## Heavy Neutral Lepton on Future Muon Collider and Beamdump Experiment

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# Outline

- Neutrino Mass
- Heavy Neutral Leptons
- HNL at Muon Collider
- HNL at LSND and Future PIP2-BD
- Conclusion

# Origin of Neutrino Mass

- In SM, neutrino is massless. While the experiments have confirmed its tiny mass smaller than O(0.1) eV.
- Effective Operator: Weinberg Operator
- Seesaw mechanism
  - Simple Type I
  - Inverse seesaw model
  - Linear seesaw model
- We choose to work in a simple scenario. Suppose there is heavy neutral lepton. We can parametrize its mass  $\,m_N\,$

mixing angle with SM neutrino.  $U_l = \sin \theta_l$ 

 $\frac{LLHH}{\Lambda}$ 

$$\mathcal{L} = \mathcal{L}_W + \mathcal{L}_Z + \mathcal{L}_H$$

$$\mathcal{L}_W = \frac{gU_l}{\sqrt{2}} \left( W_\mu \bar{l}_L \gamma^\mu N + h.c. \right)$$

$$\mathcal{L}_{Z} = -\frac{gU_{l}}{2\cos\theta_{w}}Z_{\mu}\left(\bar{\nu}_{L}\gamma^{\mu}N + \bar{N}\gamma^{\mu}\bar{\nu}_{L}\right)$$
$$\mathcal{L}_{H} = -\frac{U_{l}m_{N}}{v}h\left(\bar{\nu}_{L}N + \bar{N}\nu_{L}\right)$$



# Short Review of Various Probes

- People have tried to constrain in the  $U_{\ell}^2 m_N$  plane via various channels and different machines.
- Cosmo and astrophysical probe: BBN, CMB, etc
- Indirect constraints: branching ratio of SM particles decays, etc
- Direct constraints
  - Production
    - Meson decay, heavy lepton decay
    - (On-shell/Off-shell) Gauge/higgs boson decay
  - Decay
    - Short-lived
    - Long-lived

#### HNL at Muon Collider

 $m_N > O(100) \text{GeV}$ 



 $\Gamma_N \sim G_F m_N^3 |U_\ell|^2$ 

#### Prompt decay

The muon collider can open and probe new region space in the parameter space. even compared to other future colliders!

Snowmass Energy Frontier Report: 2211.11084

# Muon Collider



**Cost** and **power** consumption drivers, limit energy reach e.g. 30 km accelerator for 10/14 TeV, 10/14 km collider ring

arxiv: 2209.01318

# Search at Muon Collider

- The future muon collider includes 3 TeV and 10 TeV scenarios.
- Clean background, fixed cms energy, excellent environment for the muon flavor HNL
- Here we show the muon-flavor Dirac HNL as benchmark.
- Tools:

Using MadGraph 3.4 to simulate and then make analysis

• Effective Vector-Boson Approximation (EVA) or gauge boson PDF has been implemented

# Muon Flavor

• Signal: Production of  $N_{\mu}$ Dominated by the t-channel

$$\mu^+ + \mu^- \to N_\mu + \bar{\nu}_\mu$$





Type	Signal process	$\sigma/ U_{\mu} ^2$ (w. conj. channel) $m_N = 1$ TeV
<i>t</i> -channel	$\mu^+\mu^- \longrightarrow N_\mu \bar{\nu}_\mu$	20.28 pb
VBF	$\mid \mu^+\mu^- \longrightarrow \mu^+\mu^- N_\mu ar{ u}_\mu \mid$	$\sim 1~{ m pb}$
VBF	$\mu^+\mu^- \longrightarrow ar{ u}_\mu  u_\mu N_\mu ar{ u}_\mu$	$\sim 0.1~{ m pb}$

# Decay of $N_{\mu}$

HNL can promptly decay via neutral current or charged current or to the higgs. Here we select its decay channel to W boson.

Goldstone-Boson Equivalence Theorem



We assume the W boson can be well reconstructed from the two jets.

We focus on the final states  $W^+$  and  $\mu^-$  and reconstruct its invariant mass distribution.

# 10TeV Background

Dijets can be from either W or Z boson.

Type	Background process	$\sigma$ (w. conj. channel)	Pre-selection cut (PSC)	Included
<i>t</i> -channel	$\mu^+\mu^- \longrightarrow W^+\mu^-\bar{\nu}_\mu$	0.214 pb	PSC	Yes
<i>t</i> -channel	$\mu^+\mu^- \longrightarrow Z\mu^+\mu^-$	0.464 pb	PSC & missing $\mu^+$	Yes
VBF	$\mu^+\mu^- \longrightarrow \mu^+\mu^- W^+\mu^- \bar{\nu}_\mu$	0.401 pb	PSC & missing $\mu^+\mu^-$	Yes
VBF	$\mu^+\mu^- \longrightarrow \bar{\nu}_\mu \nu_\mu W^+\mu^- \bar{\nu}_\mu$	0.0686 pb	PSC	No

Table 4.  $N_{\mu}$  background at 10 TeV. The cross section includes the charge conjugate process.

Using EVA in MadGraph, especially photon PDF VBF processes dominates at 10 TeV

Default cut: For muon: PT > 20GeV, Eta < 2.5

Using EVA will lead to t-channel singularity. So we just generate 2 -> 5 processes directly in MadGraph.

# Cutflow Analysis

- Pre-selection: require single visible charged lepton
  - $|\eta(\mu)| < 2.5$  and  $p_T(\mu) > 20 \text{ GeV}$
- Central hadronic W selection: require visible on-shell W boson
  - $|\eta(W)| < 2.5$  and  $p_T(W) > 20 \text{ GeV}$
- Mass window: reconstructed mass  $m_{W\mu}$  within  $m_N \pm 5\% m_N$
- Optimization cuts:
  - Customized cut on missing  $p_T$ , E(W),  $p_T(W)$  for each  $m_N$  benchmark



Process	Central $W$	Mass window 150/1000/5000/9000 GeV	Optimization
Background	34.19%	1.2/0.63/0.023/0.134%	0.16/0.22/0.011/0.0032%
$m_N = 150 \text{ GeV}$	83.84%	83.84%	66.63%
$m_N = 1000 \text{ GeV}$	93.67%	93.67%	80.55%
$m_N = 5000 { m ~GeV}$	99.01%	99.01%	89.69%
$m_N=9000~{\rm GeV}$	99.48%	99.48%	87.53%

# Projected sensitivity



Sensitivity to e and  $\tau$  flavor is moderate

Muon Collider features the strong direct probe of the  $\mu$  flavored HNL

10 TeV muon collider can probe the  $|U_{\mu}|^2$  to a few  $10^{-7}$  for TeV scale HNLs.

The VBF background increases for high energy muon colliders and renders the 3 TeV muon collider competitive in sub TeV scale.

The 95% projected sensitivity of  $|U_e|^2$ ,  $|U_\mu|^2$  and  $|U_\tau|^2$  as a function of HNL mass mN at 3 and 10 TeV muon collider.



K. Mekała, J. Reuter and A.F. Zarnecki, arXiv:2301.02602

### HNL at LSND and Future PIP2-BD

# Various Bounds

Some future proposed beam-dump experiments or far detector to probe the long-lived HNL

Low mass region, three body decay

$$\Gamma_N \sim G_F^2 m_N^5 |U_\ell|^2$$
$$c\tau_N \sim 10^8 \,\mathrm{m} \times \left(\frac{m_\mu}{m_N}\right)^5 \left(\frac{10^-}{|U_{lN}|^2}\right)^{1/2}$$



# Fixed-Target: LSND

- Fixed-target experiment provides a good platform to search for feebly interacting GeV-scale particles.
- Light HNL with tiny mixing angle can be long-lived.
- It can travel for long distance before decaying. Thus it can leave imprints at the far detector.
- We are interested in the case  $m_N < m_{\pi}$  and recast on the old LSND as well as future PIP2-BD experiment.
- First let me review the HNL search at DUNE.

#### Probing HNL at Dune

Production modes for the e flavor traveling toward the DUNE MPD



1912.07622 Berryman etc

Decay Mode

#### e flavor

#### mu flavor



Irrel. Decays: background dominated

1912.07622 Berryman etc

## Projected Sensitivity at DUNE



#### Liquid Scintillator Neutrino Detector (LSND) Experiment



Leave imprints at detector

# Production: Muon and Pion Decay at Rest

• At LSND, the neutrino arise from the decay at rest (DAR) of stopped  $\pi^+$  and  $\mu^+.$ 



Decay of  $N_{\mu}$ 



Three body decay

 $\Gamma_N \sim G_F^2 m_N^5 |U_\ell|^2$ 

$$c\tau_N \sim 10^8 \,\mathrm{m} \times \left(\frac{m_\mu}{m_N}\right)^5 \left(\frac{10^{-6}}{|U_{lN}|^2}\right)$$

Signal at the detector: 
$$e^+ e^-$$
 pair  $\exp\left(-\frac{D}{\gamma c \tau}\right) \left[1 - \exp\left(-\frac{L_{det}}{\gamma c \tau}\right)\right]$   
 $N_{ee}^{(i)} = N_i \times \epsilon_{det} \times \frac{1}{\Gamma_i} \int dE_N \frac{d\Gamma(i \to fN)}{dE_N} \times \frac{L_{det}}{\gamma \beta c \tau_{N \to ee\nu}}$ 



.

cut 1:  $18 \text{ MeV} < E_{\pm} < 50 \text{ MeV}, \ E_{\mp} < E_{\text{th}}, \ \cos \theta_{\pm} > 0.9, \ \cos \theta_{\mp} < 0.9,$ cut 2:  $18 \text{ MeV} < E_{+} + E_{-} < 50 \text{ MeV}, \ \cos \theta_{\pm} > 0.9.$ 

# The LSND experiment observed in total 242 single e events (including all the $\nu_e \nu_\mu$ and $\bar{\nu}_\mu$ initiated signals) while 229 events are expected within the SM.

With the systematic error included, we impose at 90% C.L.  $N = N(\mu) \times \epsilon(\mu) + N(\pi) \times \epsilon(\pi) < 55$ .

### PIP2-BD

- Proton Improvement Project II (PIP-II) is a major upgrade of the accelerator complex at Fermilab to meet the requirement of hosting the Deep Underground Neutrino Experiment (DUNE).
- We may assume five years of physics run with the baseline PAR option, which results in an 800 MeV proton beam with  $1.2 \times 10^{23}$  POT. Considering the formation rate

$$N_{\pi} = N_{\mu} = 1.2 \times 10^{22}$$

• Detector is in cylindrical in shape with 4.5m in height and 4.5m in diameter, located 18m away from the HNL production point.

#### e flavor mu flavor $|U_{eN}| = |U_{\tau N}| = 0$ $|U_{\mu N}| = |U_{\tau N}| = 0$ $10^{-3}$ $10^{-4}$ $10^{-5}$ HBOONE $10^{-4}$ PS] $10^{-6}$ LSND (this work T2K PIENU $\frac{1}{N} \frac{1}{M^{N-2}}$ $|U_{eN}|^2$ $10^{-7}$ PIENU LSND (this work) TRIUMF PIENU $10^{-8}$ DUNE $10^{-6}$ PIP2-BD (this work) PIONEER $10^{-9}$ PIONEER PIP2-BD (this work) $10^{-7}$ DUNE $10^{-10}$ 10 10 30 50 70 90 1130 507090 110 130 $m_N \, [{ m MeV}]$ $m_N \, [{ m MeV}]$

## Conclusion

- We focus on two mass range for the HNL.
- Muon Collider is a good platform to probe the TeV scale HNL. We can open a new region in the parameter space.

For the muon flavor case, we can probe the  $|U_{\mu}|^2$  down to  $10^{-7}$ .

- For the lighter HNL, we revisit LSND and make projections on future PIP2-BD. The sensitivity can be improved a lot.
- There are more interesting phenomena in the HNL sector.

# Existing Bounds

#### Snowmass Energy Frontier Report: 2211.11084

From Past Experiments



## Upgraded Bounds



Future Upgraded Projection on LHC, NA62 and DUNE

## Various Bounds



Bounds from the proposed future collider: FCC, CEPC, ILC, LHeC