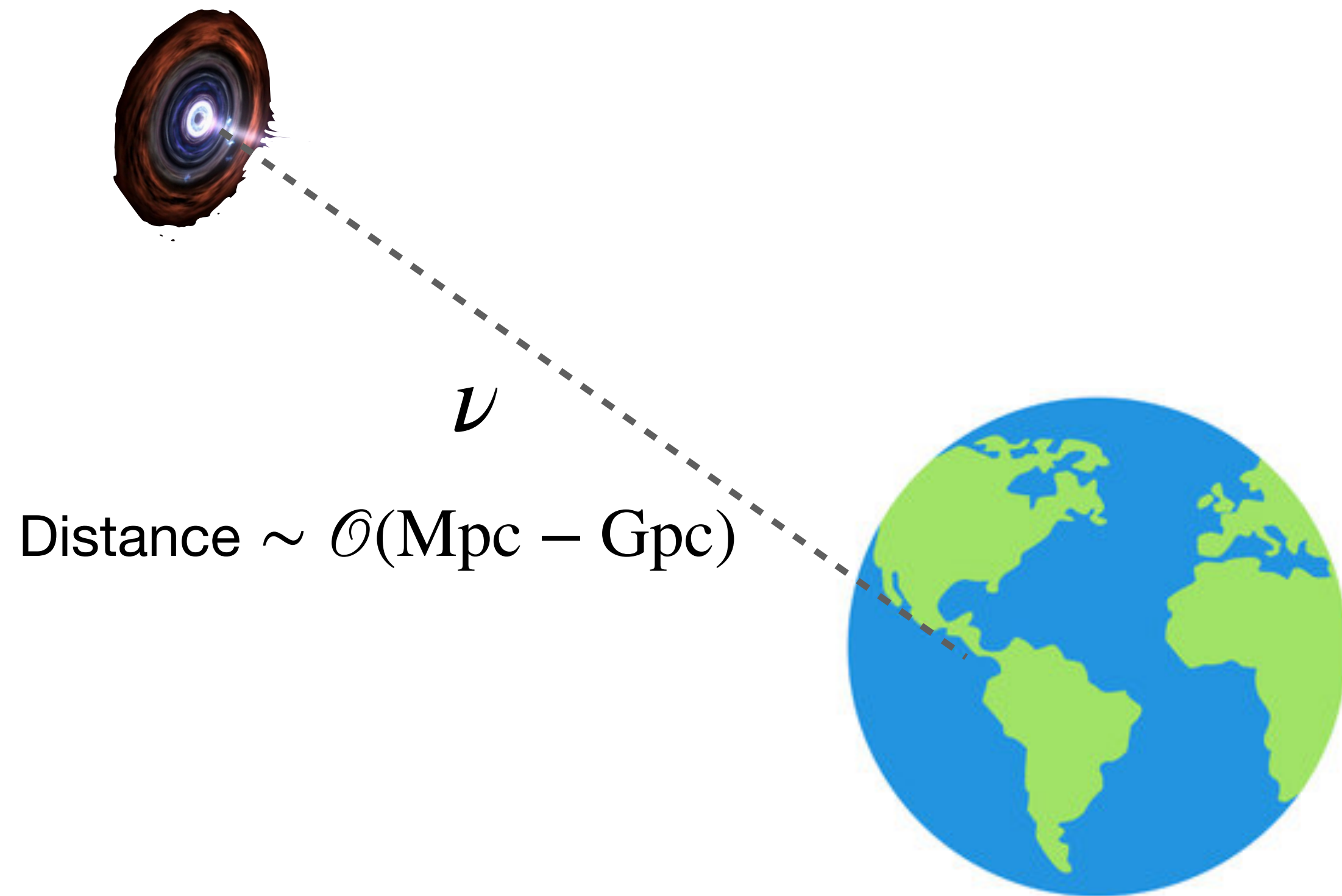


Neutrino Flux

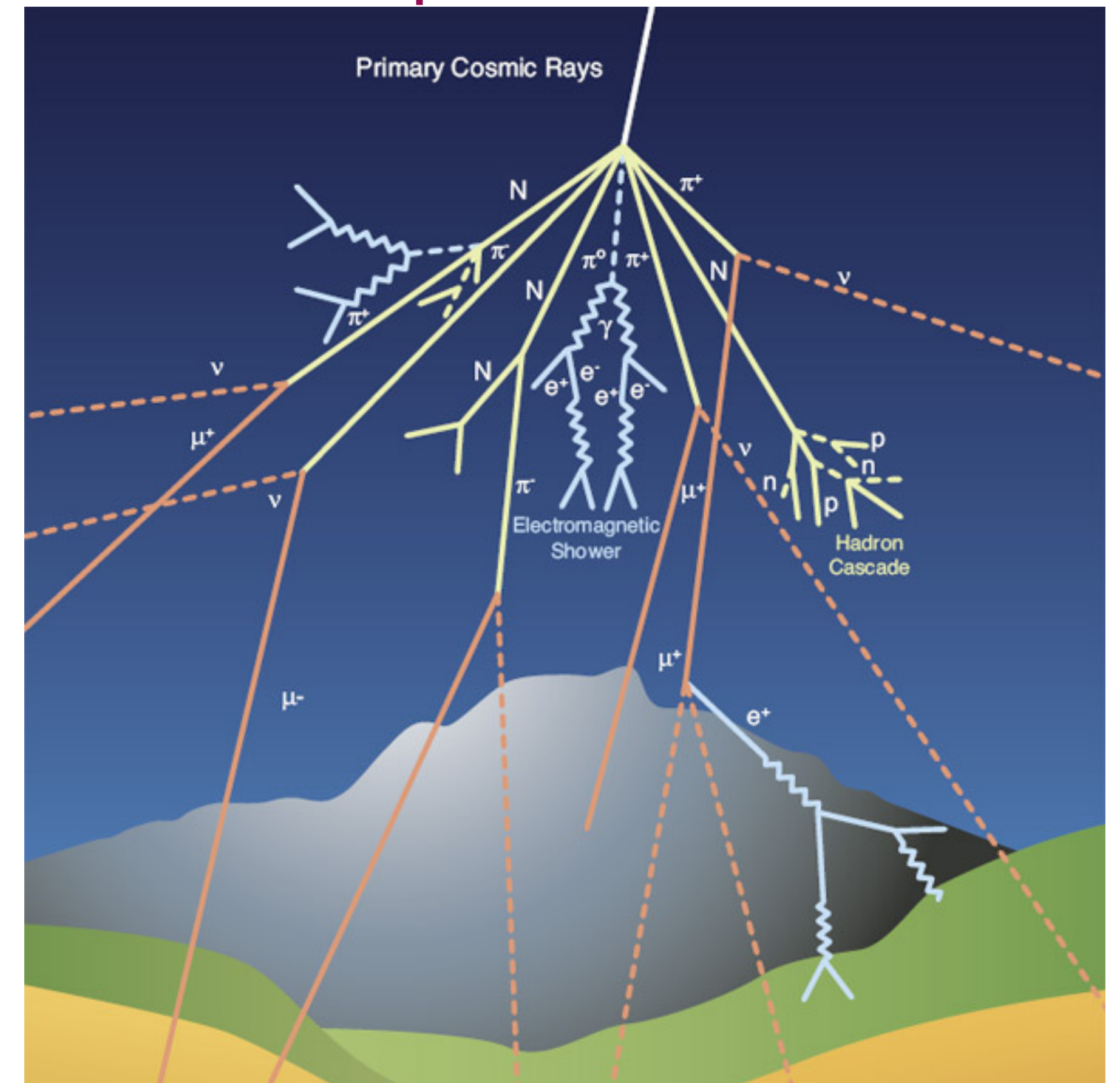


Astrophysical vs Atmospheric Neutrinos

Astrophysical Neutrinos



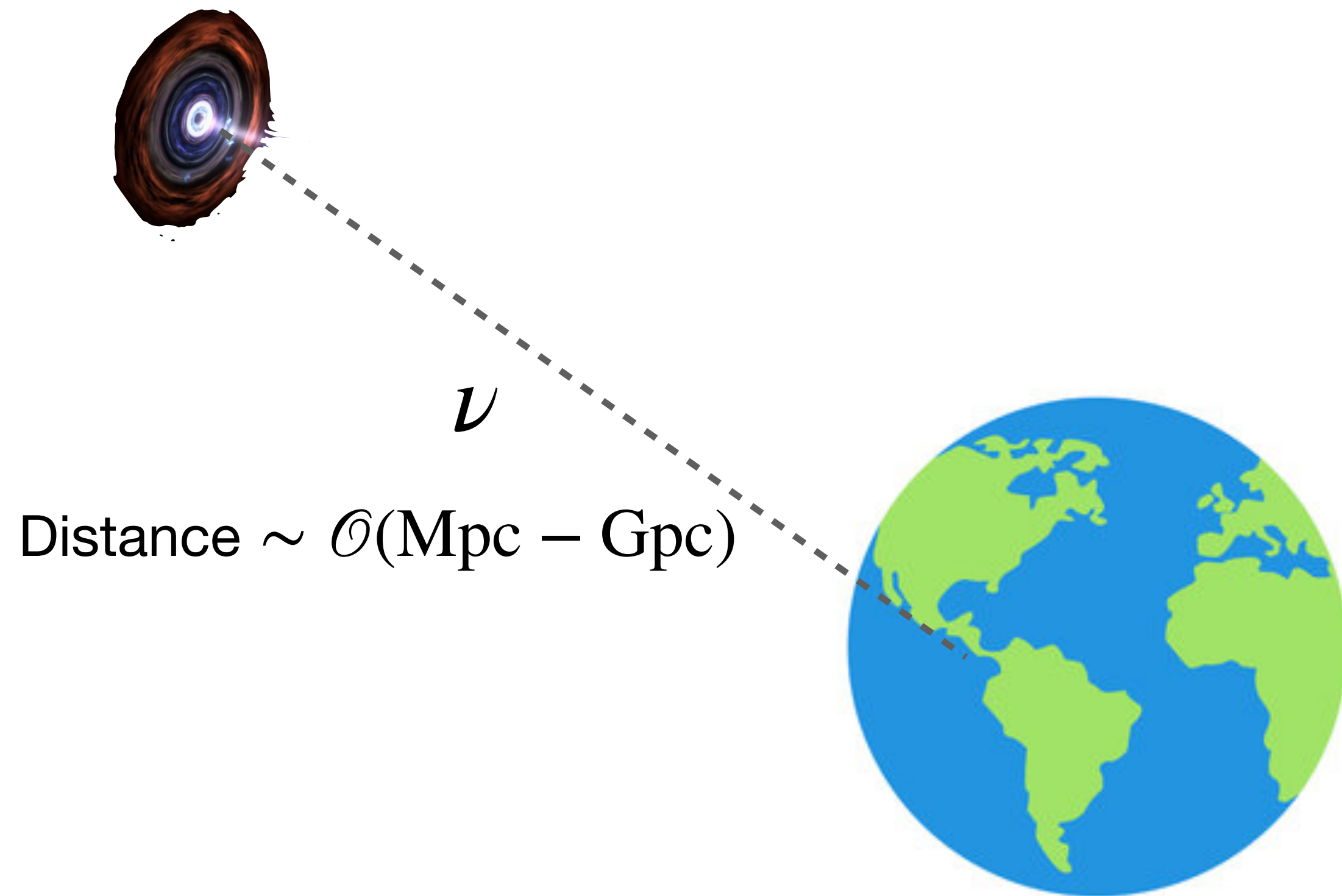
Atmospheric Neutrinos



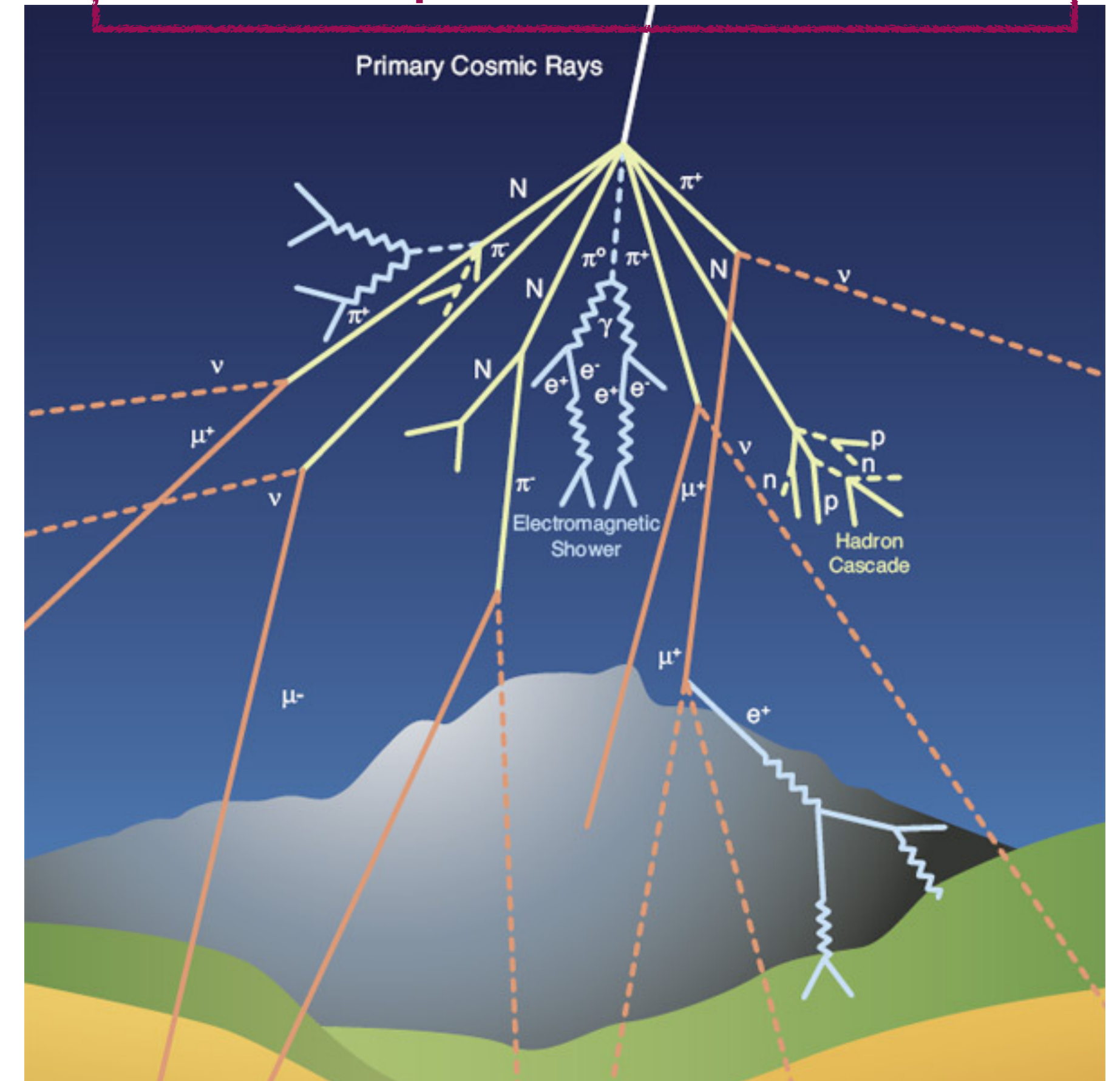
Src: CERN/Cosmic Rays Particles Outer Space

Astrophysical vs Atmospheric Neutrinos

Astrophysical Neutrinos



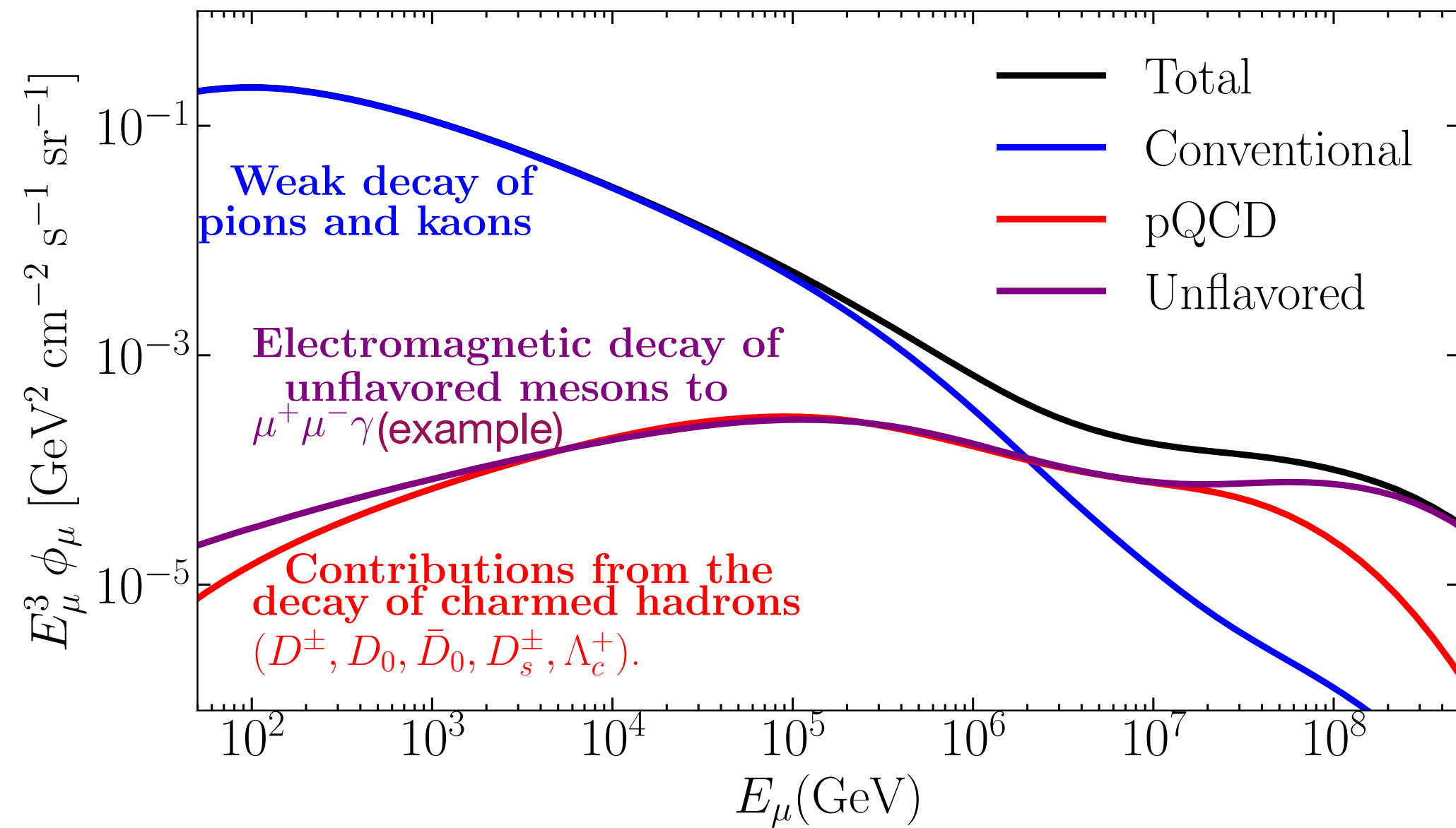
Atmospheric Neutrinos



Src: CERN/Cosmic Rays Particles Outer Space

Atmospheric Muons and Neutrinos

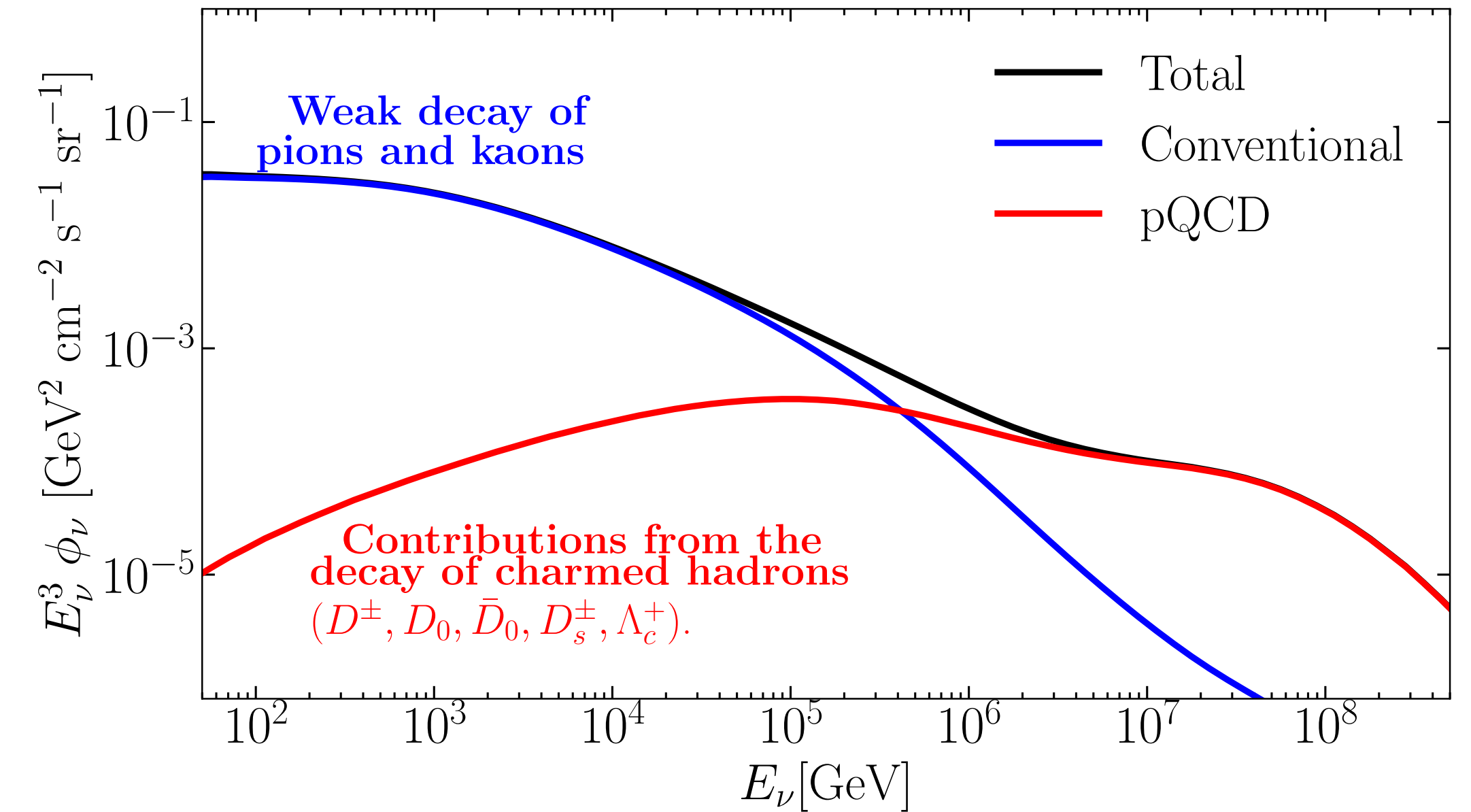
Muons



- $\phi_\mu = \phi_\mu^{\text{conv}} + \underbrace{\phi_\mu^{\text{pQCD}} + \phi_\mu^{\text{unfl}}}_{\text{prompt}}$
- Unflavored Mesons: $\eta, \eta', \phi, \rho^0, \omega, J/\psi$

$$\phi_\mu^{\text{pQCD}} \approx \phi_{\nu_\mu}^{\text{pQCD}}$$

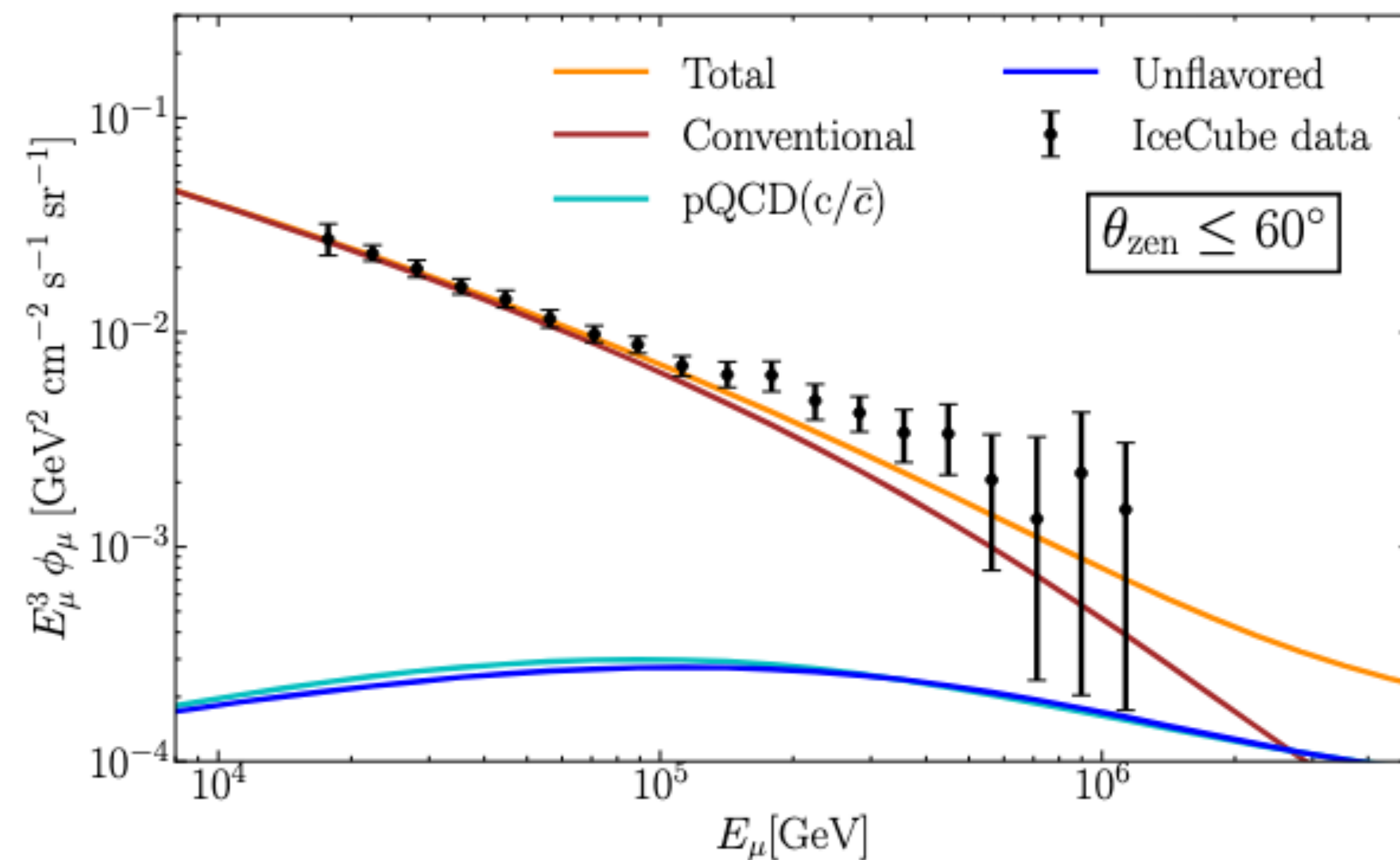
Muon Neutrinos



- $\phi_{\nu_\mu} = \phi_{\nu_\mu}^{\text{conv}} + \underbrace{\phi_{\nu_\mu}^{\text{pQCD}}}_{\text{prompt}}$

IceCube Experiment - Data and Limit

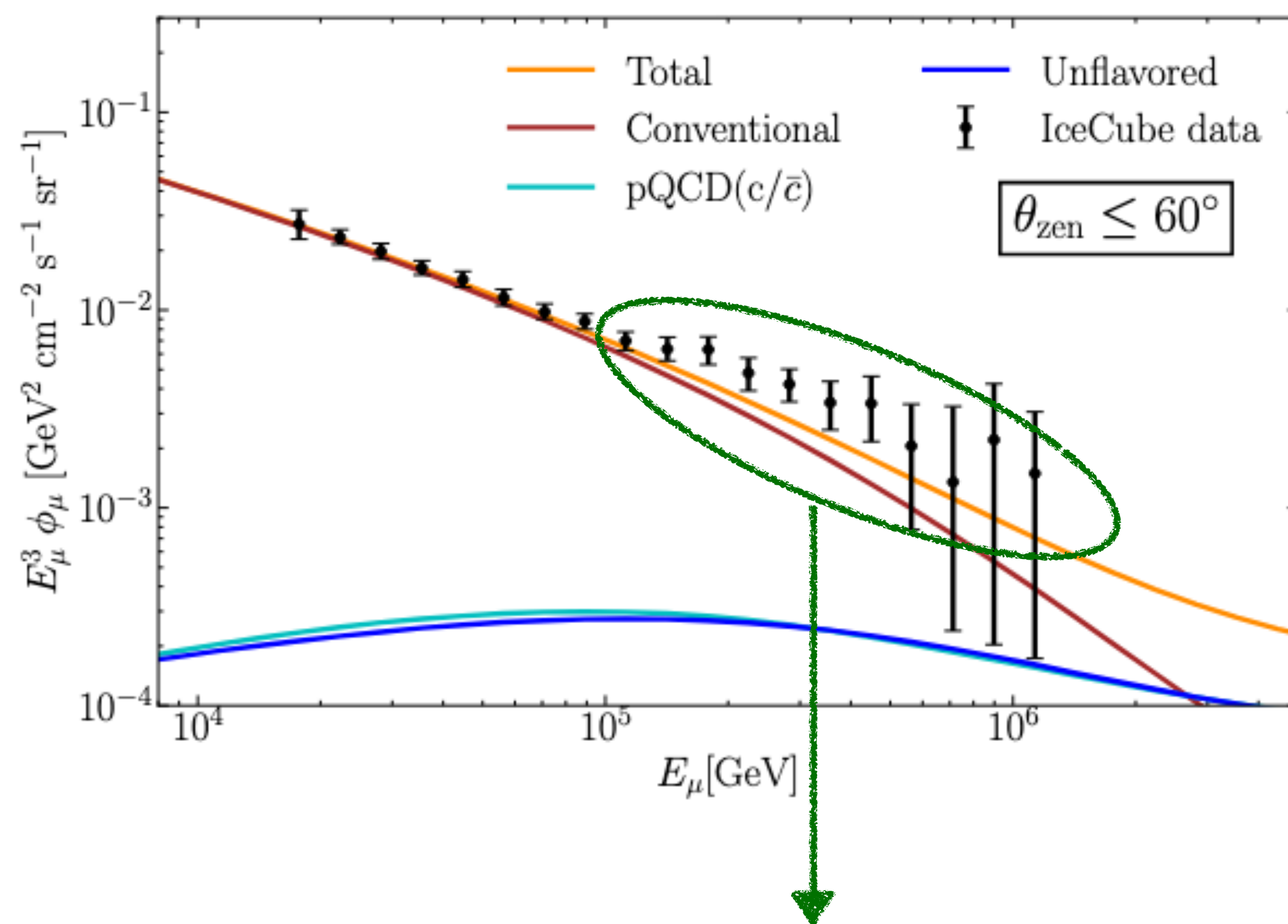
Muons



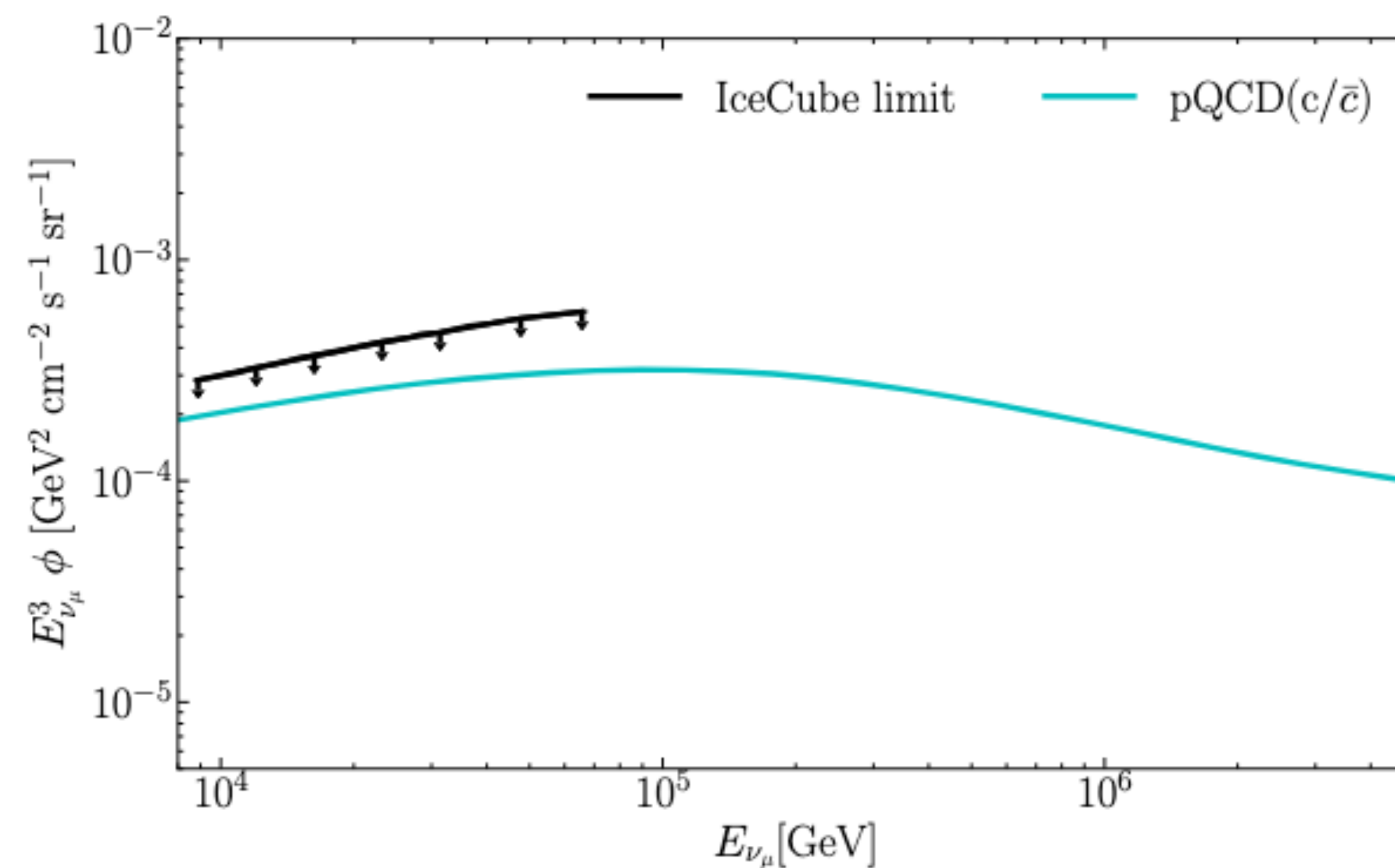
Muon data: MG Aartsen et al., Astropart.Phys. 78 (2016) 1-27

IceCube Experiment - Data and Limit

Muons



Muon Neutrinos



Main motivation: Add a new contribution to produce missing muon flux

Matrix Cascade Equations (MCEq) package

<https://github.com/mceq-project/MCEq>

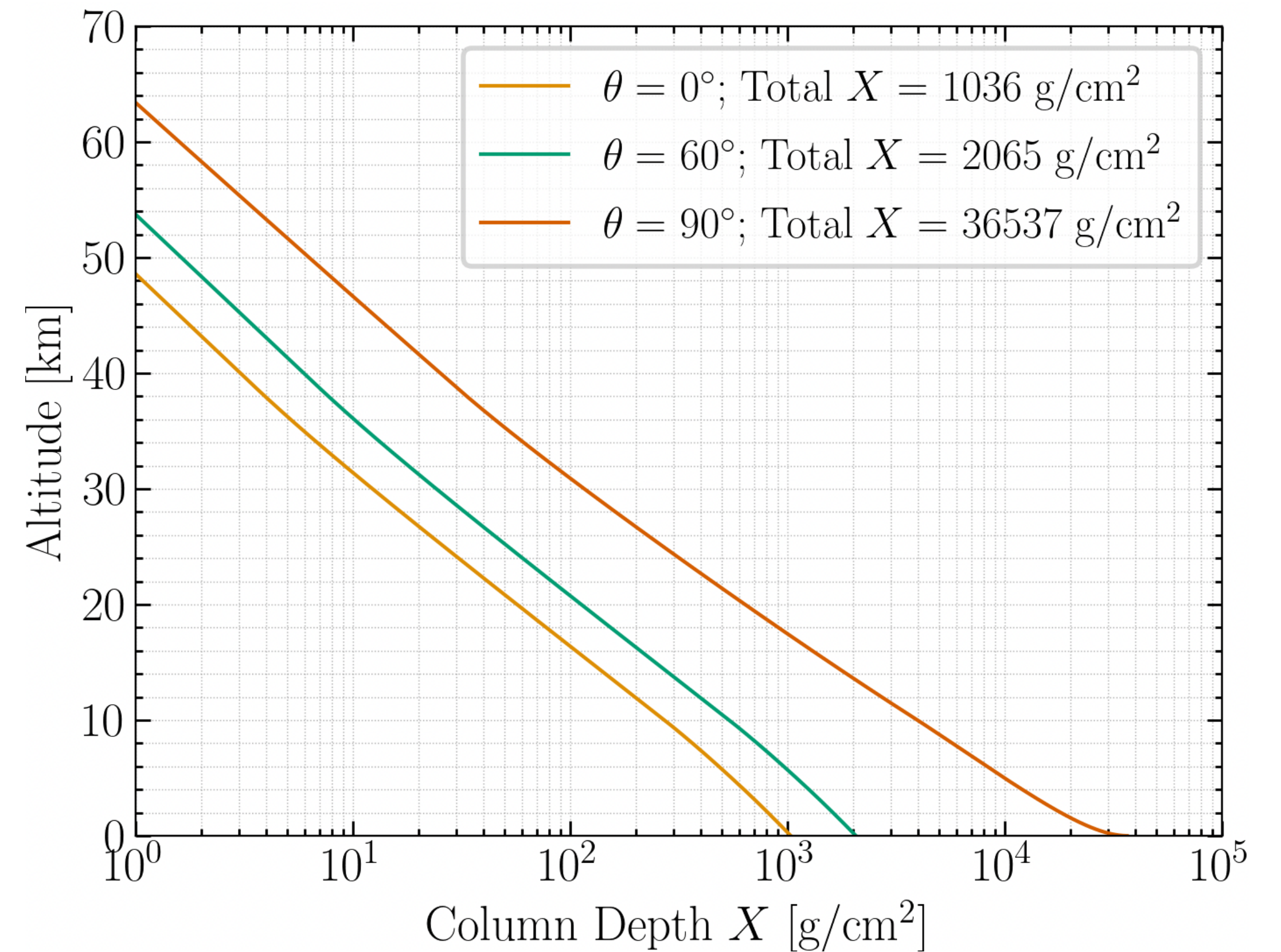
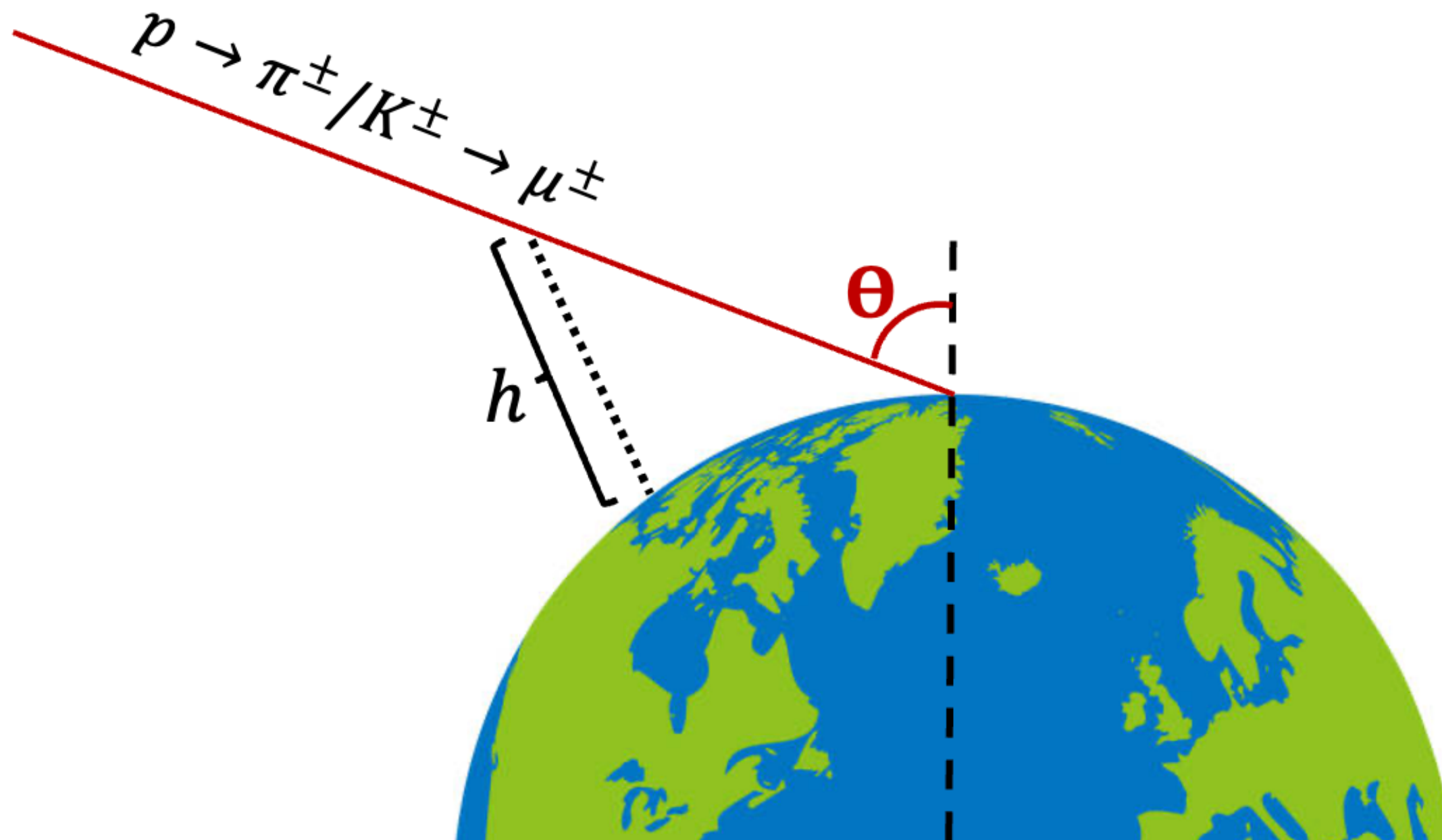
- US Standard Earth atmosphere^[1]
- Cosmic ray flux - Gaisser Hillas model H3a^[2]
- Hadronic interaction model - *SIBYLL2.3c*^[3]
- Continuous energy loss for particles considered.
- No Earth's magnetic field considered.

[1]: D. Heck et al., Tech. Rep. FZKA 6019, Karlsruhe (1998)

[2]: Gaisser, T.K., Astroparticle Physics 35, 801 (2012)

[3]: F. Riehn et al., PoS ICRC2017

Altitude vs Column Depth



$$\text{Column Depth: } X(l, \alpha) = \int_l^\infty dl' \rho(h(l', \alpha))$$

Cascade equations

To evaluate the flux of muons, we step through the column depth of the atmosphere with steps ΔX :

- Muon flux:

$$\phi_\mu(E, X + \Delta X) = \left[\underbrace{\phi_\mu(E', X)}_{\text{Muon flux at previous X step}} \underbrace{\left(1 - \frac{\Delta X}{\lambda_\mu^{\text{dec}}}\right)}_{\text{Loss from decay}} + \sum_{j=\pi, K, \dots} \underbrace{Z_{j \rightarrow \mu}}_{\text{Source term}} \phi_j(E', X) \frac{\Delta X}{\lambda_j^{\text{dec}}} \right] \exp(b \Delta X)$$

$$E' > E$$

Intrinsic Charm

- Non-perturbative fluctuations of proton and neutron.
 - $|uudc\bar{c}\rangle$ and $|uddc\bar{c}\rangle$
 - $pA \rightarrow \bar{D}^0 \Lambda_c^+ X$ and $nA \rightarrow D^- \Lambda_c^+ X$
- $\bar{D}^0 \rightarrow \mu^- + \bar{\nu}_\mu + X$
- $D^- \rightarrow \mu^- + \bar{\nu}_\mu + X$
- $\Lambda_c \rightarrow \mu^+ + \nu_\mu + X$

Intrinsic Charm production models

$$\frac{d\sigma_{p+\text{air} \rightarrow h_c}^{(\text{intr})}(E, x_{h_c})}{dx_{h_c}} = w_{\text{intr}}^c \sigma_{p-\text{air}}(E) f_{h_c}^{(\text{intr})}(x_{h_c}) \quad \text{where} \quad x_{h_c} = \frac{E_{h_c}}{E_p}$$

- Regge fragmentation functions [1]:

$$f_{h_c}^{\text{intr}}(x) = N_{\text{intr}} x^{-a_\psi} (1-x)^{-a_\psi+2(1-a_N)}$$

$$N_{\text{intr}} = \frac{\Gamma(-2a_\psi + 4 - 2a_N)}{\Gamma(-a_\psi + 1)\Gamma(-a_\psi + 3 - 2a_N)}$$

[1]: A.B. Kaidalov et al., Z.Phys. C 30 (1986) 145

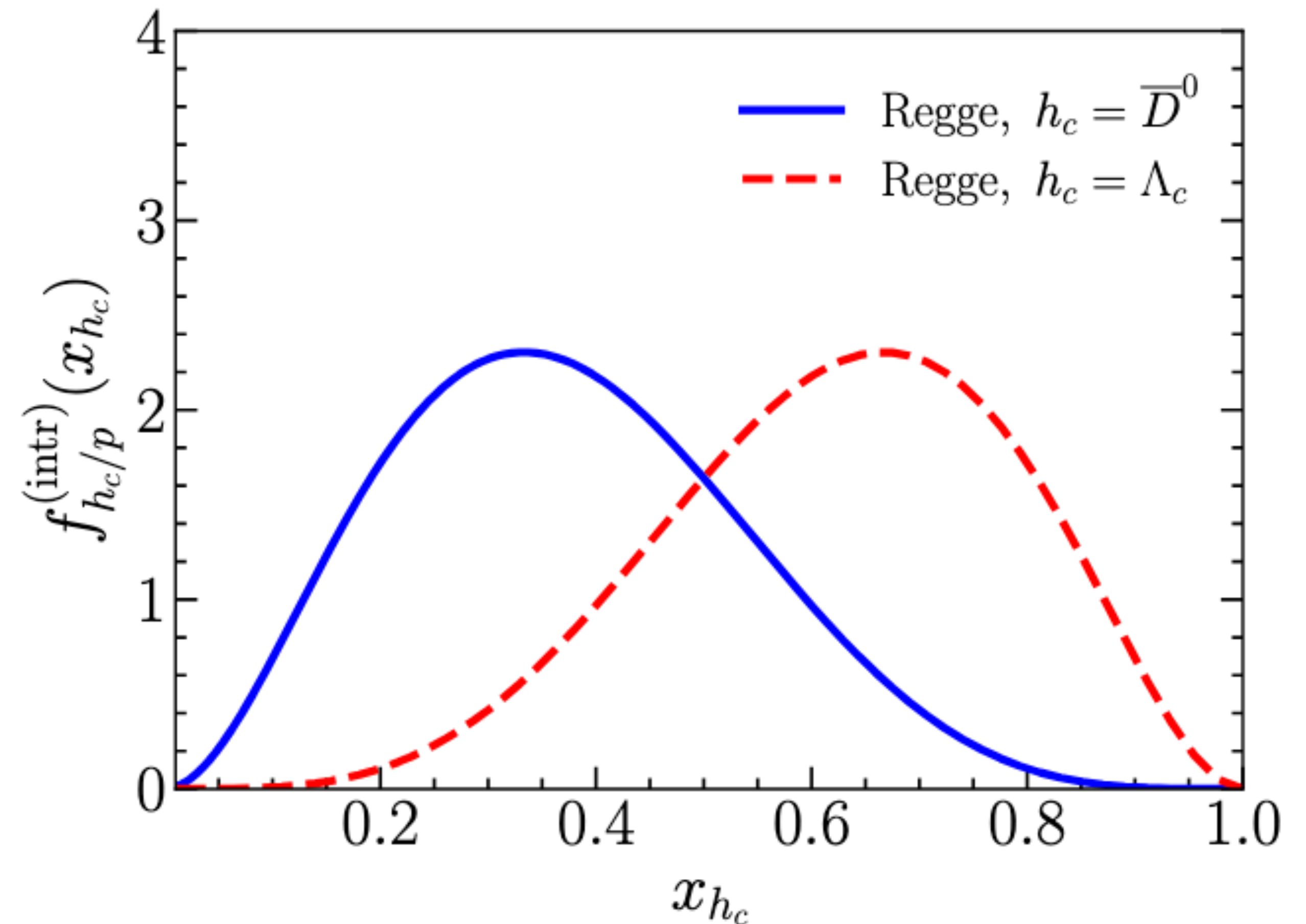
Intrinsic Charm production models

Regge formulation with $a_\psi = -2$ and $a_N = -0.5$

- For Regge Model:

$$f_{D^-}^{(\text{intr})}(x_D) = f_{\bar{D}^0}^{(\text{intr})}(x_D)$$

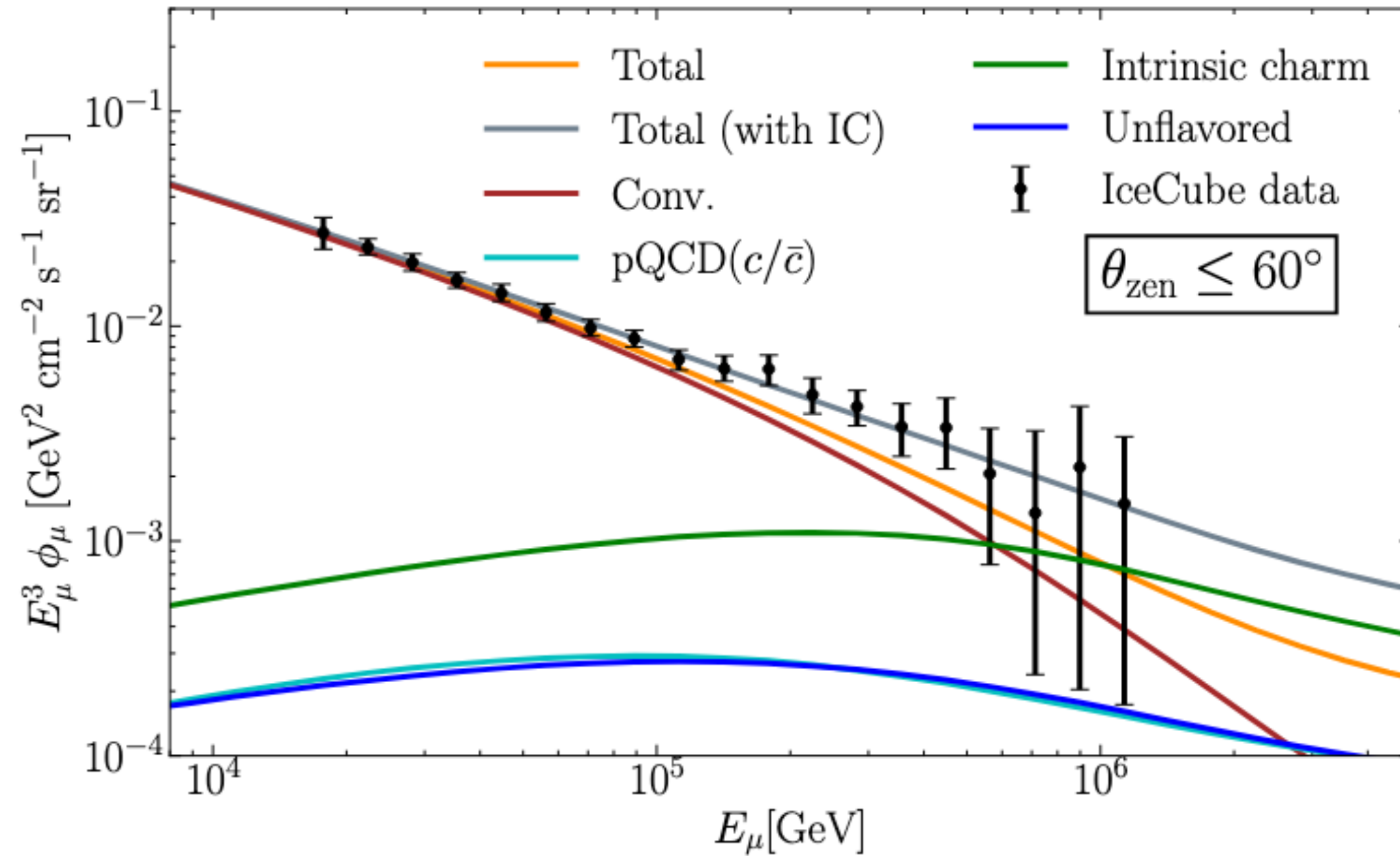
$$f_{\Lambda_c}^{(\text{intr})}(x_\Lambda) = f_{\bar{D}^0}^{(\text{intr})}(1 - x_\Lambda)$$



Muon flux with Intrinsic Charm

Regge formulation with $a_\psi = -2$ and $a_N = -0.5$

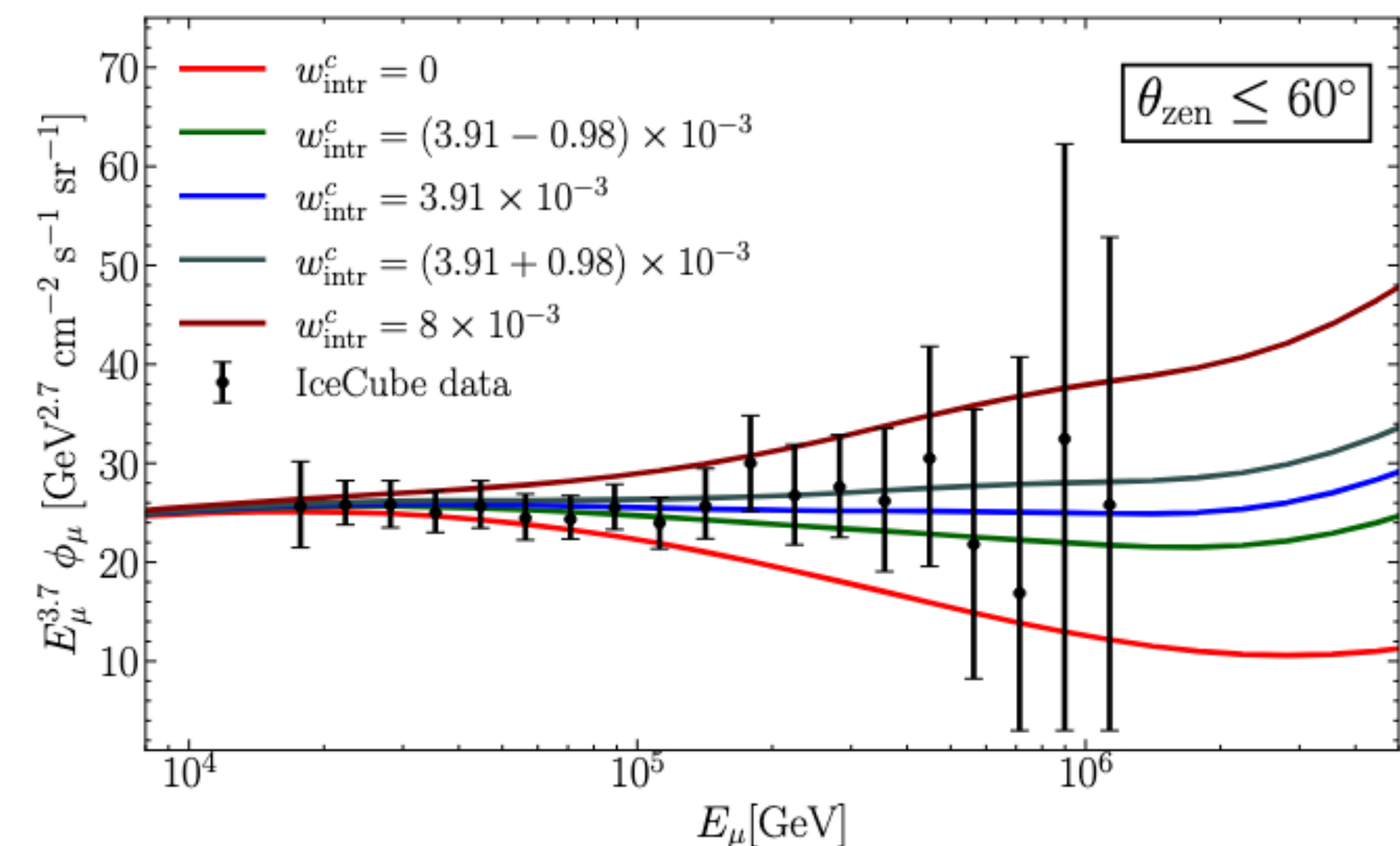
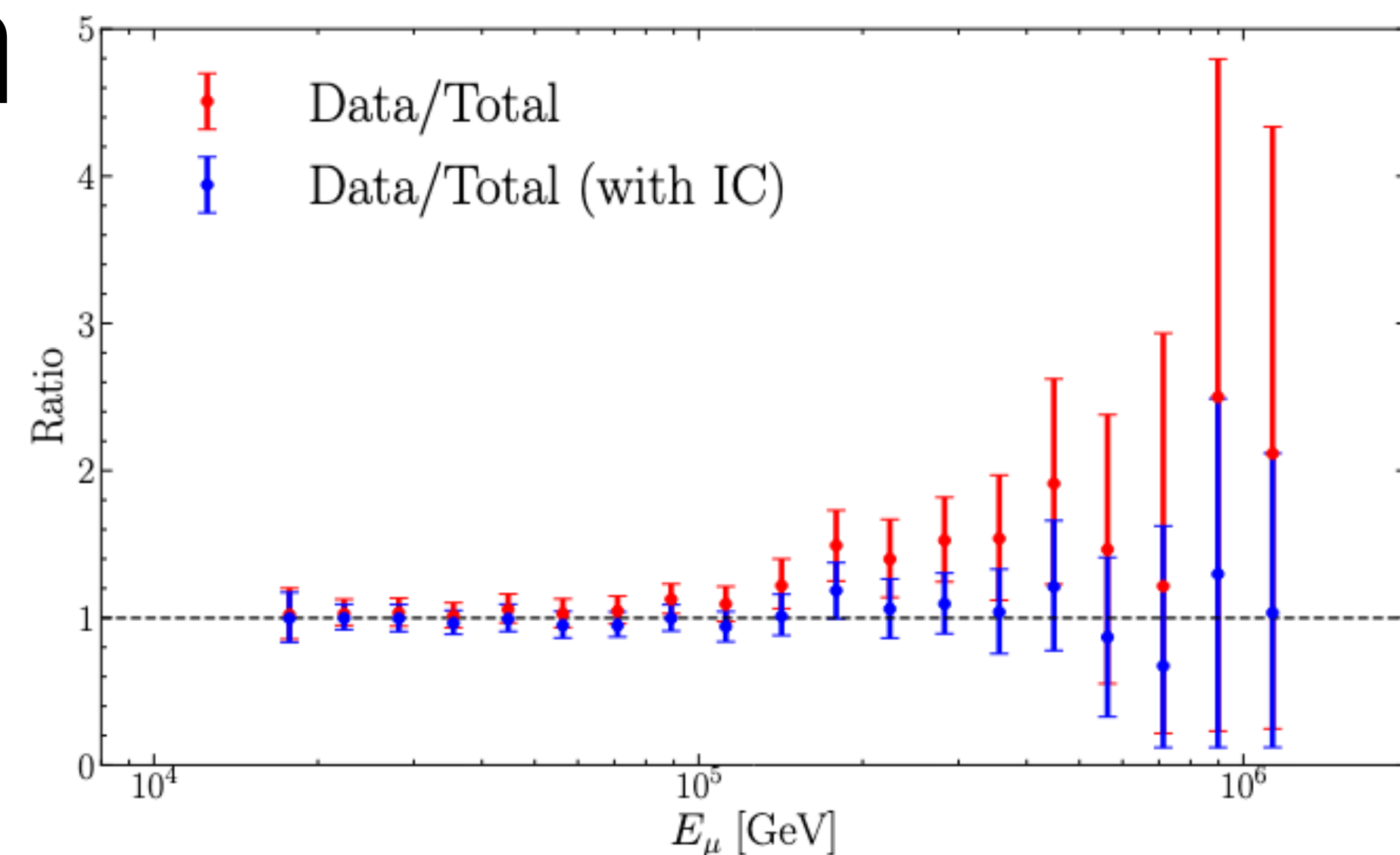
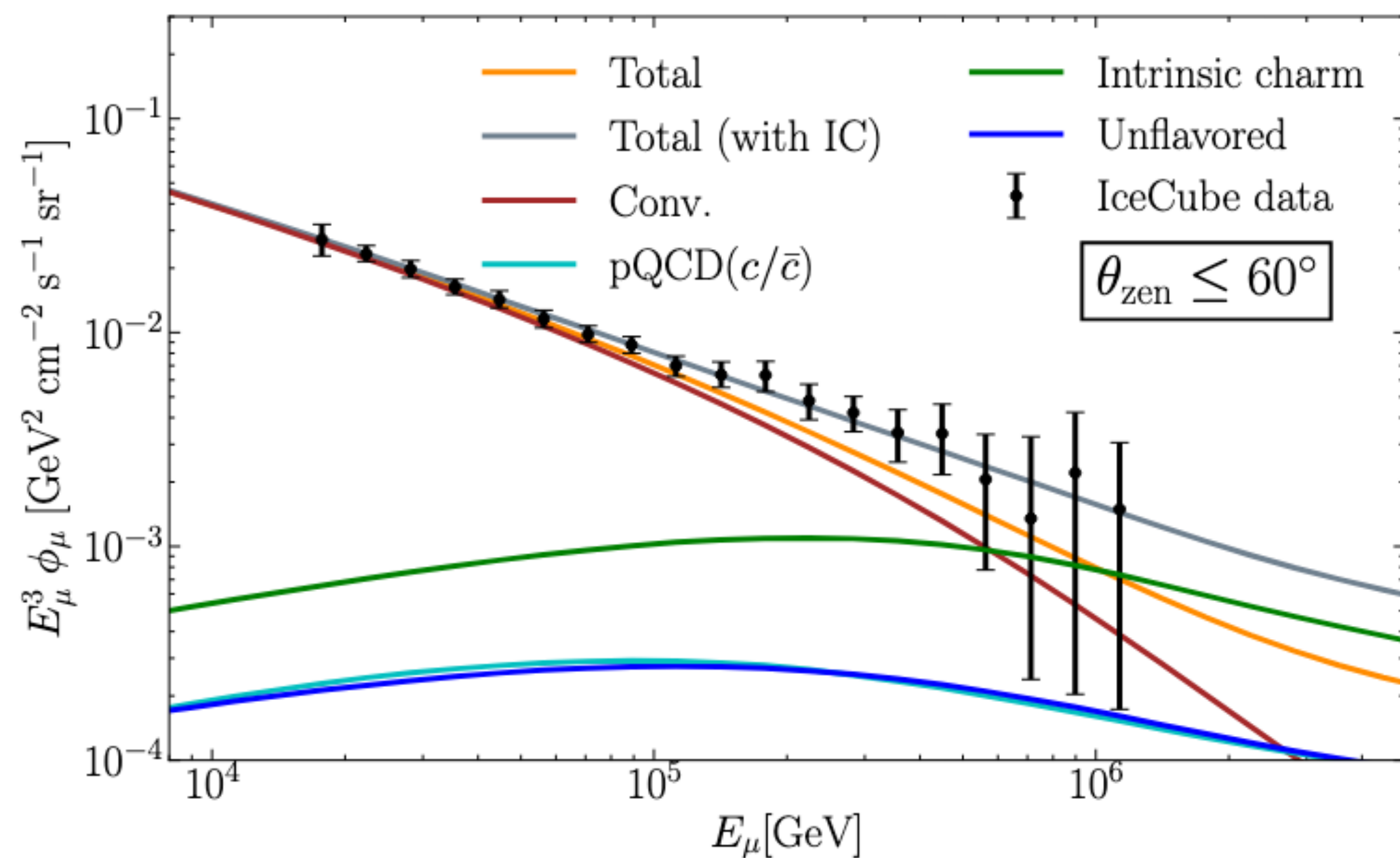
$$w_c^{intr} = 3.91 \times 10^{-3}$$



Muon flux with Intrinsic Charm

Regge formulation with $a_\psi = -2$ and $a_N = -0.5$

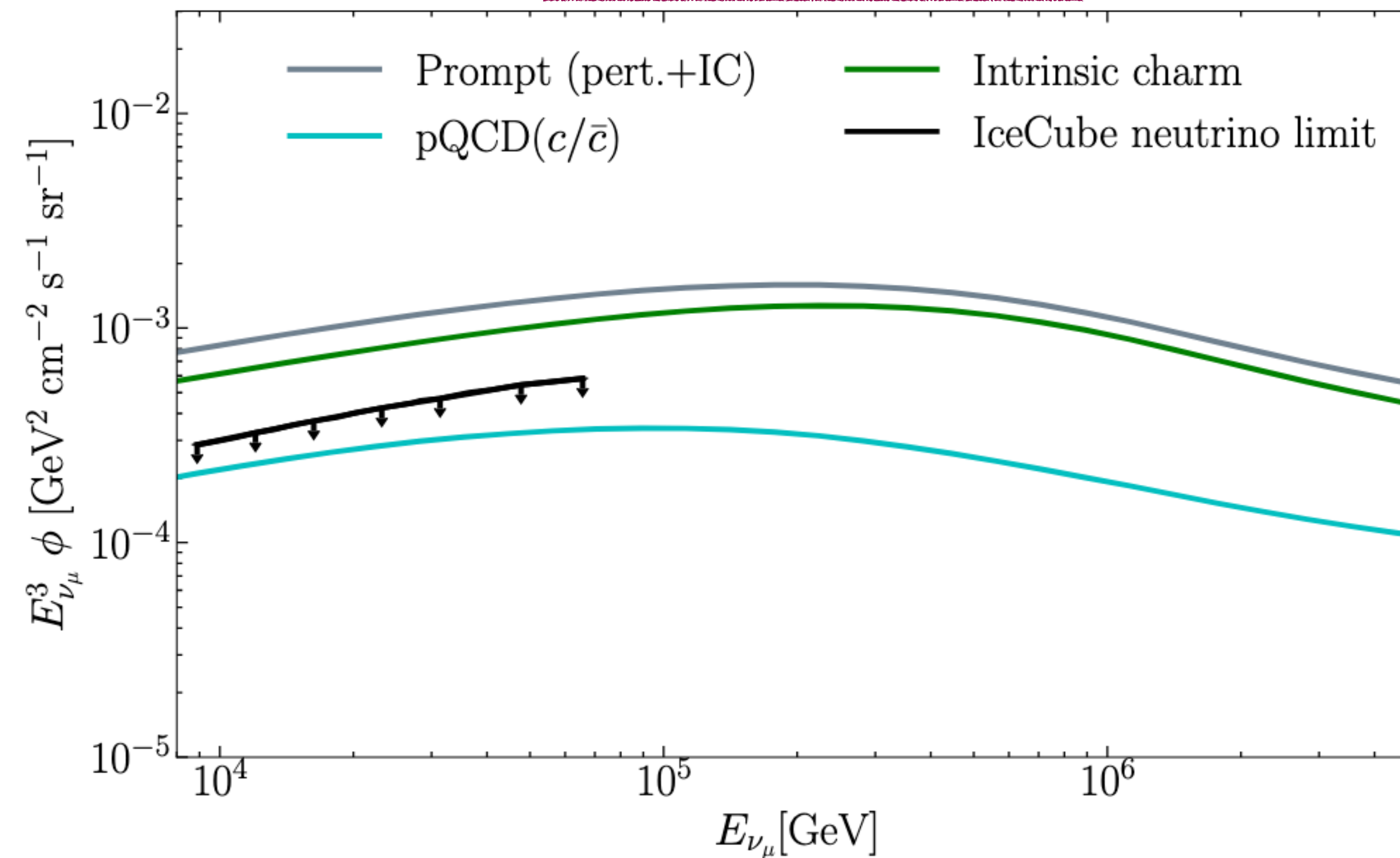
$$w_c^{intr} = 3.91 \times 10^{-3}$$



Muon Neutrino flux

Regge formulation with $a_\psi = -2$ and $a_N = -0.5$

$$w_c^{intr} = 3.91 \times 10^{-3}$$



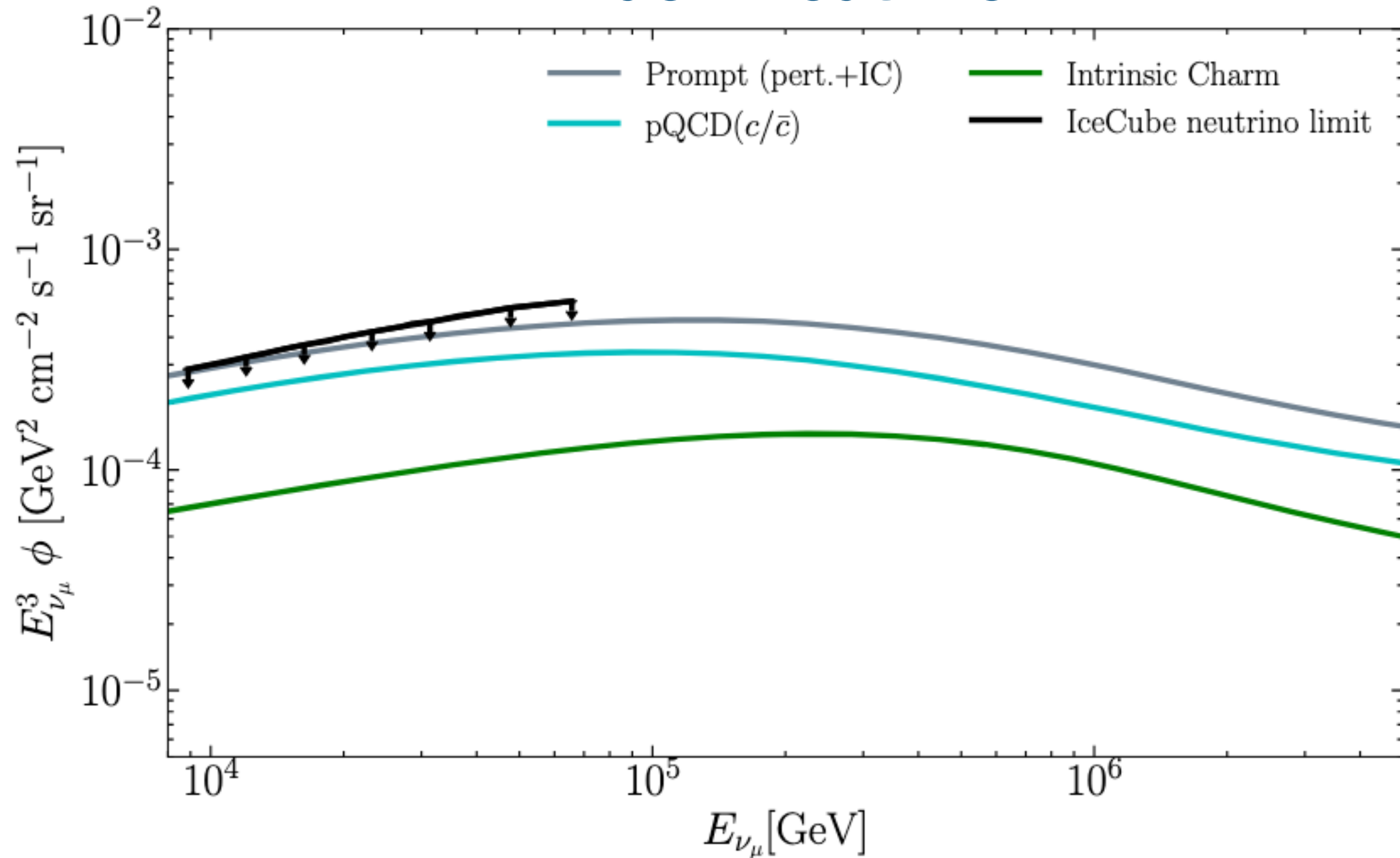
Overshoots the upper bound!

Fitting Muon Neutrino flux limit first

Regge formulation with $a_\psi = -2$ and $a_N = -0.5$

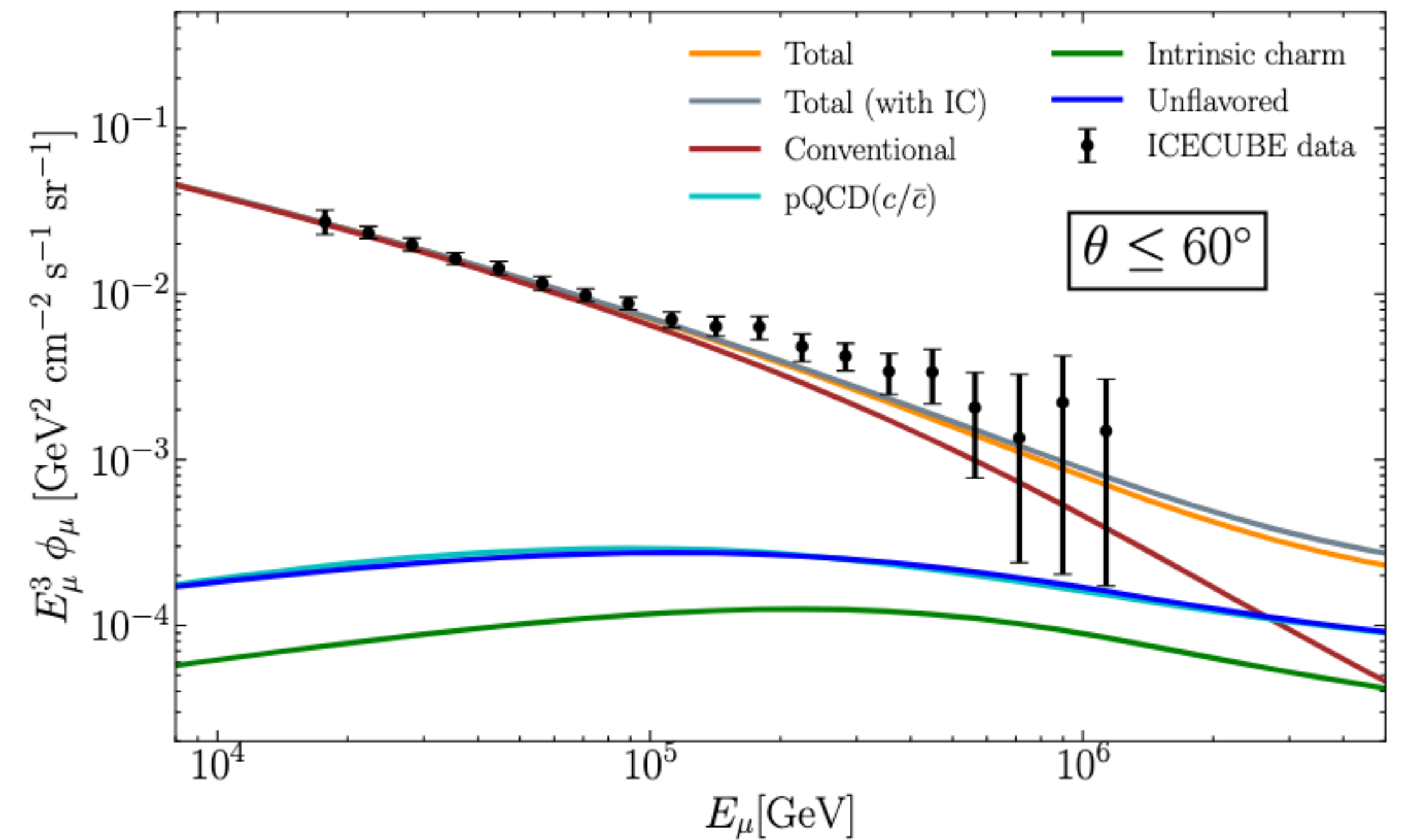
Undershoots the data!

Muon Neutrino



$$w_c^{intr} = 4.46 \times 10^{-4}$$

Muon

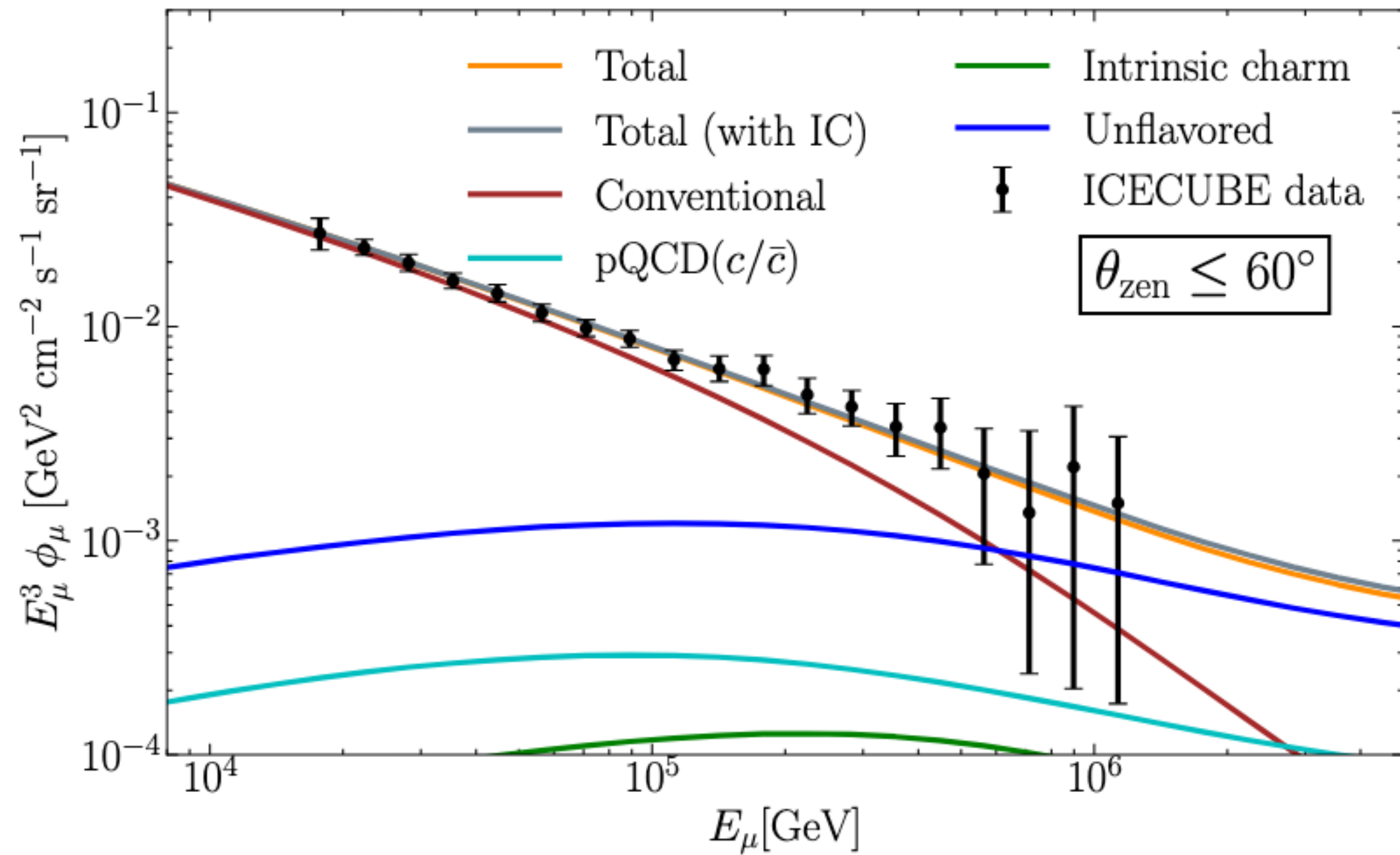


$$w_c^{intr} = 4.46 \times 10^{-4}$$

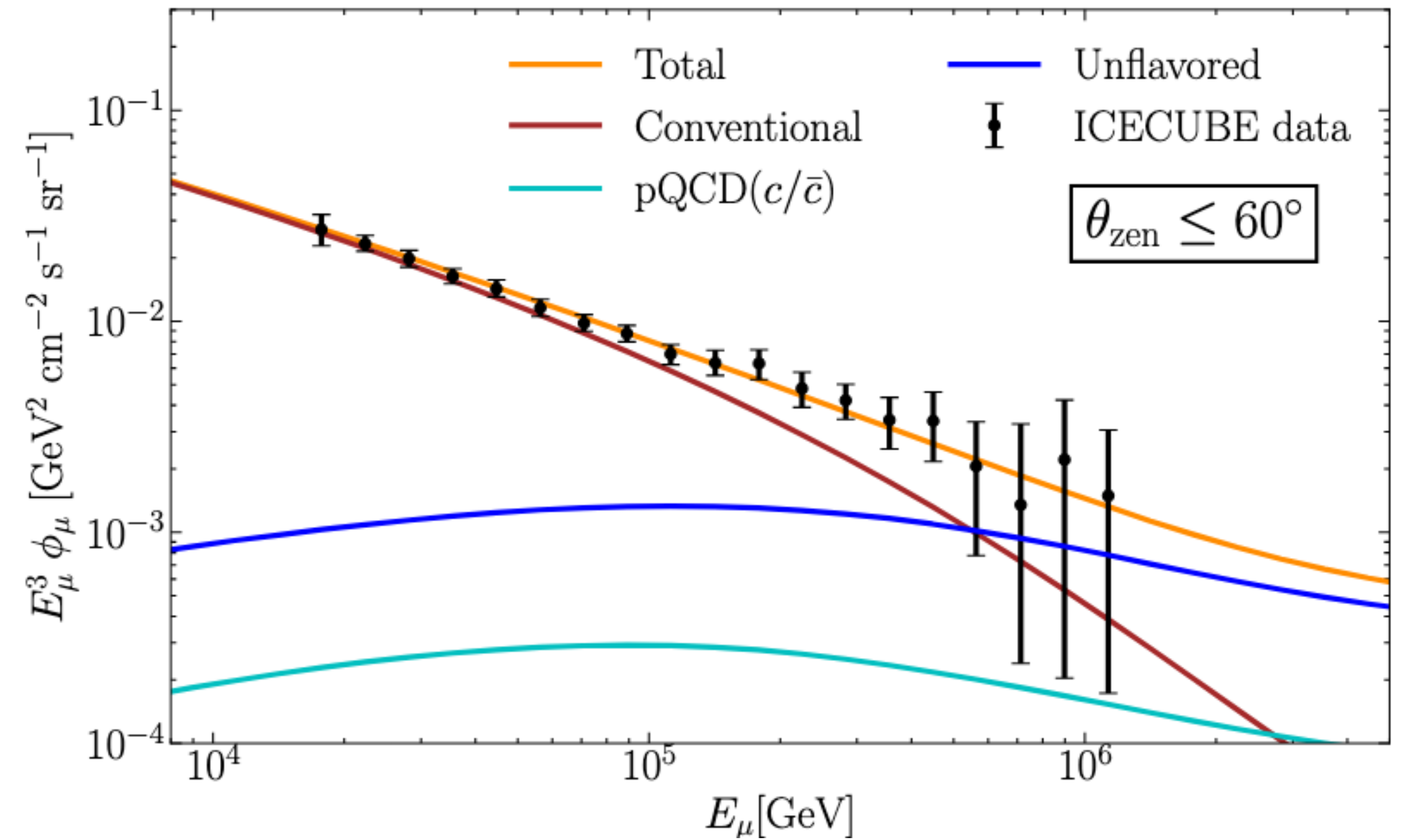
Unflavored mesons

For muon flux

Regge formulation with $a_\psi = -2$ and $a_N = -0.5$



$$w_c^{intr} = 4.46 \times 10^{-4} \text{ and } \alpha_{\text{unfl}} = 4.39$$



$$w_c^{intr} = 0 \text{ and } \alpha_{\text{unfl}} = 4.84$$

Uncertainties in Prompt flux

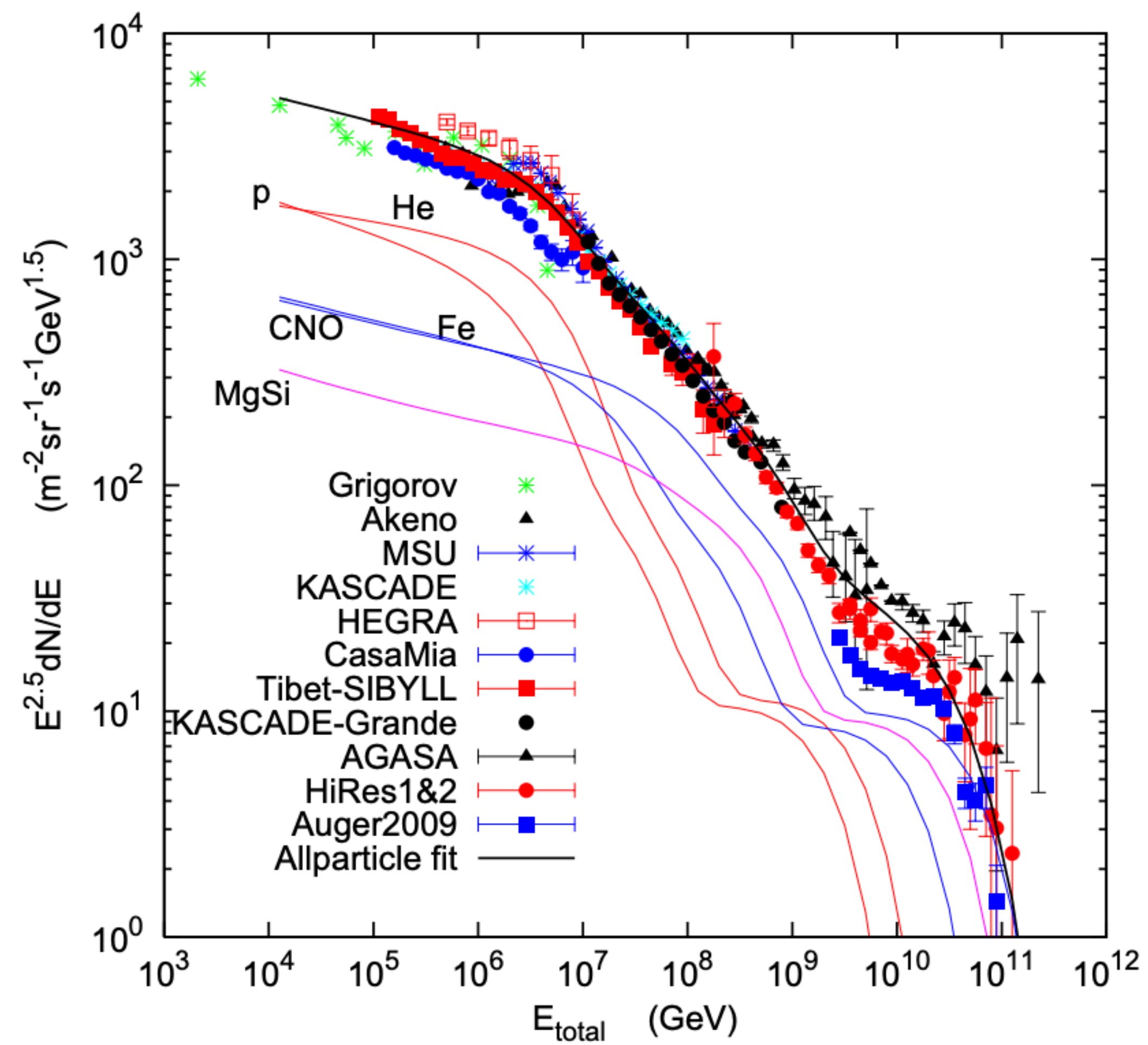
1. Since, $\phi_{\nu_{\mu}, \text{pQCD}} \simeq \phi_{\mu, \text{pQCD}}$, to reach neutrino upper bound: $\sim 1.4\phi_{\mu, \text{pQCD}}$.
 - From unflavored meson decays $\sim 4.4\phi_{\mu, \text{unfl}}$
 - Large enhancement of forward unflavored meson production in *p-air* collisions at high energies required in modeling to make up this gap.
2. Neutrino upper limit: can be relaxed.
3. Other hadronic interaction models for unflavored meson contributions to $\mu^+\mu^-$:
 - comparable *DPMJET-III* and *EPOS LHC* to *SIBYLL2.3c*.
 - lower *QGSJET-II* and *QGSJET-III* than *SIBYLL2.3c*.

Summary

- IceCube data exists for atmospheric muons and upper bound on prompt muon neutrino.
- With $w_c^{\text{intr}} = 3.91 \times 10^{-3}$: best fit for Muon IceCube data but overshoot the prompt muon neutrino upper limit.
- With $w_c^{\text{intr}} = 4.46 \times 10^{-4}$: best fit for Muon neutrino upper bound but fall short for muon data.
- Another possibility is changing unflavored contribution to atmospheric muons $\alpha^{\text{unfl}} = 4.4 - 4.8$.
- Neutrino upper limit can be relaxed based on uncertainties in the prompt production.

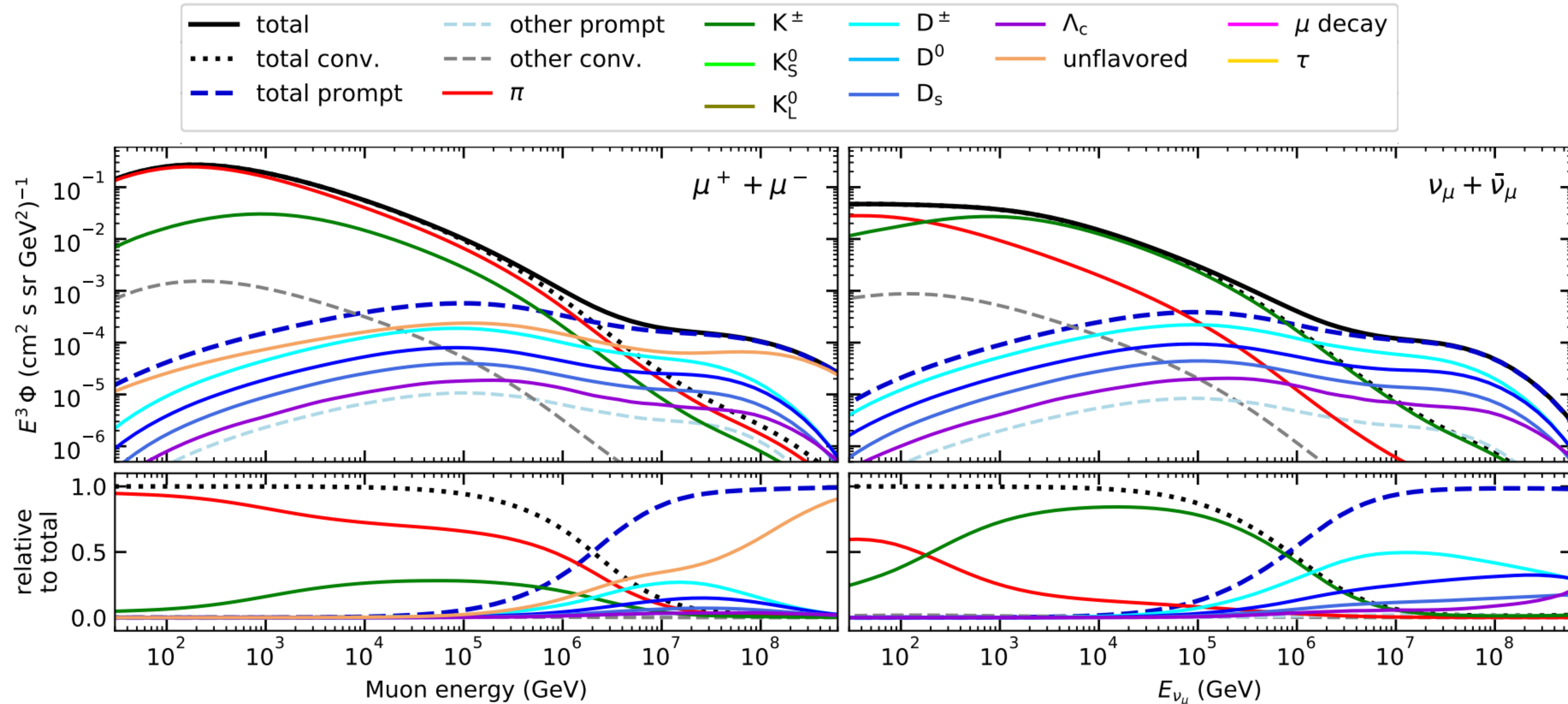
Backup slides

CR flux - H3a



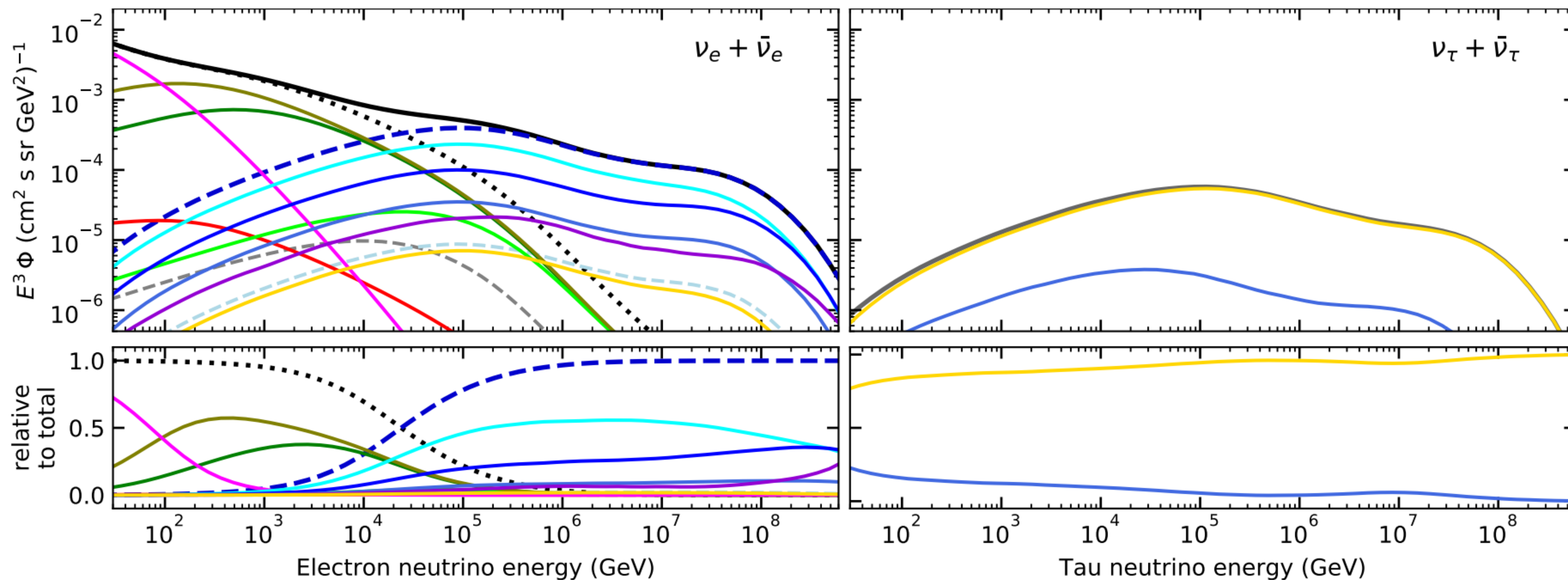
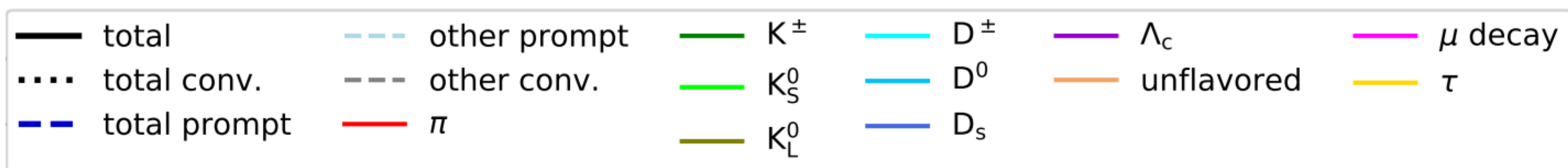
MCEq Flux - Muons and Muon neutrinos

<https://arxiv.org/pdf/1806.04140>



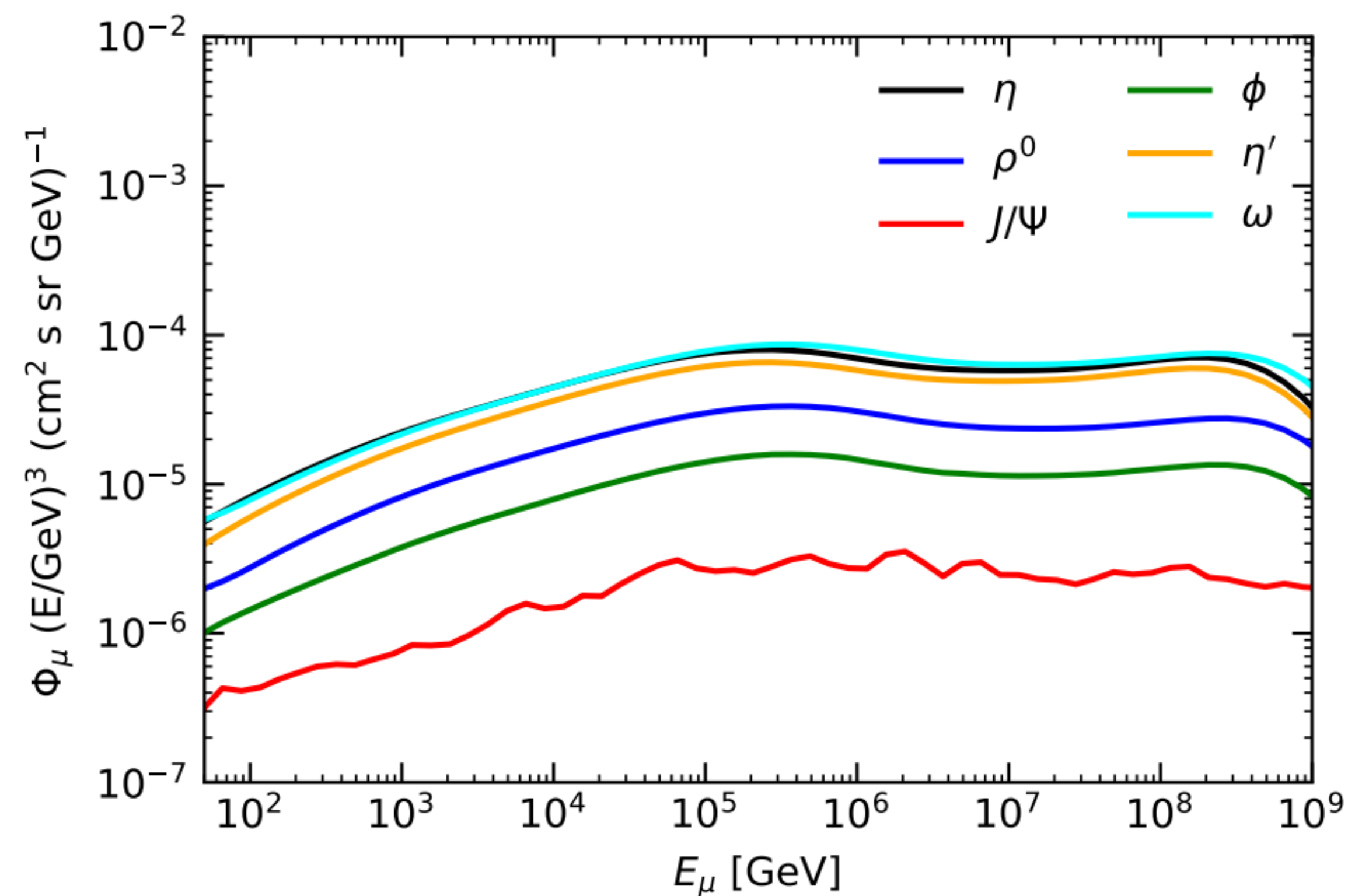
MCEq Flux - Electron and Tau neutrinos

<https://arxiv.org/pdf/1806.04140>



MCEq - Unflavored Mesons

<https://arxiv.org/pdf/1806.04140>



Cascade equations

To evaluate the flux of muons, we step through the column depth of the atmosphere with steps ΔX :

- Muon flux:

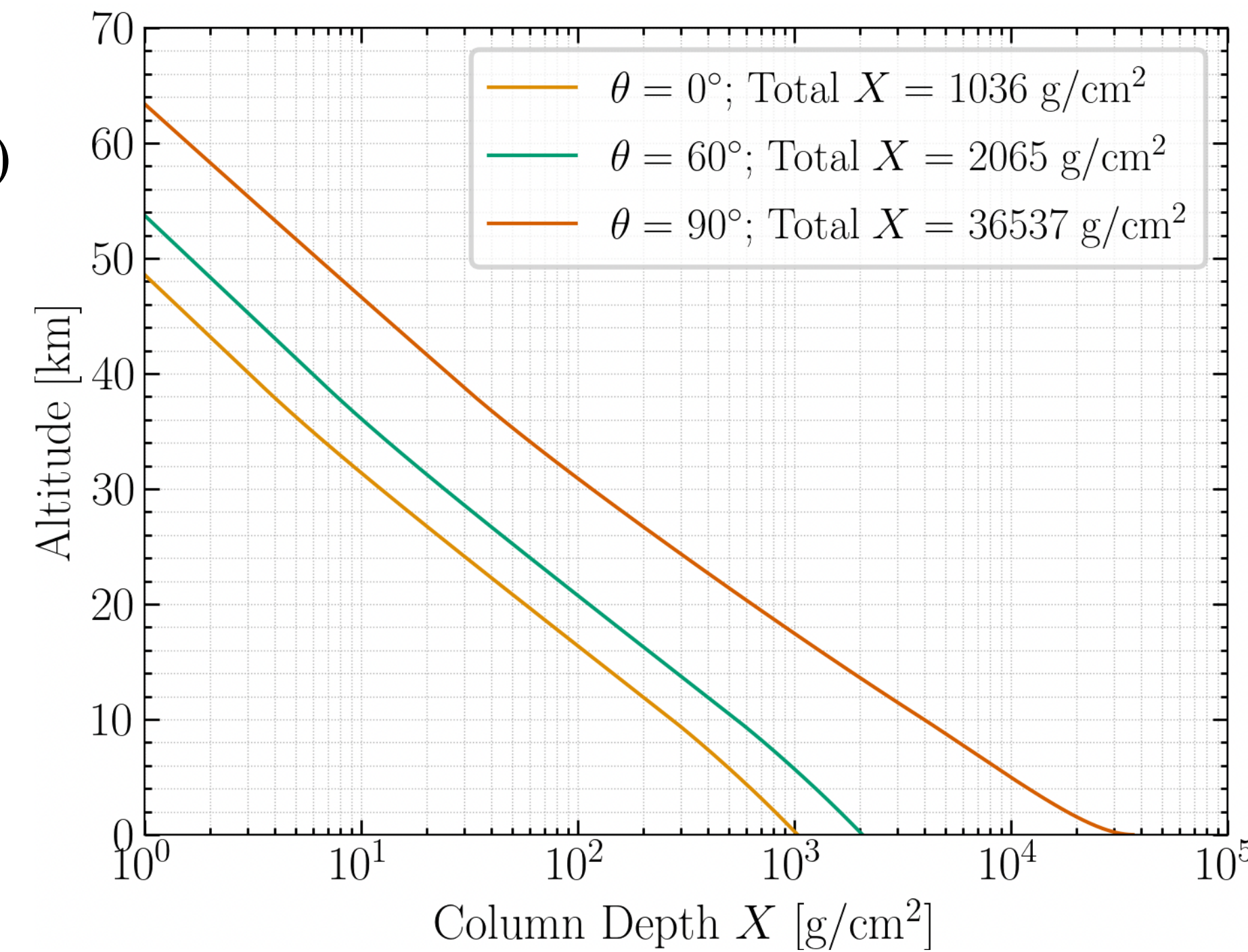
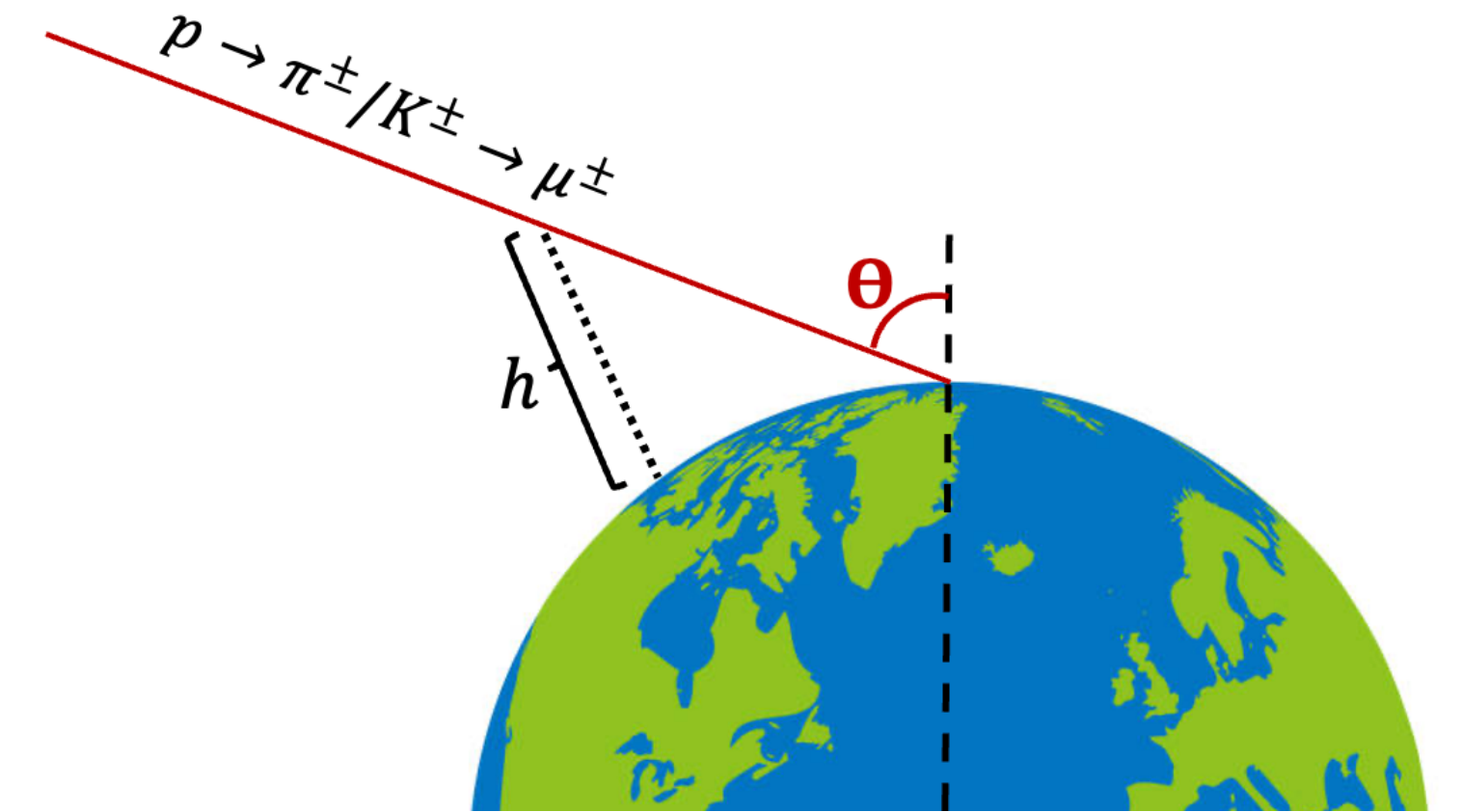
$$\phi_{\mu}(E, X + \Delta X) = \left[\phi_{\mu}(E', X) \left(1 - \frac{\Delta X}{\lambda_{\mu}^{\text{dec}}} \right) + Z_{\pi/K \rightarrow \mu}^{\text{dec}} \phi_{\pi/K}(E', X) \frac{\Delta X}{\lambda_{\pi/K}^{\text{dec}}} \right] \exp(b\Delta X)$$

- Meson flux like Pion and Kaon:

$$\phi_{\pi/K}(E, X + \Delta X) = \phi_{\pi/K}(E, X) \left(1 - \frac{\Delta X}{\lambda_{\pi/K}^{\text{dec}}} \right) + Z_{CR \rightarrow \pi/K} \phi_{CR}(E, X) \frac{\Delta X}{\lambda_{CR}}$$

- Cosmic ray flux:

$$\phi_{CR}(E, X + \Delta X) = \phi_{CR}(E, X) \left(1 - \frac{\Delta X}{\Lambda_{CR}} \right)$$



Z-moments

$$Z(k \rightarrow j) = \left[\int_E^\infty dE' \frac{\phi_k(E', X)}{\phi_k(E, X)} \frac{\lambda_k(E)}{\lambda_k(E')} \frac{dn(k \rightarrow j; E', E)}{dE} \right] \frac{\phi_k(E, X)}{\lambda_k(E)}$$

$$Z(CR \rightarrow IC) = w_{intr}^c \left[\int_0^1 \frac{dx}{x} \frac{\phi_{CR}(E_{CR}, X)}{\phi_{CR}(E_{IC}, X)} \frac{\lambda_{CR}(E_{IC})}{\lambda_{CR}(E_{CR})} \frac{dn(CR \rightarrow IC; E_{CR}, E_{IC})}{dx} \right] \frac{\phi_{CR}(E_{IC}, X)}{\lambda_{CR}(E_{IC})}$$

$$Z(h \rightarrow \mu) = \left[\int_{E_\mu}^\infty dE_h \frac{\phi_h(E_h, X)}{\phi_h(E_\mu, X)} \frac{\lambda_h^{dec}(E_\mu)}{\lambda_h^{dec}(E_h)} \frac{dn(h \rightarrow \mu; E_h, E_\mu)}{dE_\mu} \right] \frac{\phi_h(E_\mu, X)}{\lambda_h(E_\mu)}$$

Branching ratio and Fragmentation functions

Charmed hadrons

- $\bar{D}^0 \rightarrow \mu^- + \bar{\nu}_\mu + X$ BR = 7%
- $D^- \rightarrow \mu^- + \bar{\nu}_\mu + X$ BR = 17.6%
- $\Lambda_c \rightarrow \mu^+ + \nu_\mu + X$ BR = 4.5%

Particle	N	B_c	ϵ
D^0	0.577	0.606	0.101
D^+	0.238	0.244	0.104
D_s^+	0.0327	0.081	0.0322
Λ_c^+	0.0067	0.061	0.00418

D0 (c ubar)

D+ (c dbar)

Lambda_c (udc)

Splitting functions for HLM model

- Splitting functions for charmed baryon-meson states (HLM [2])

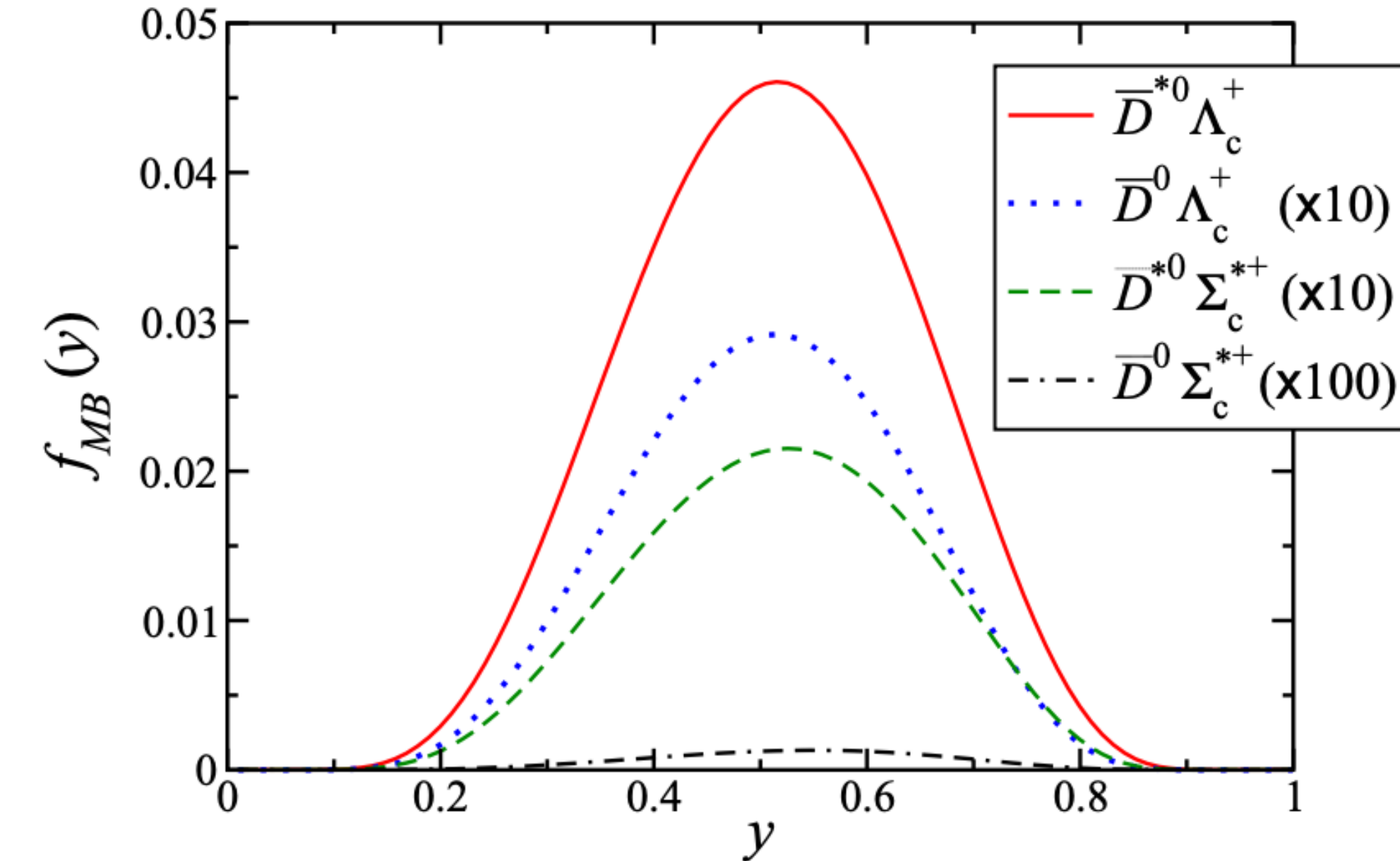
$$f_{D^*B}(y) = T_B \frac{1}{16\pi^2} \int \frac{dk_\perp^2}{y(1-y)} \frac{|F(s)|^2}{(s-M^2)^2} \times \left[g^2 G_v(y, k_\perp^2) + \frac{gf}{M} G_{vt}(y, k_\perp^2) + \frac{f^2}{M^2} G_t(y, k_\perp^2) \right], \quad (19)$$

where

$$G_v(y, k_\perp) = -6MM_B + \frac{4(P \cdot k)(p \cdot k)}{m_D^2} + 2P \cdot p, \quad (20a)$$

$$G_{vt}(y, k_\perp) = 4(M + M_B)(P \cdot p - MM_B) - \frac{2}{m_D^2} [M_B(P \cdot k)^2 - (M + M_B)(P \cdot k)(p \cdot k) + M(p \cdot k)^2], \quad (20b)$$

$$G_t(y, k_\perp) = -(P \cdot p)^2 + (M + M_B)^2 P \cdot p - MM_B(M^2 + M_B^2 + MM_B) + \frac{1}{2m_D^2} [(P \cdot p - MM_B)[(P - p) \cdot k]^2 - 2(M_B^2 P \cdot k - M^2 p \cdot k)[(P - p) \cdot k] + 2(P \cdot k)(p \cdot k)(2P \cdot k - M_B^2 - M^2)], \quad (20c)$$



- For HLM Model:

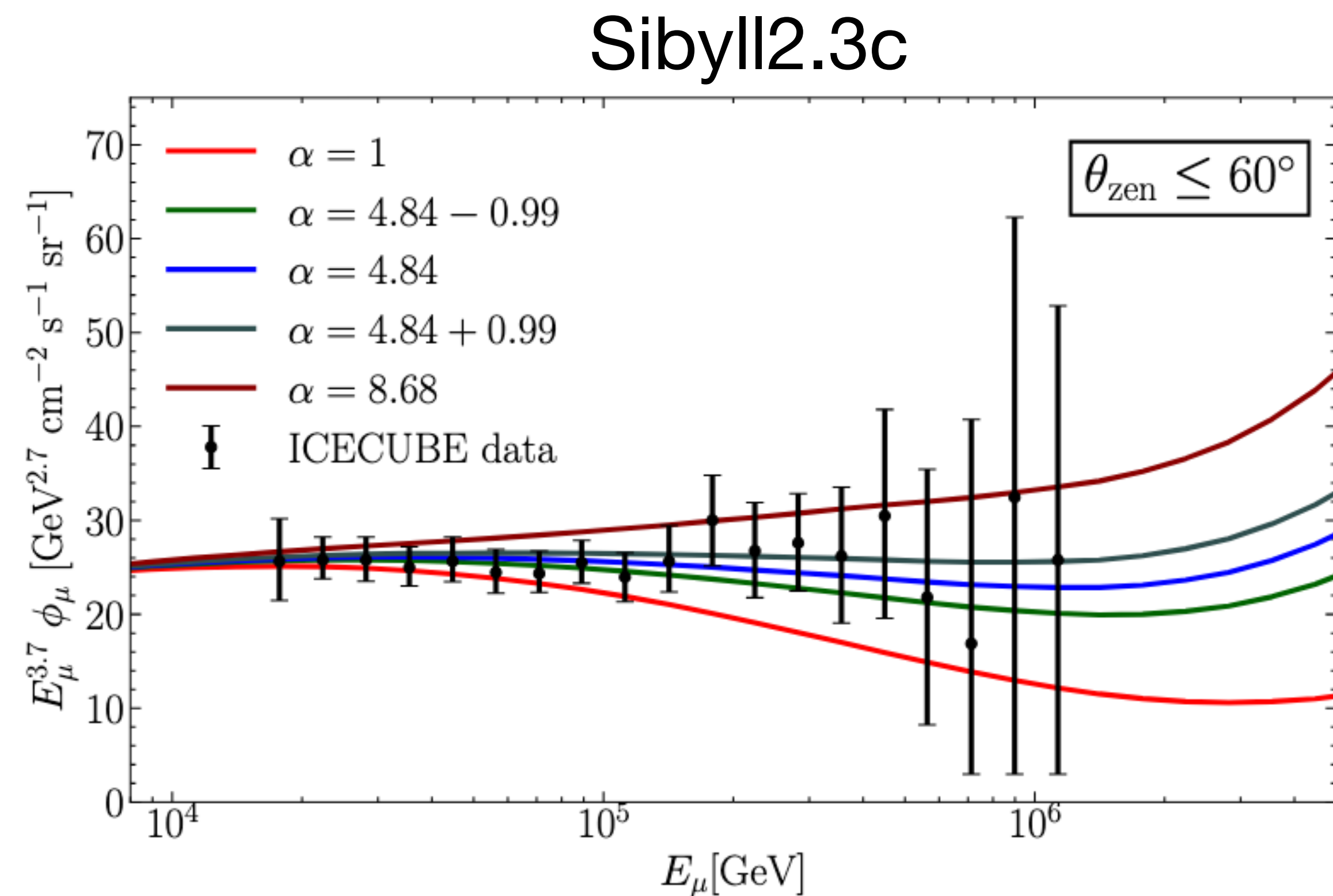
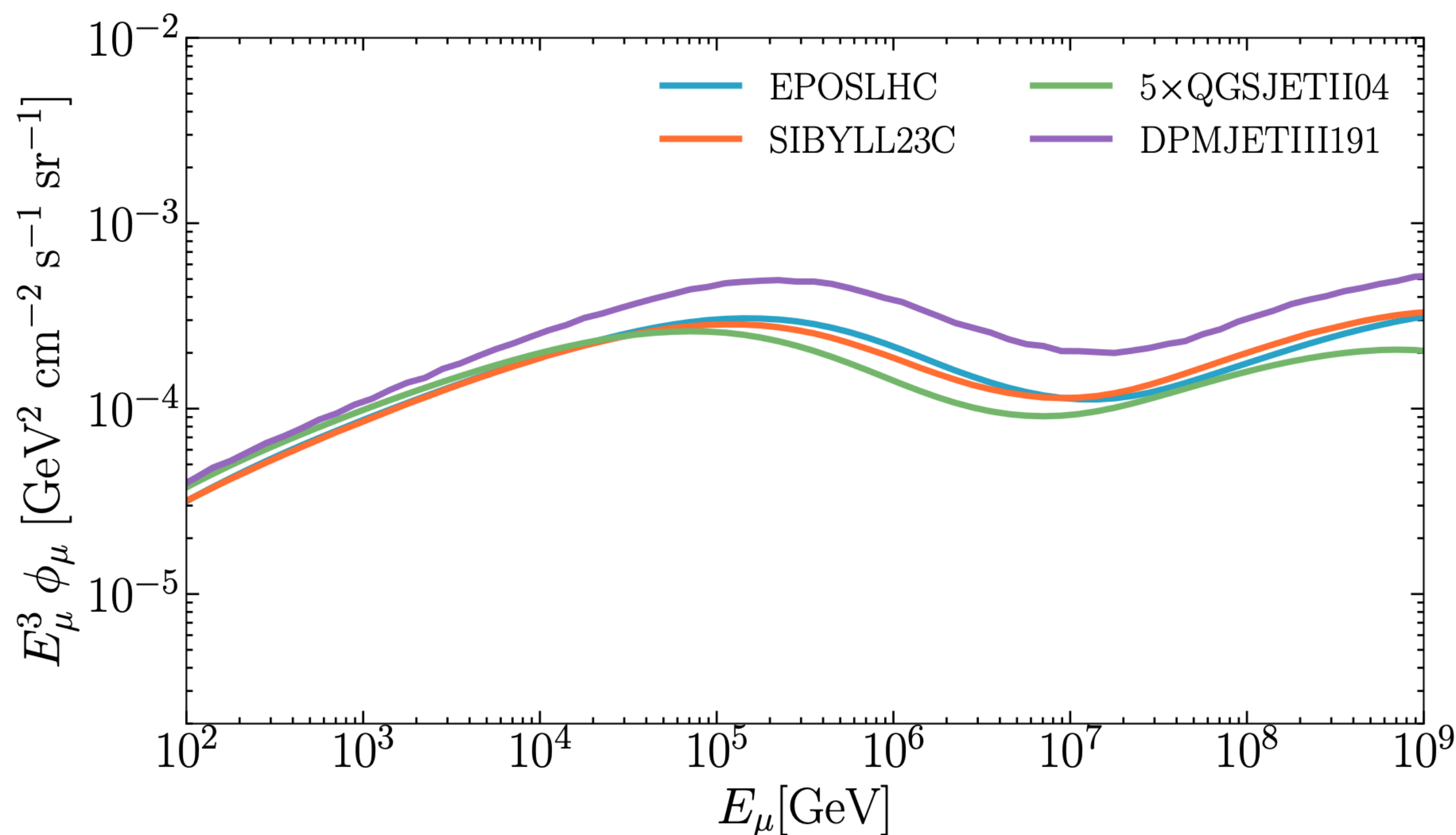
- $pA \rightarrow \bar{D}^{*0} \Lambda_c^+$ dominates.

- $\bar{D}^{*0} \rightarrow \bar{D}^0 \gamma$ (first approx)

- $x_{\Lambda_c} = 1 - x_{\bar{D}^{*0}}$

Unflavored contribution

To muon flux from different MCEq models



$$w_c^{\text{intr}} = 0 \text{ and } \alpha_{\text{unfl}} = 4.84$$

$$\begin{aligned}
\phi_{\mu,\text{prompt}} &= \phi_{\mu,\text{pQCD}} + \phi_{\mu,\text{unfl}} \\
&\sim \phi_{\mu,\text{pQCD}} + 4.8\phi_{\mu,\text{unfl}} \\
&\simeq 5.8f_{\mu,\text{prompt}} \text{ as } \phi_{\mu,\text{pQCD}} \simeq \phi_{\mu,\text{unfl}} = f_{\mu,\text{prompt}}
\end{aligned}$$

Fit values

Table 1: Best fit values of w_{intr}^c for model-dependent fit to angle averaged muon energy spectrum along with the 1σ interval.

Model	Best fit $w_{\text{intr}}^c (\times 10^{-3})$	1σ interval $(\times 10^{-3})$
Regge 1($a_\psi = -2, a_N = -0.5$)	3.91	2.93 – 4.89
Regge 2($a_\psi = -2, a_N = 0$)	3.53	2.65 – 4.42
HLM	3.02	2.26 – 3.77

Overshoots neutrino upper limit

Table 2: Best fit values for the scaling factor of the unflavored flux if we use w_c^{intr} needed to meet the neutrino upper limit, along with the 1σ interval. For no intrinsic charm, we have $\alpha_{\text{unfl}} = 4.84$ and 1σ interval is $3.85 - 5.83$

Model	$w_{\text{intr}}^c \times 10^{-4}$	Best fit α_{unfl}	1σ interval
Regge 1($a_\psi = -2, a_n = -0.5$)	4.46	4.39	3.40 - 5.38
Regge 2($a_\psi = -2, a_n = 0$)	4.15	4.38	3.39 - 5.37
HLM	3.69	4.36	3.37 - 5.35

Unflavored is increased to match with muon data and still within neutrino upper bound

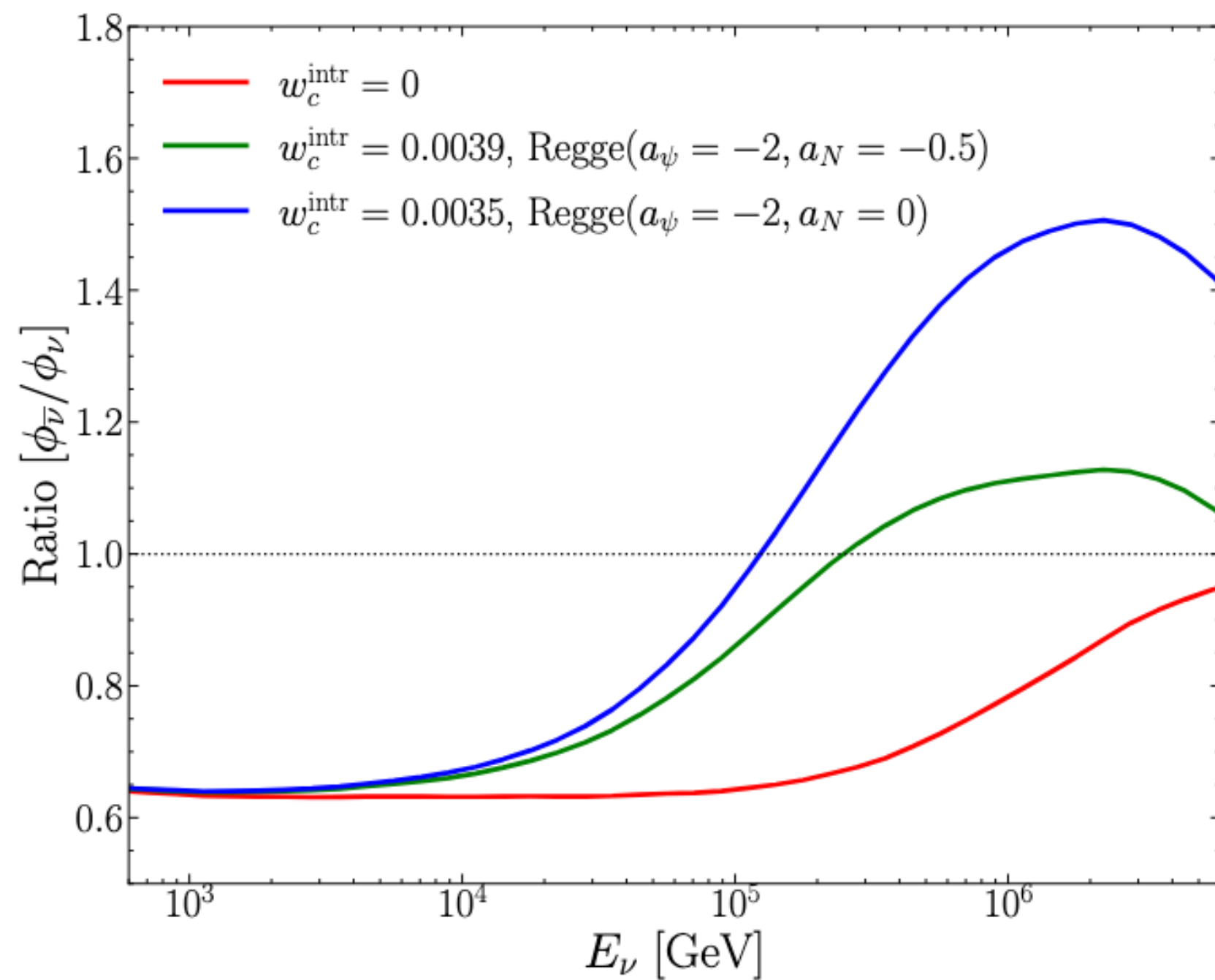
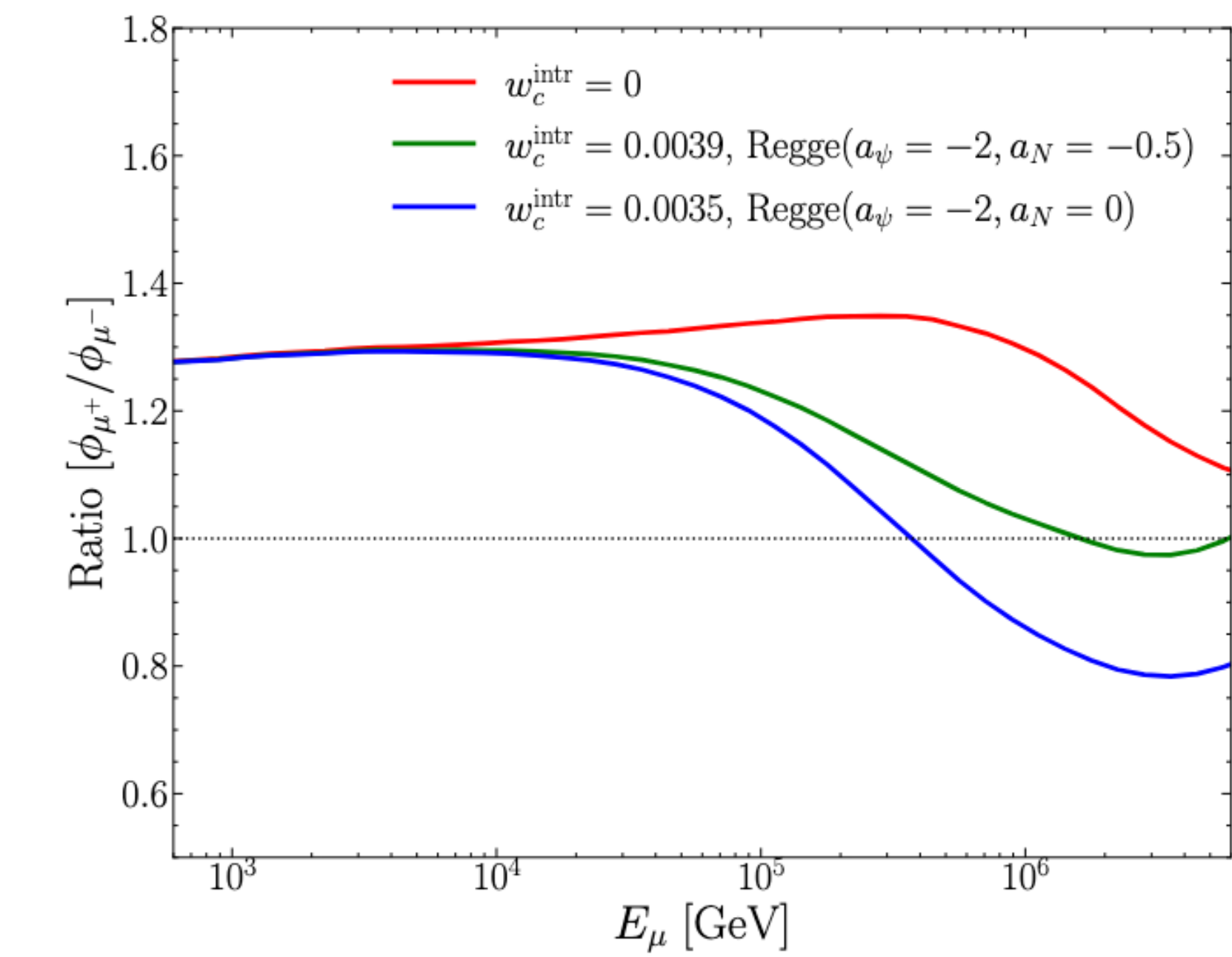


Figure 9. Left: Muon charge ratio without any intrinsic charm and with intrinsic charm. Right: Anti-neutrino to neutrino flux ratio without and with intrinsic charm. Ratios are of fluxes angle averaged for $\theta < 60^\circ$ and $\alpha_{\text{unfl}} = 1$.

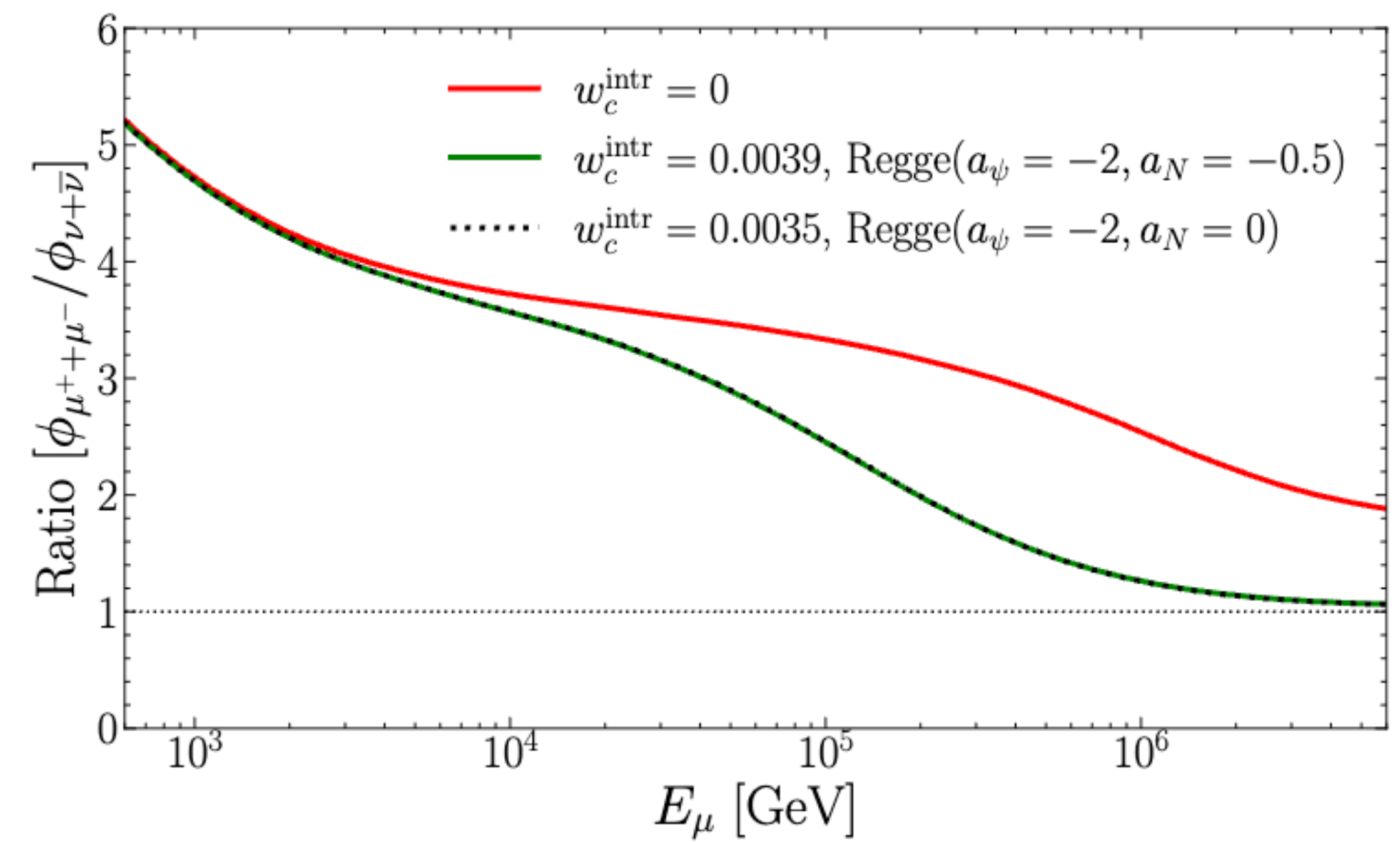


Figure 10. Ratio of muon flux to muon neutrino flux with and without intrinsic charm. For intrinsic charm, two Regge models are used. The w_c^{intr} for the two models are the best fit values we get in order to fit the model to the muon data. Here, $\alpha_{\text{unfl}} = 1$.