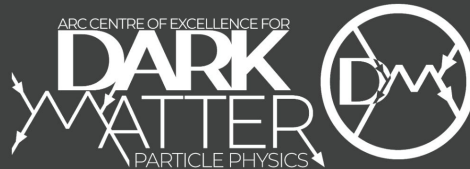


Updates on the Migdal effect and hydrogen doping for dark matter detection

CETUP* Workshop

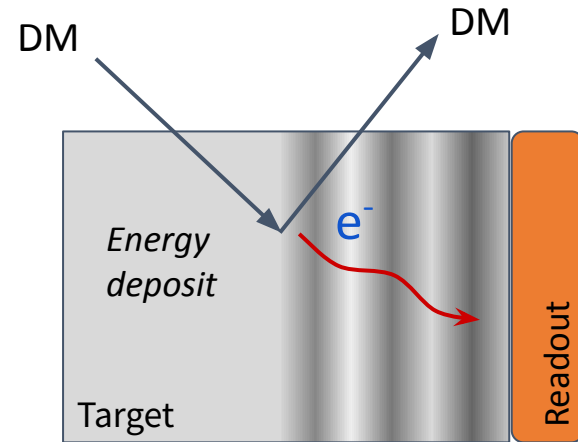
Institute for Underground Science
at SURF, South Dakota
June-July 2024

Jayden Newstead



Direct detection fundamentals

- Look for signals of dark matter from the galactic halo scattering off nuclei or electrons in a detector
- Kinetic energy of recoil deposited as:
 - Scintillation
 - Ionization
 - Phonons
- This is read out via PMT's, current, TES, imaging...

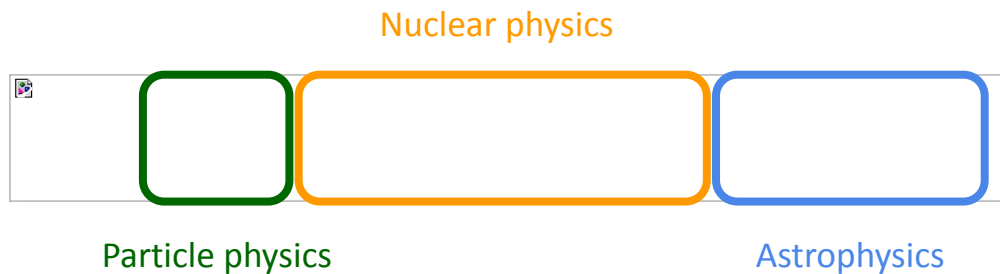


The Migdal effect allows us to probe lighter dark matter, which would otherwise fall below threshold



Elastic dark matter-nucleus scattering

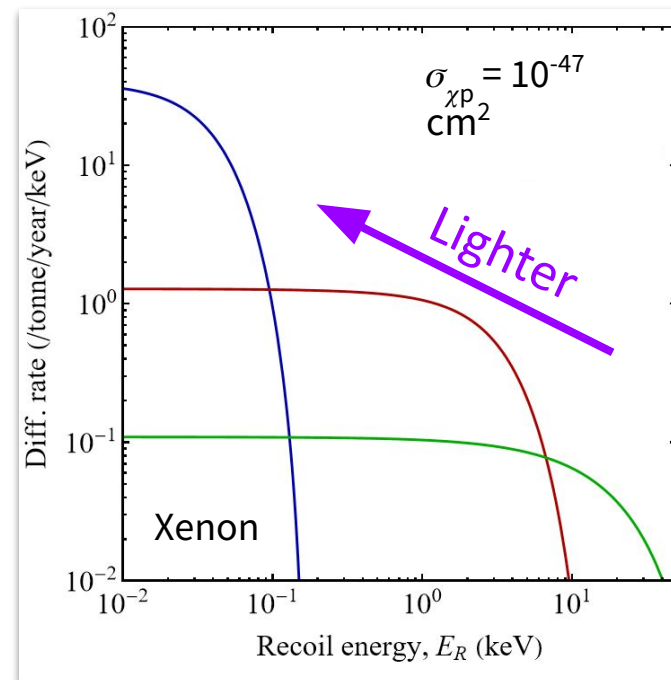
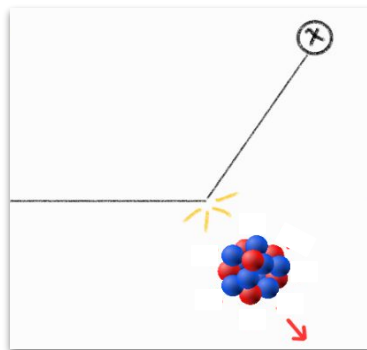
Differential rate:



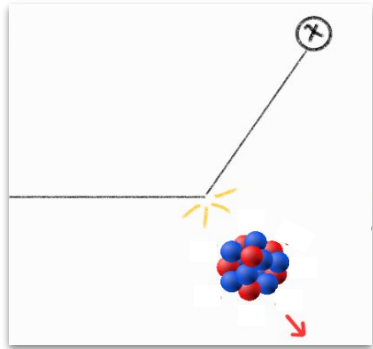
Where:

$$v_{\min} = \sqrt{\frac{E_R m_T}{2\mu_{\chi T}^2}}$$

$$E_{R_{\max}} = \frac{2\mu_T^2}{m_T} v_{\max}^2$$



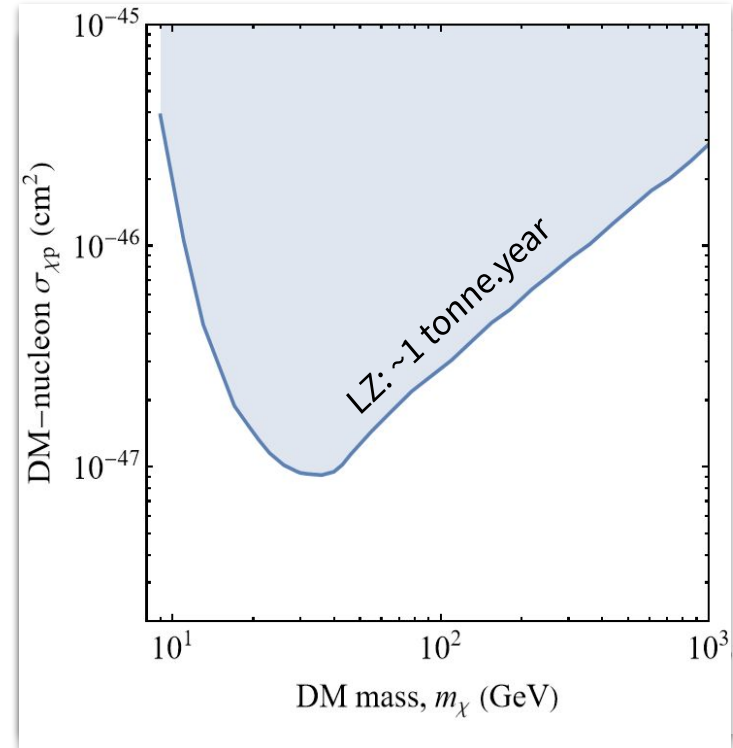
Direct detection's kinematic problem



$$E_{R_{\max}} \approx \frac{m_{\chi}^2}{m_T} \times 10^{-5}$$

$$E_{EM_{\max}} \approx m_{\chi} \times 10^{-5}$$

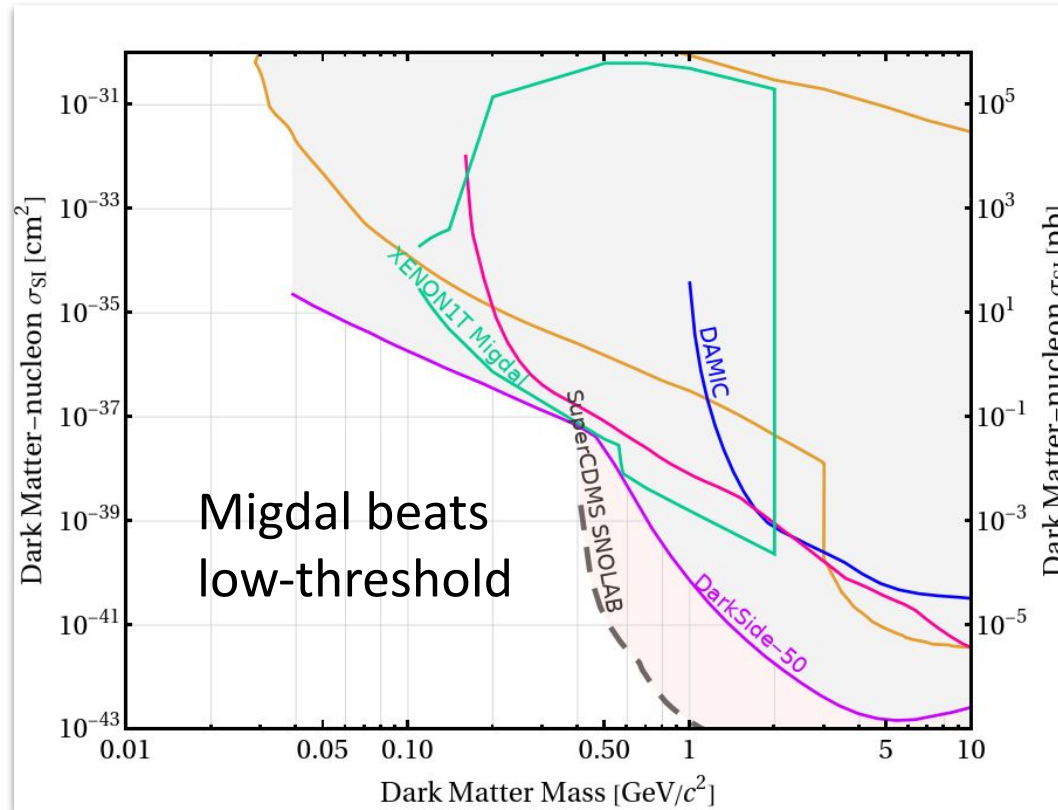
→ Light dark matter does not pack much of a punch



*assuming $v_{\max} = 800 \text{ km/s}$

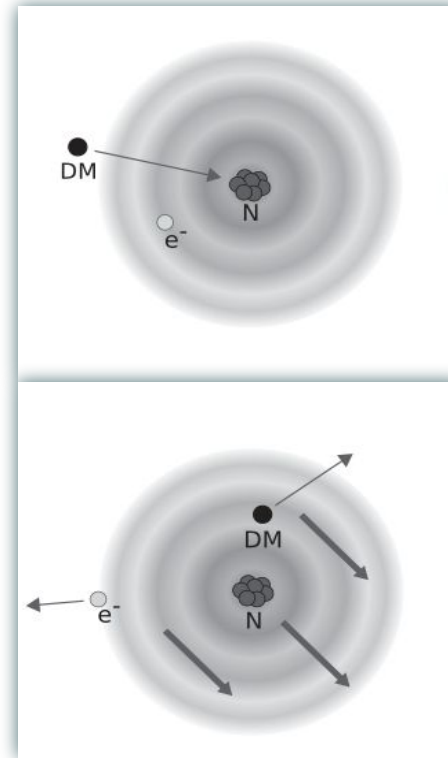


The future of direct detection



The Migdal Effect

- The Migdal effect is atomic ionization or excitation due to a nuclear recoil
- ‘Electron shakeoff’ has been observed during nuclear decay, but not due to scattering (see for example: *Couratin et al. Phys. Rev. Lett. 108 (2012)*)
→ **Agreement with theory is mixed**



Credit: Dolan et al. PRL 2017



A brief history of the Migdal effect

1939: A.B. Migdal, J. Phys. USSR 4 449

1958: Landau and Lifshitz Vol. 3: Quantum Mechanics, sec. 41:

PROBLEM 2. The nucleus of an atom in the normal state receives an impulse which gives it a velocity v ; the duration τ of the impulse is assumed short in comparison both with the electron periods and with a/v , where a is the dimension of the atom. Determine the probability of excitation of the atom under the influence of such a “jolt” (A. B. MIGDAL 1939).

(A. B. *Мигдал*, 1939).

2005: First application to DM detection:

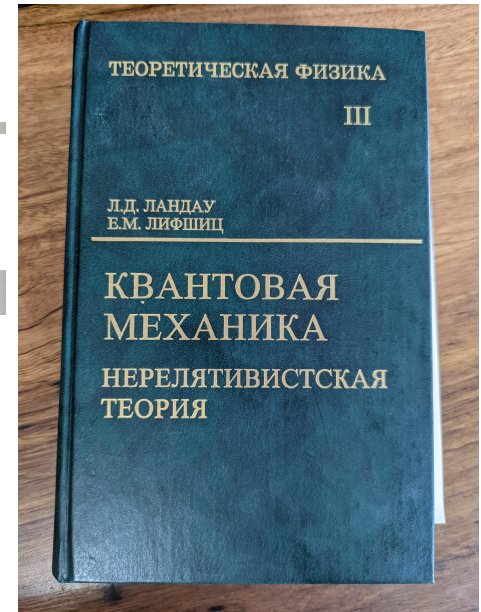
J.D. Vergados and H. Ejiri, Phys. Lett. B 606, 313, arXiv:[hep-ph/0401151](https://arxiv.org/abs/hep-ph/0401151)

2018: First detailed atomic calculations for DM:

M. Ibe, W. Nakano, Y. Shoji and K. Suzuki, JHEP 1803 (2018) 194 [arXiv:1707.07258](https://arxiv.org/abs/1707.07258)

2018: First experimental constraints:

M. Dolan, F. Kahlhoefer and C. McCabe Phys. Rev. Lett. 121 (2018) [arXiv:1711.09906](https://arxiv.org/abs/1711.09906)



Ionization probabilities

What goes into the rate calculation?

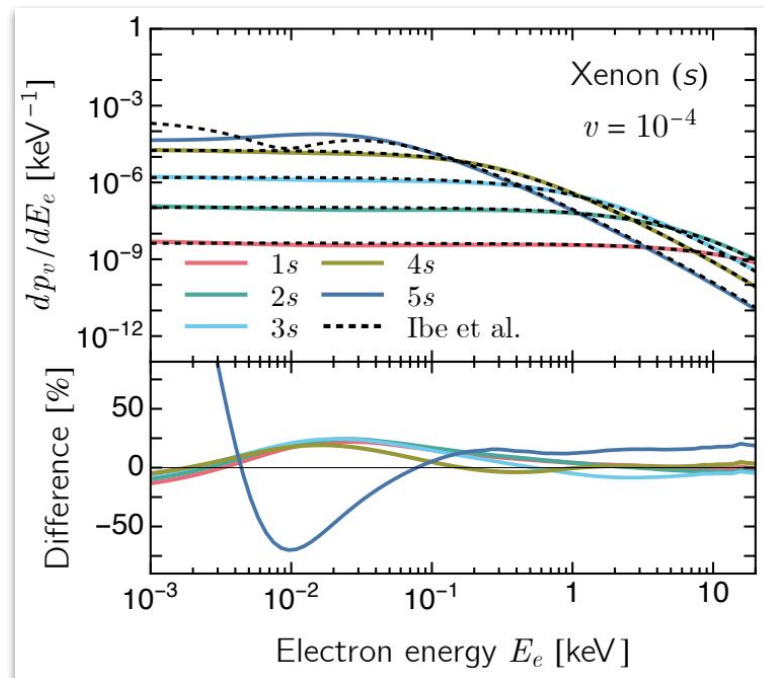
$$\frac{d^2 R}{dE_{\text{NR}} dE_i} = \frac{d^2 R_{iT}}{dE_{\text{NR}} dE_i} \times |Z_{\text{ion}}|^2$$

$$|Z_{\text{ion}}|^2 = \frac{1}{2\pi} \sum_{n,\ell} \int dE_e \frac{d}{dE_e} p_{q_e}^c(n\ell \rightarrow (E_e))$$

Ionization prob.

Relevant matrix elements obtained by boosting the electronic wavefunction:

$$\left\langle \Psi_f \left| \exp \left(i m_e \mathbf{v} \cdot \sum_{k=1}^N \mathbf{r}_k \right) \right| \Psi_i \right\rangle$$

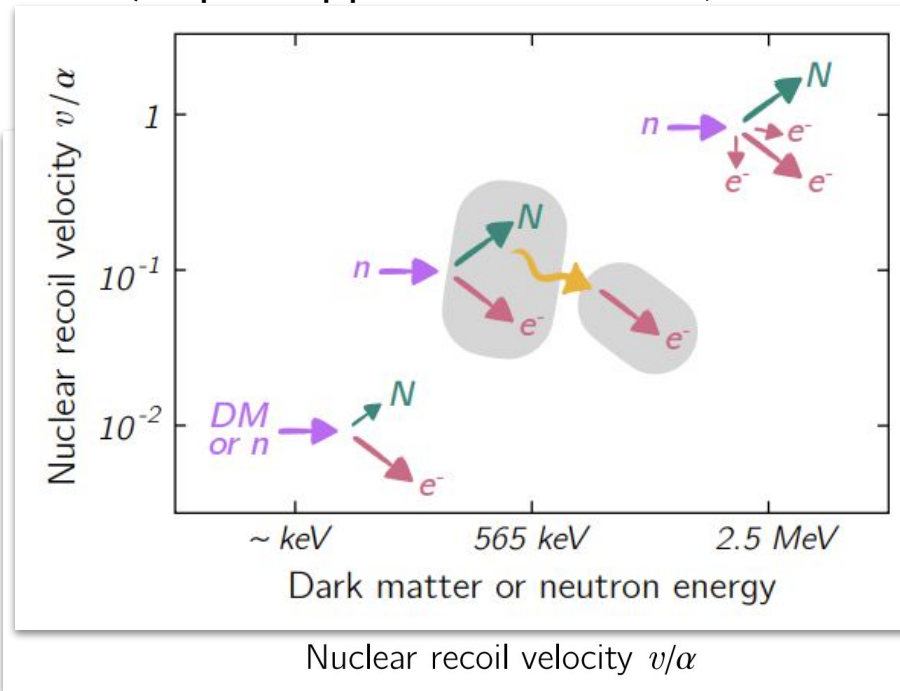


Cox et al. Phys.Rev.D 107 (2023)

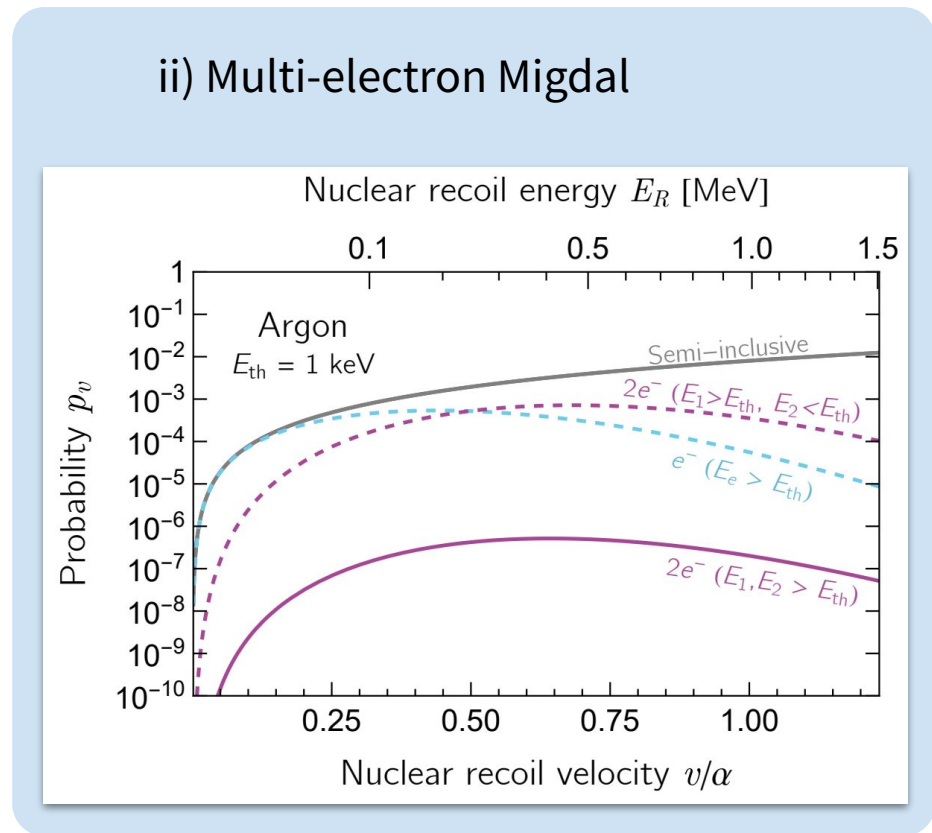
[arXiv:2208.12222](https://arxiv.org/abs/2208.12222)

Ionization probabilities cont.

i) Dipole approx is fine for DM, but

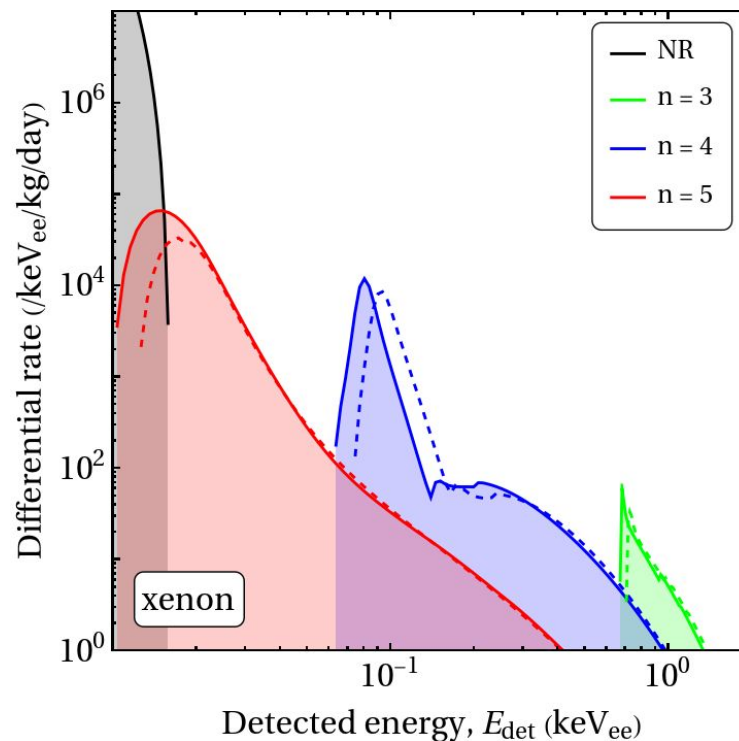
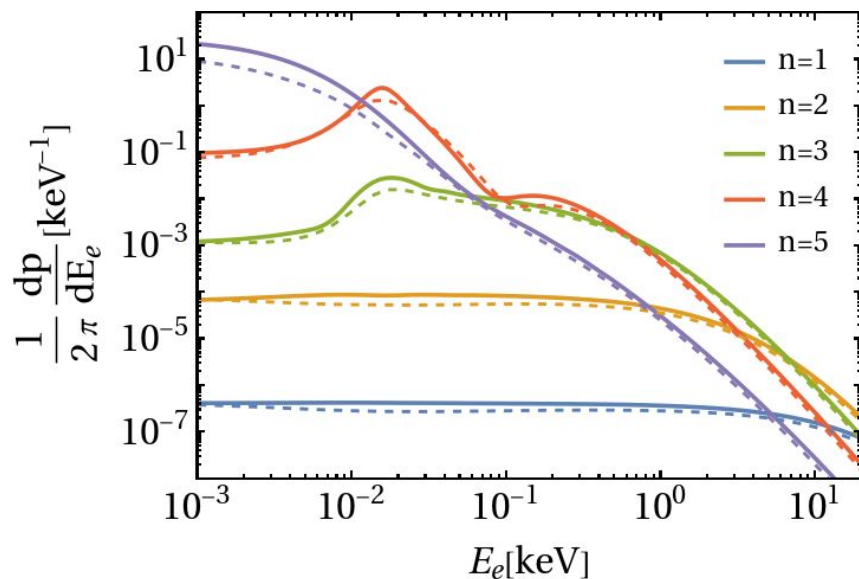


ii) Multi-electron Migdal



Ionization probabilities: Cox (dashed) vs. Ibe/dipole (solid)

Difference mostly from shifted ionization energies

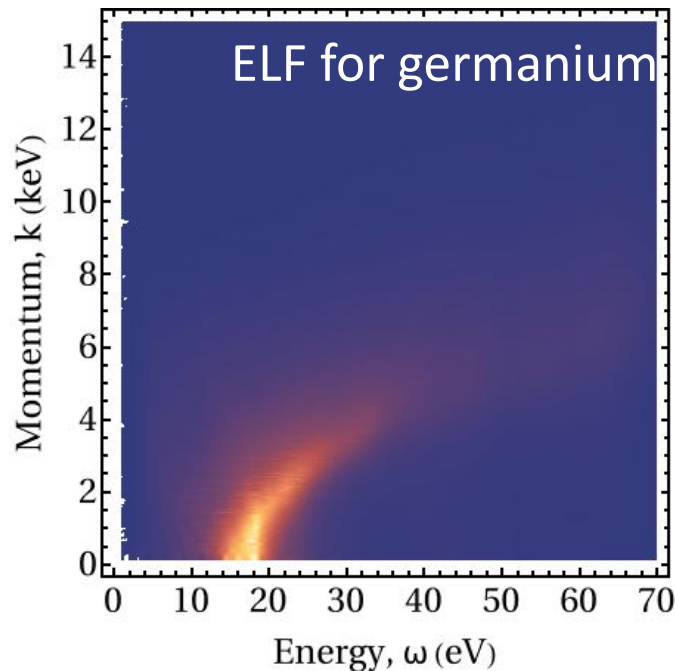
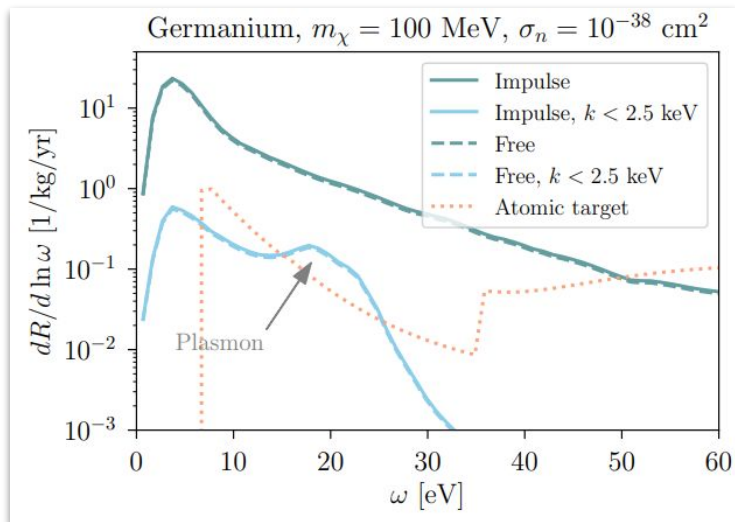


Ionization probabilities in semiconductors

When the atom is not isolated things are more complicated:

Energy loss function

$$\frac{dP}{d\omega} = 4\alpha \int \frac{d^3\mathbf{k}}{(2\pi)^3} \frac{Z_{\text{ion}}^2(k)}{k^2} \text{Im} [-\epsilon_{00}^{-1}(\mathbf{k}, \omega)] \frac{|\mathbf{v}_N \cdot \mathbf{k}|^2}{\omega^4}.$$

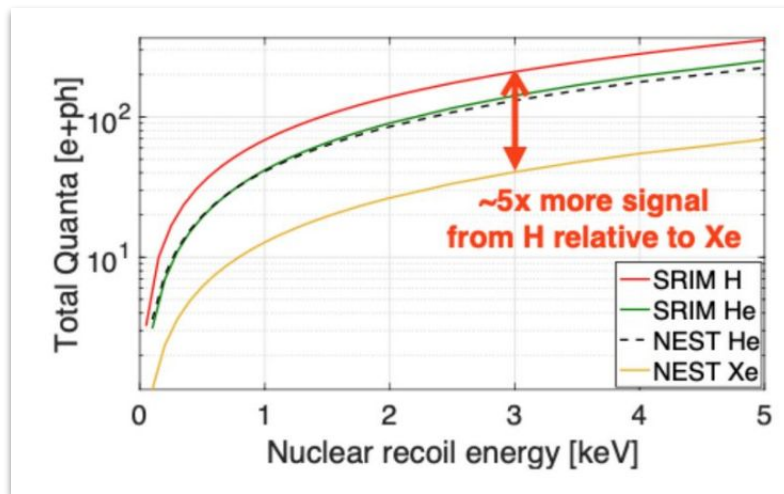
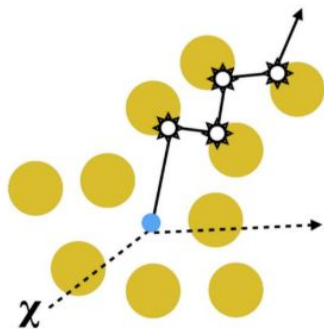


From the [DarkELF package](#), calculated with DFT (GPAW)

Hydrogen doping LXe TPCs

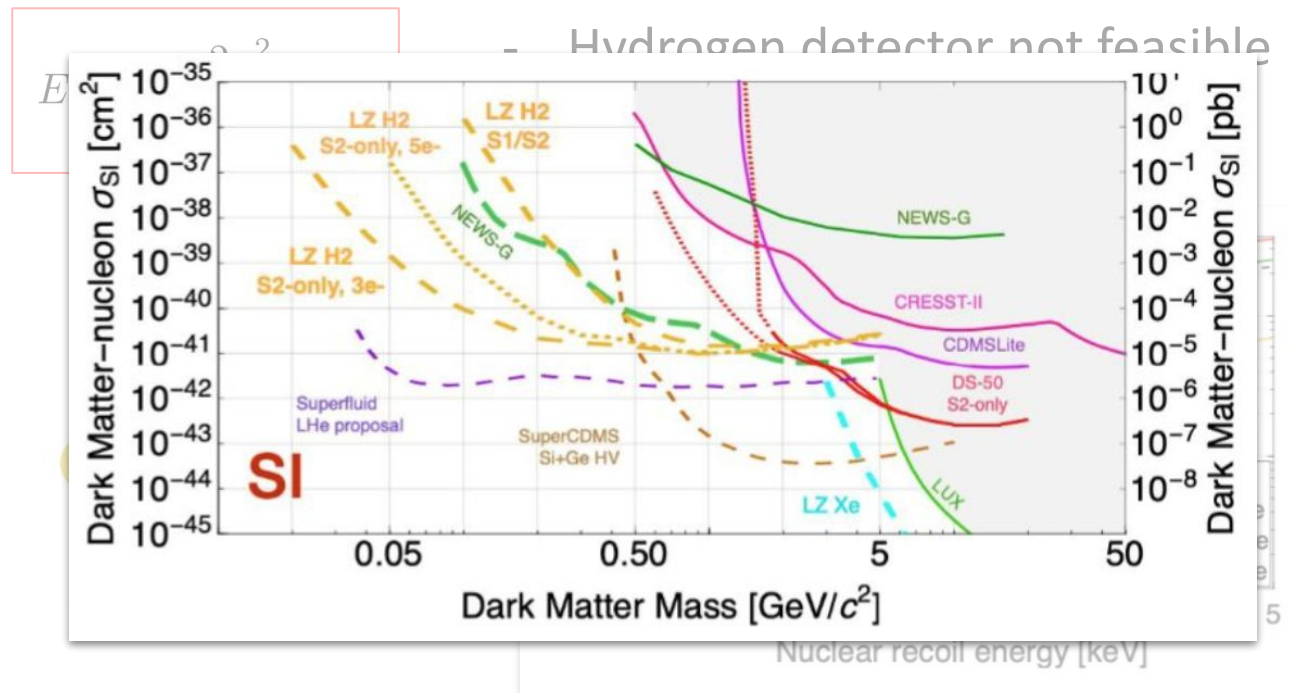
$$E_{R_{\max}} = \frac{2\mu_T^2}{m_T} v_{\max}^2$$

- Hydrogen detector not feasible
- Can we add H₂ to LXe?



From [talk by Drew Ames, SLAC, CPAD workshop 2023](#)

Hydrogen doping LXe TPCs



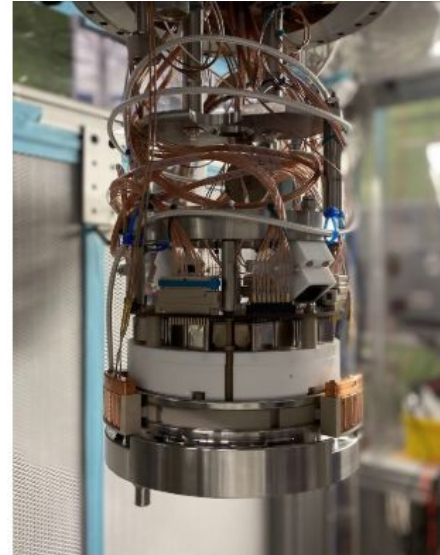
From [talk by Drew Ames, SLAC, CPAD workshop 2023](#)



Hydrogen doping LXe TPCs

Hydro-X platform at SLAC will:

- Investigate effect on S2
- Develop gas-handling system
- Test effects of H on PMTs



From [talk by Drew Ames, SLAC, CPAD workshop 2023](#)



Combining hydrogen doping with Migdal

- Projections for adding 2.5 kg of H_2 to LZ and doing S2-only search

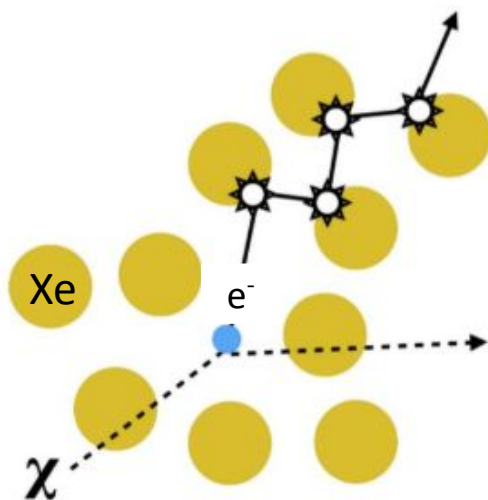
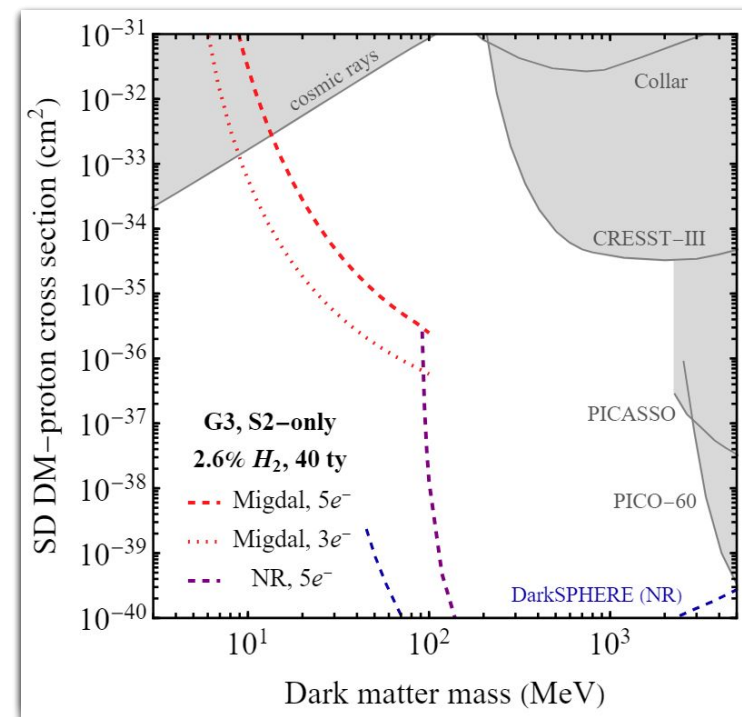
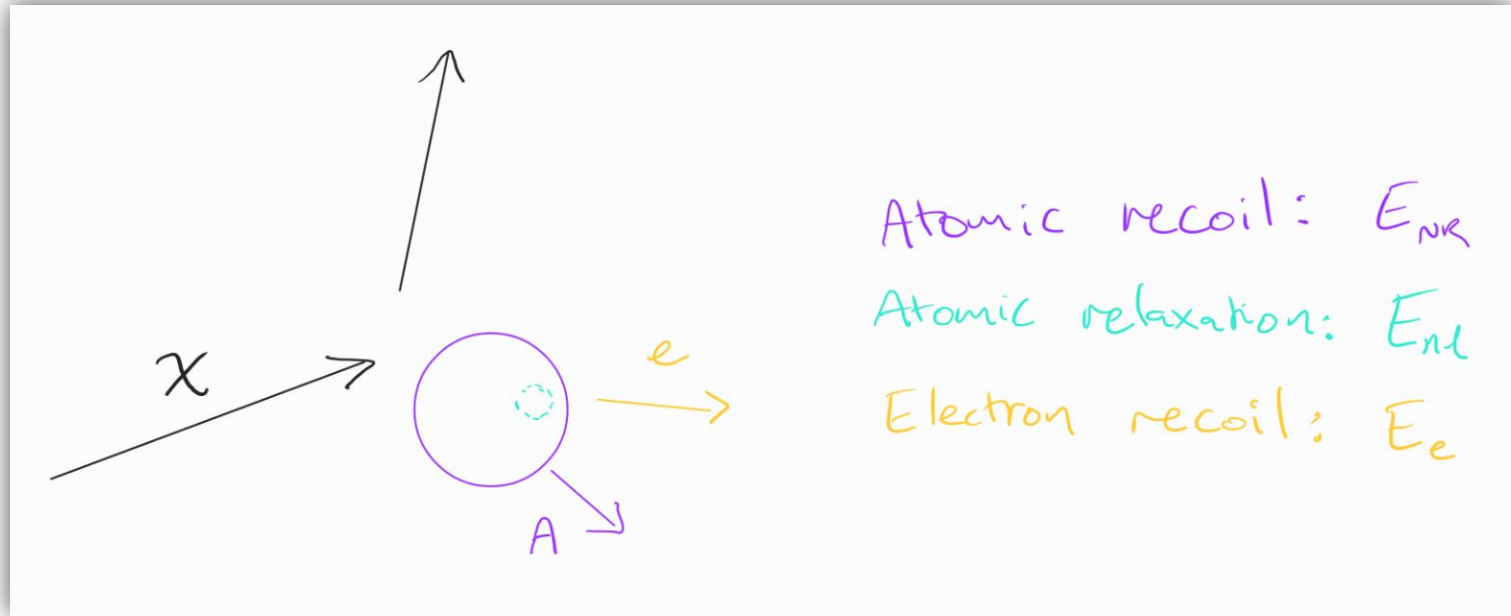


Image credit [Drew Ames, SLAC](#)



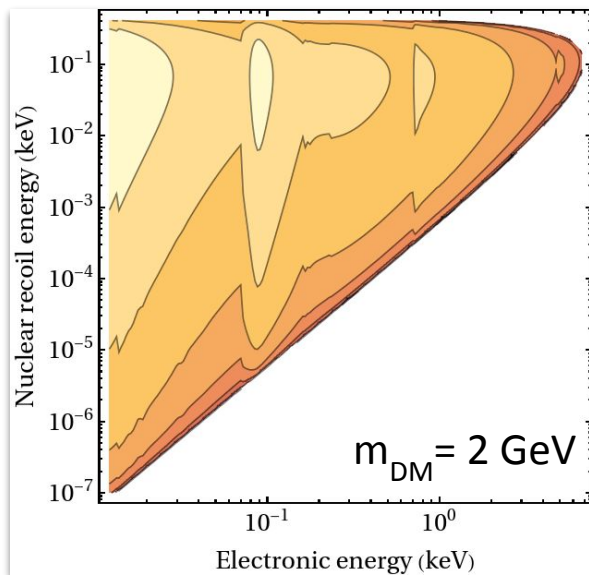
N. Bell, P.Cox, M.Dolan, **JLN**, A.Ritter
[arXiv:2305.04690](https://arxiv.org/abs/2305.04690)

Let's rewind: What does a Migdal event look like?



What does a Migdal event look like?

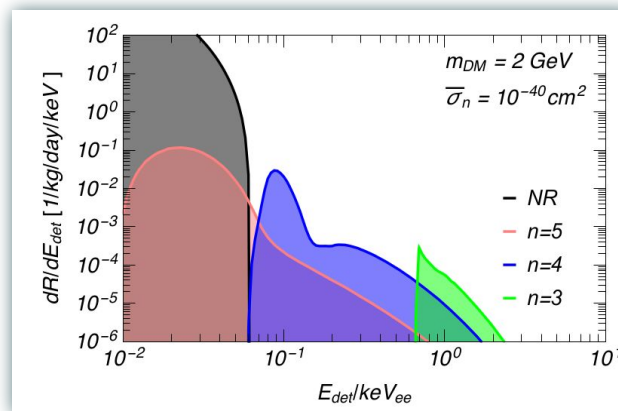
Double differential rate:



Simple:

Energy deposited w quenching:

$$E_{\text{det}} = \mathcal{L}E_R + E_e + E_{nl}$$



Hard:

Detector modelling/calibration:

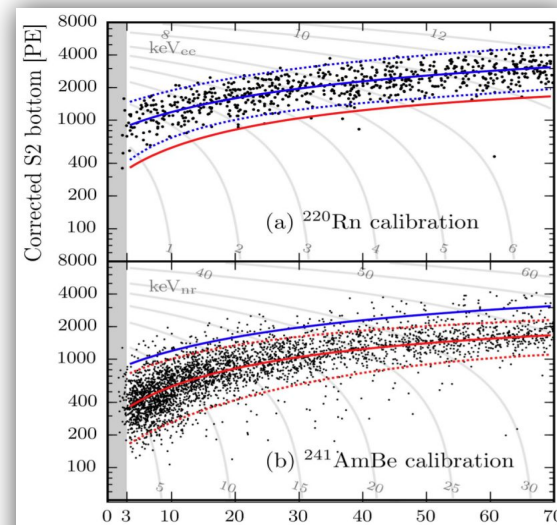
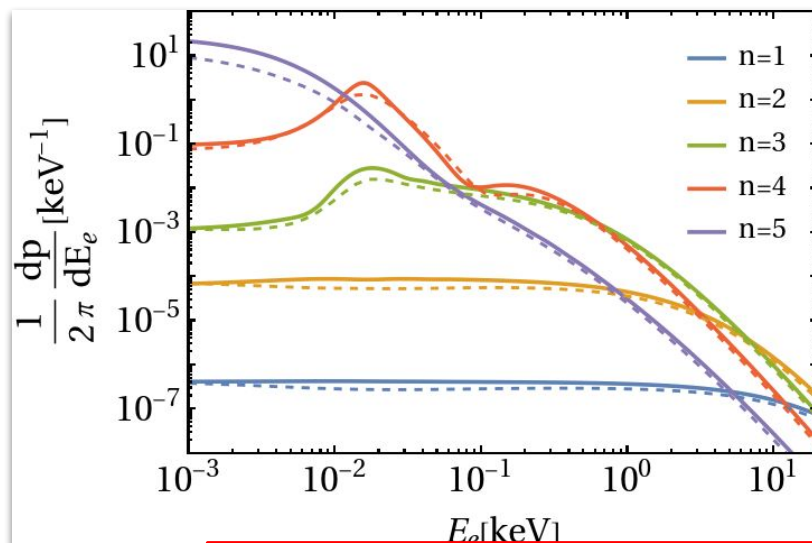
?



Calibrating the Migdal effect

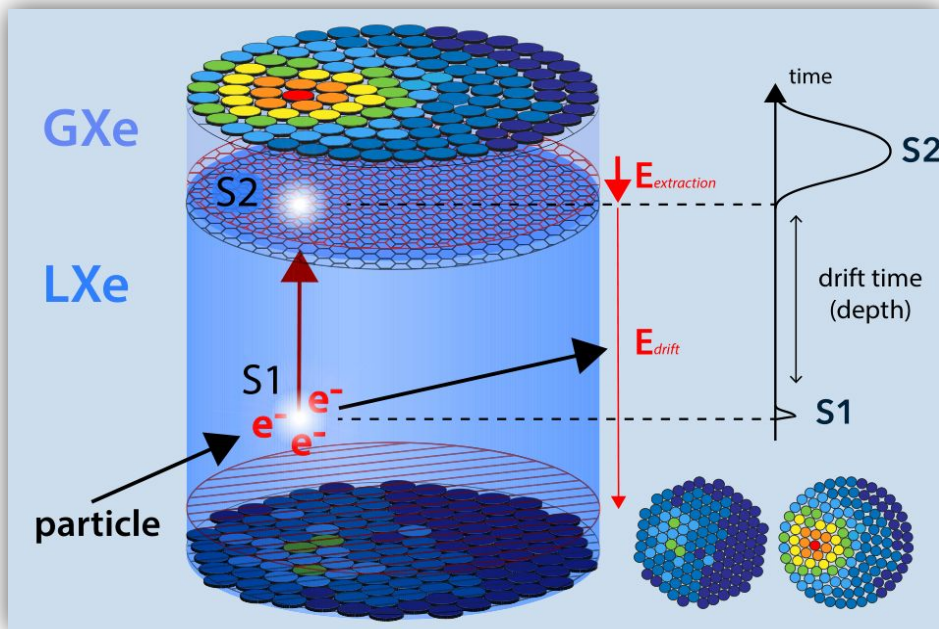
Two distinct tasks:

1. Verify theoretical predictions of the ionization probabilities
2. Calibrate the detector response to the energy depositions

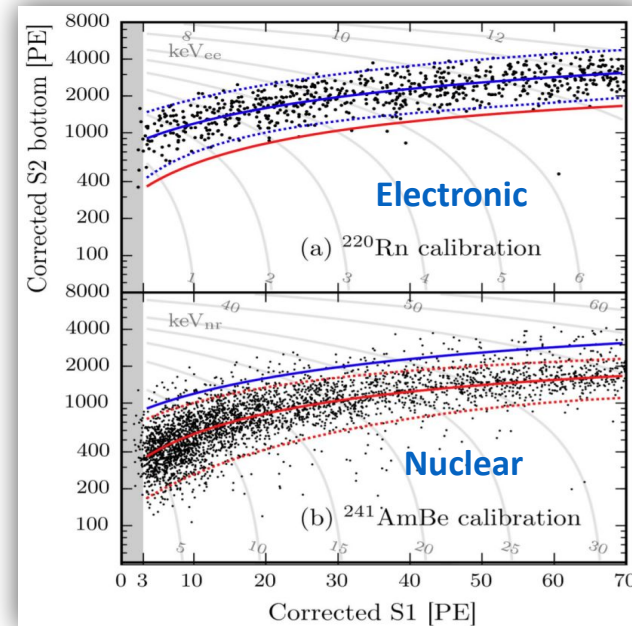


Both tasks most easily performed with neutron scattering

Experiment: Anatomy of a liquid xenon detector



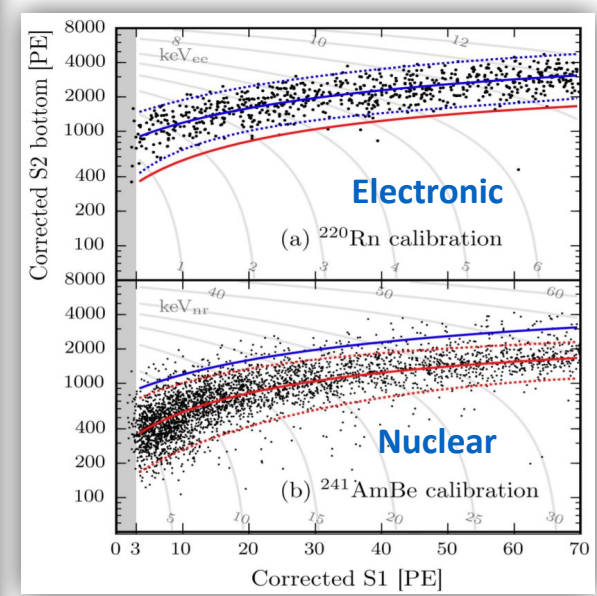
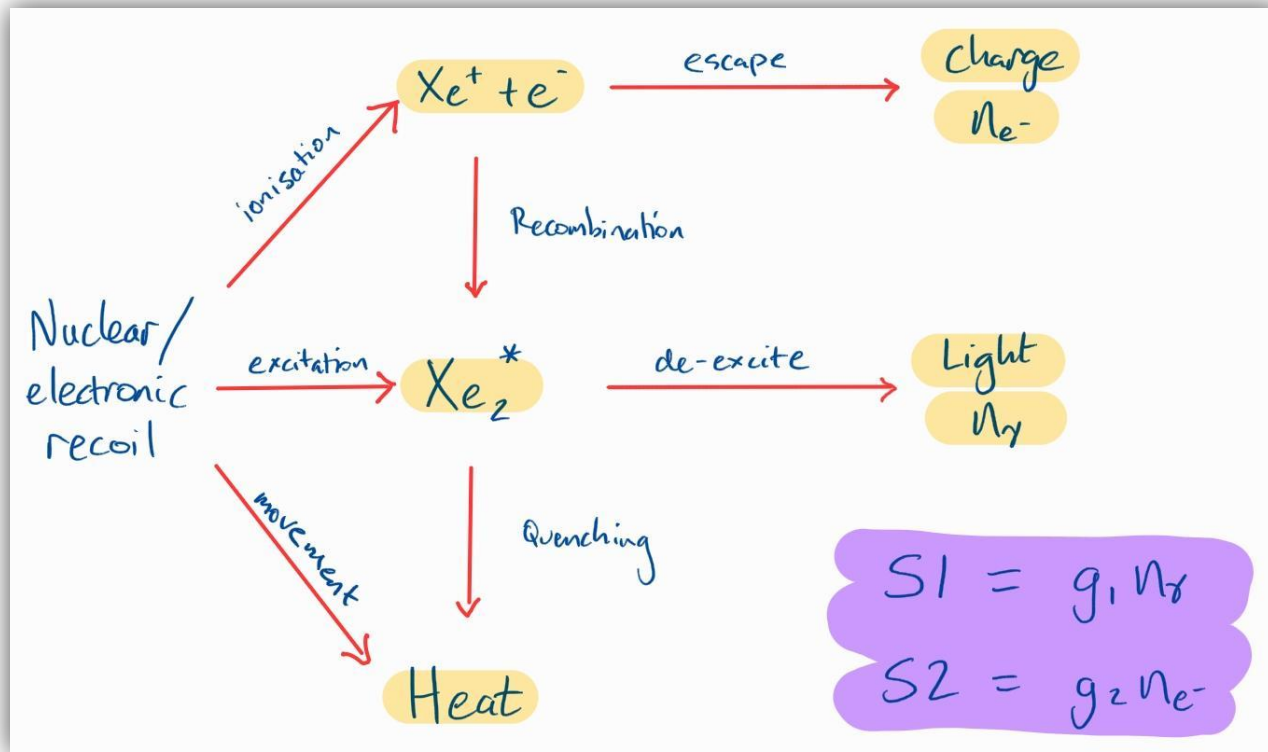
Credit: XENON1T collaboration



XENON1T [Phys.Rev.Lett. 119 \(2017\)](https://arxiv.org/abs/1708.07449)



Experiment: signal production

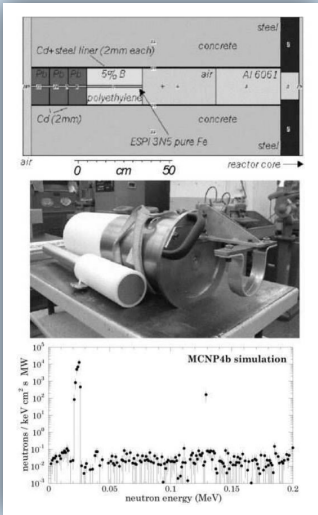


XENON1T [Phys.Rev.Lett. 119 \(2017\)](https://arxiv.org/abs/1708.07401)



Potential low-energy neutron sources

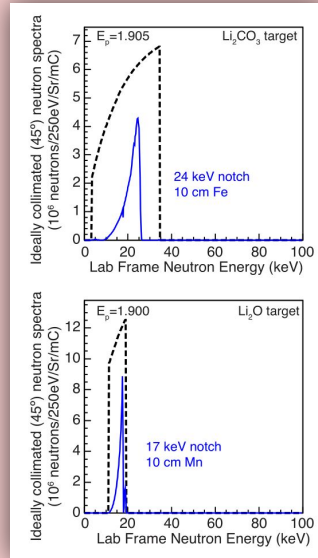
Nuclear reactor + filter



- Pros:**
- Large flux
 - Continuous operation
- Cons:**
- Gamma backgrounds
 - Location

Barbeau et al. [arXiv:nucl-ex/0701011](https://arxiv.org/abs/0701011)

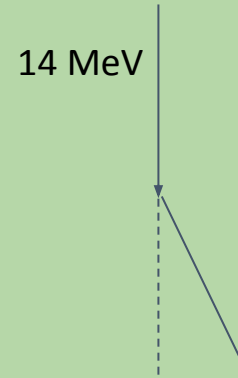
Li + p near threshold + filter



- Pros:**
- Pulsed beam
- Cons:**
- May require large/cooled targets
 - Location

Joshi et al. [arXiv:1403.1285](https://arxiv.org/abs/1403.1285)

DT/DD-generator + measure recoil angle

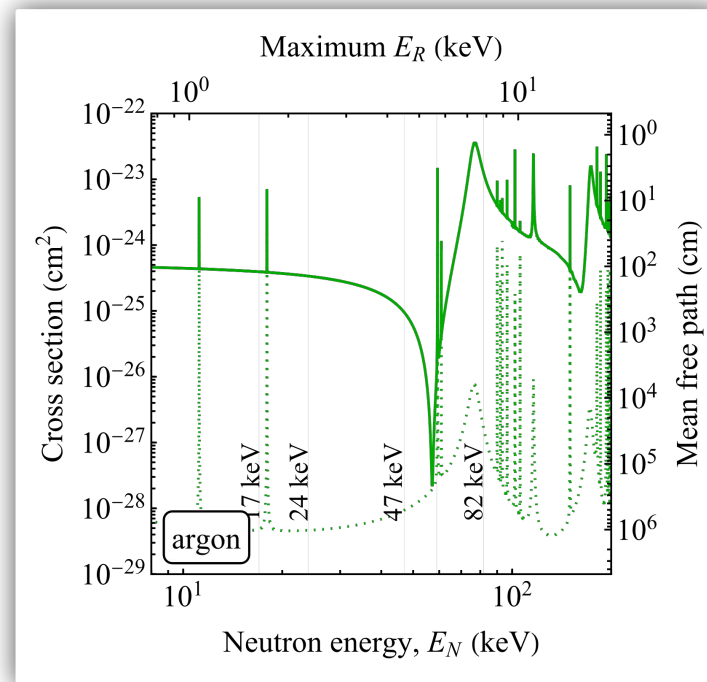
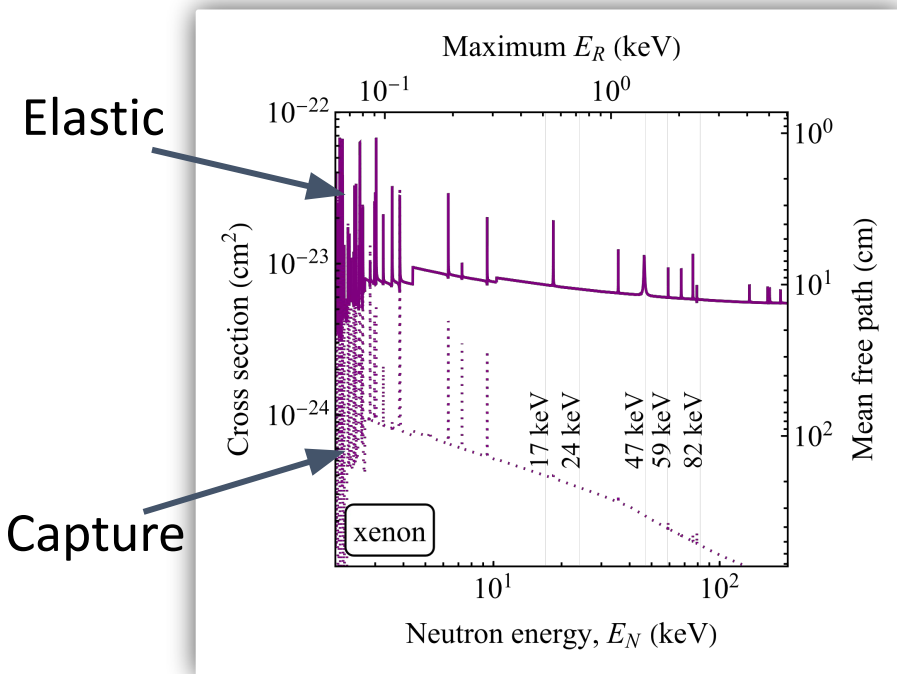


- Pros:**
- Potential for in situ
- Cons:**
- Small flux

Xu et al. [arXiv:2307.12952](https://arxiv.org/abs/2307.12952)



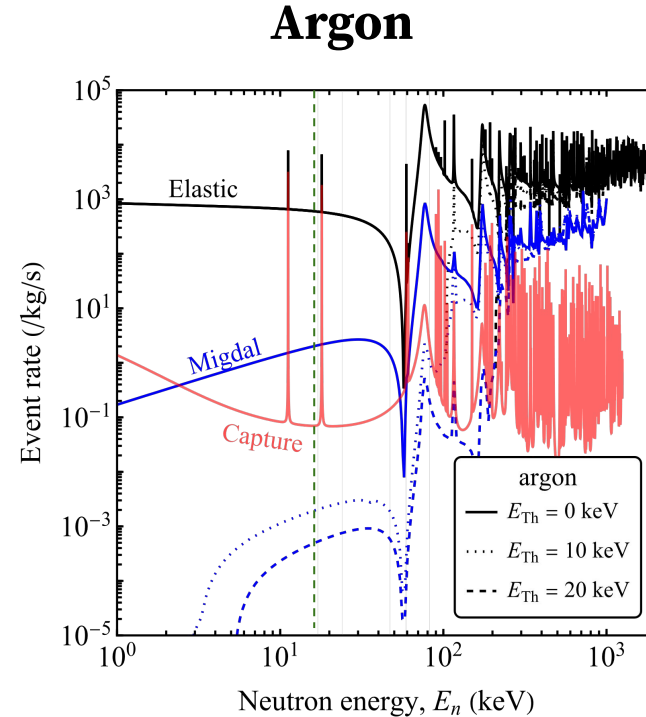
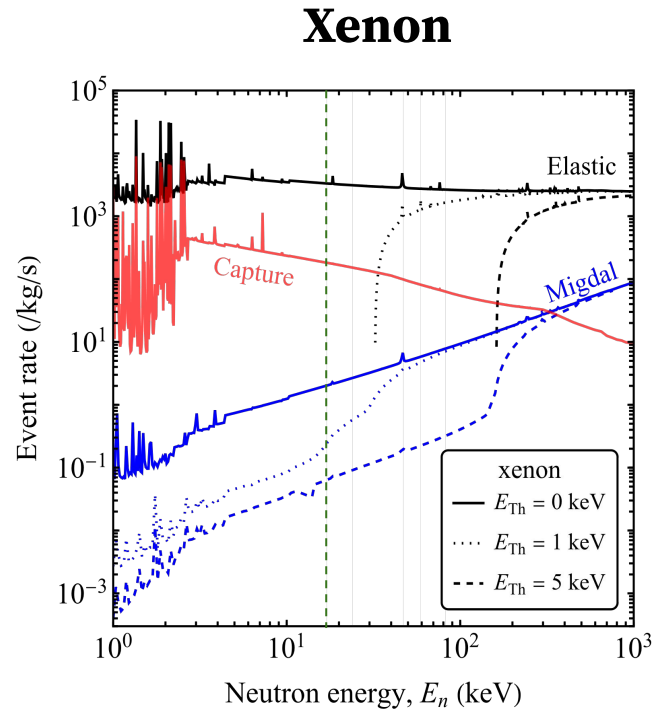
Low-energy neutron cross sections



- Radiative capture of neutrons will be a significant background
- Inelastic scattering is >100 keV threshold for all but xenon-129



Low-energy neutron scattering rates

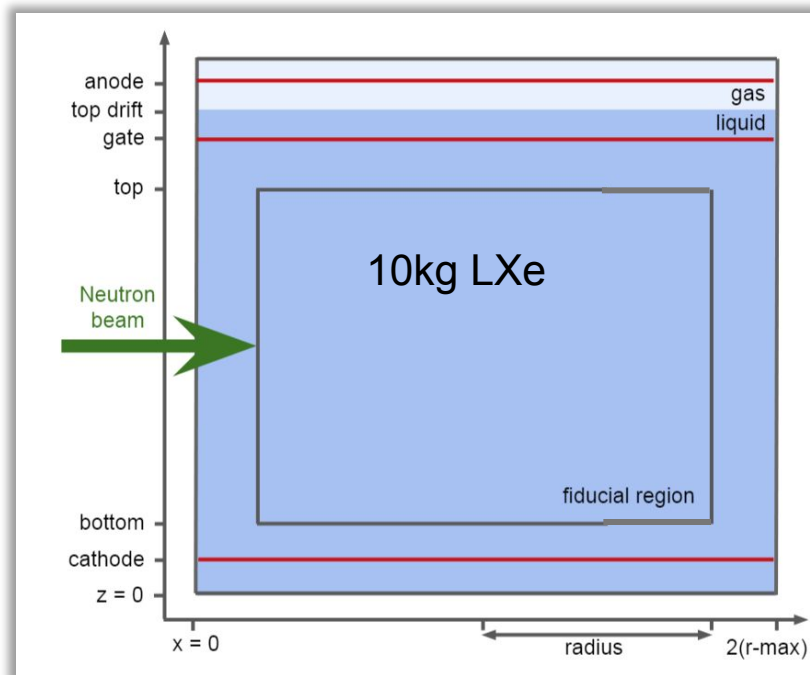


Simulation of LXe detector and neutron beam

Gaussian
neutron beam:

FWHM = 6cm
Peak flux = 10^8 n/hr
(avg 100 n/cm²/s)

Modelled on Barbeau
et al.



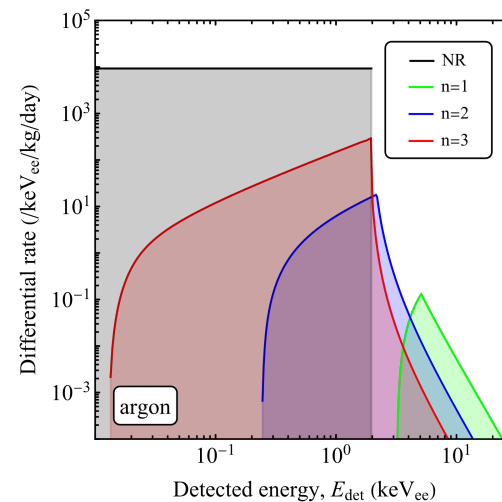
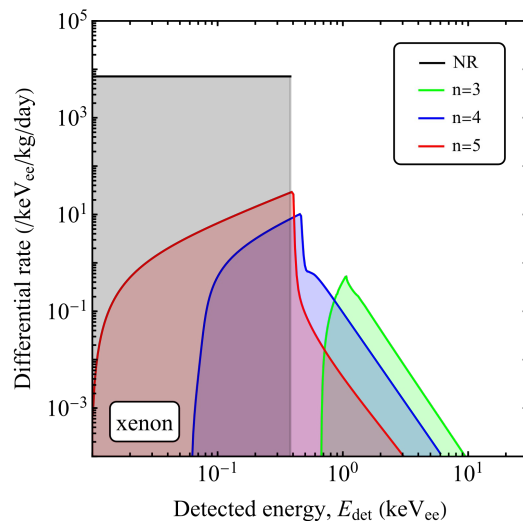
dimension	position (mm)
r_{\max}	120.
radius	100.
cathode	20.0
bottom	40.0
top	160.
gate	190.
top drift	195.
anode	200.

parameter	value
g_1	0.15 PE/ γ
g_2	24 PE/ e^-
field	300 V/cm
e^- lifetime	350. μ s
min S1	2 phd
min S2	250 phd
no. PMTs	60



Low-energy neutron Migdal rates

$E = 82 \text{ keV}$ neutrons, flux = $100 \text{ n/cm}^2/\text{s}$



Total rates:

Nuclear: 2,700 events/kg/s

Migdal: 8 events/kg/s

12,300 events/kg/s

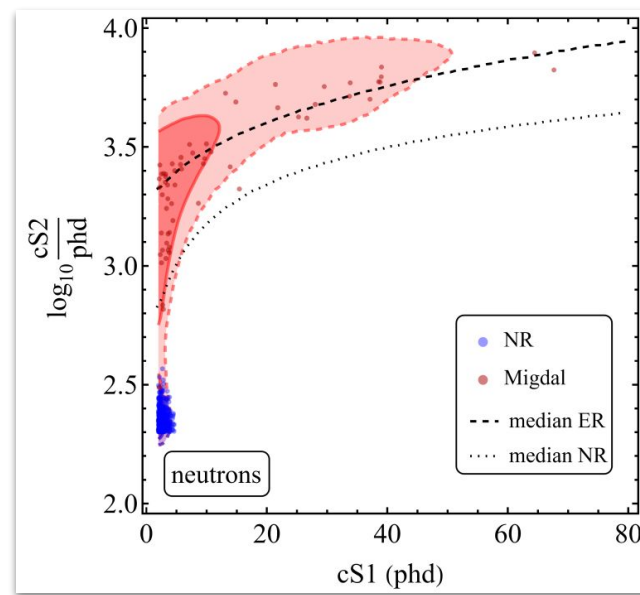
320 events/kg/s



Simulation with NEST (xenon)

Monte Carlo procedure:

1. Random NR energy from E_R distribution, calculate max. allowed E_{EM}
2. Loop over atomic shells, E_{nl} , and randomly ionize an electron with E_e
3. Calculate the yields of ions and excitons produced by E_R , E_e and E_{nl} using models for NR, β and β respectively
4. Calculate the quanta from the summed yields and then the subsequent S1 & S2

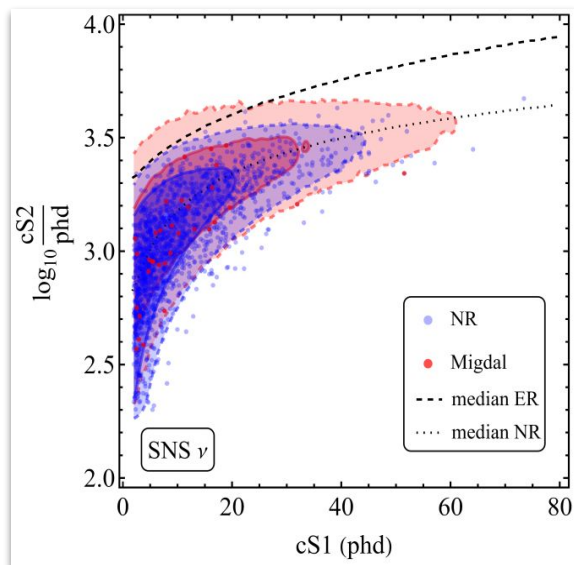


Source	Calc. ratio	Sim. ratio	Sim. rate/kg/day
neutron (17 keV)	6.0×10^{-4}	0.1	600

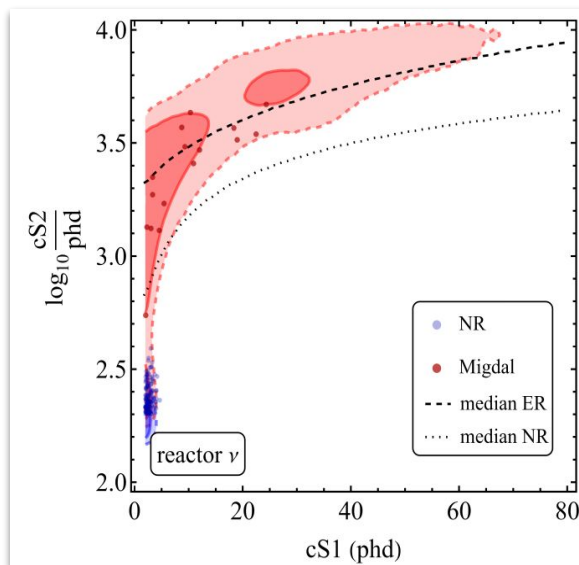


Brief aside: what about neutrino sources?

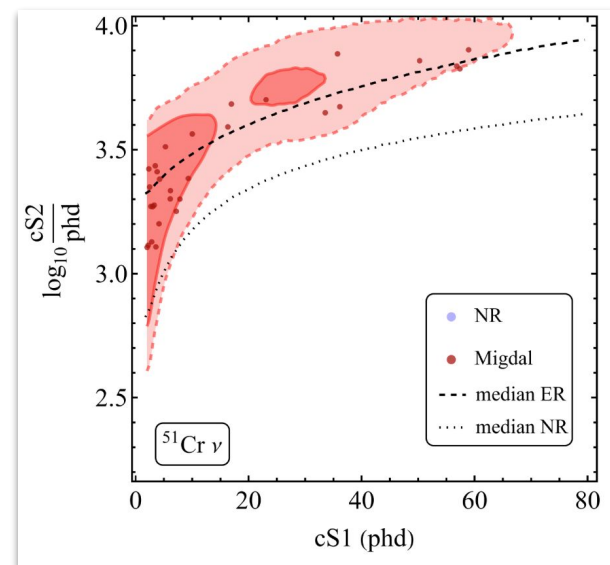
piDAR neutrinos:



Reactor neutrinos:



Radio-isotope:



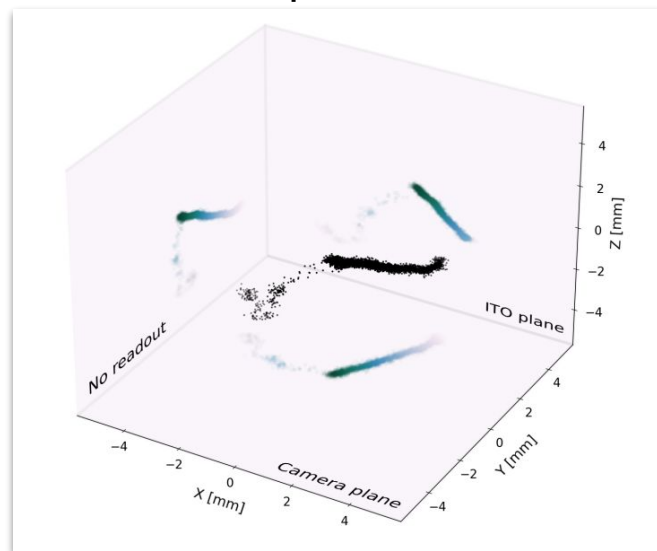
- Poor separation

- Require large exposures

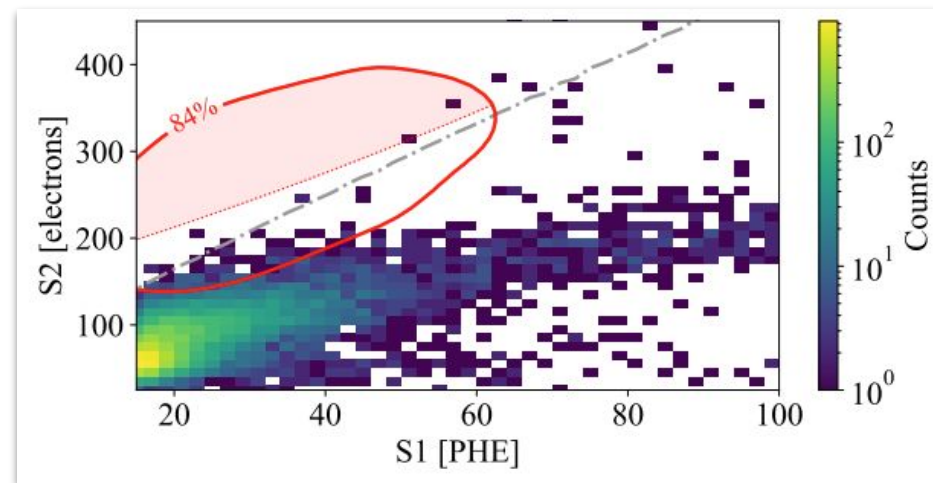


Current experimental calibration efforts

1. Verify theoretical predictions:
The MIGDAL experiment

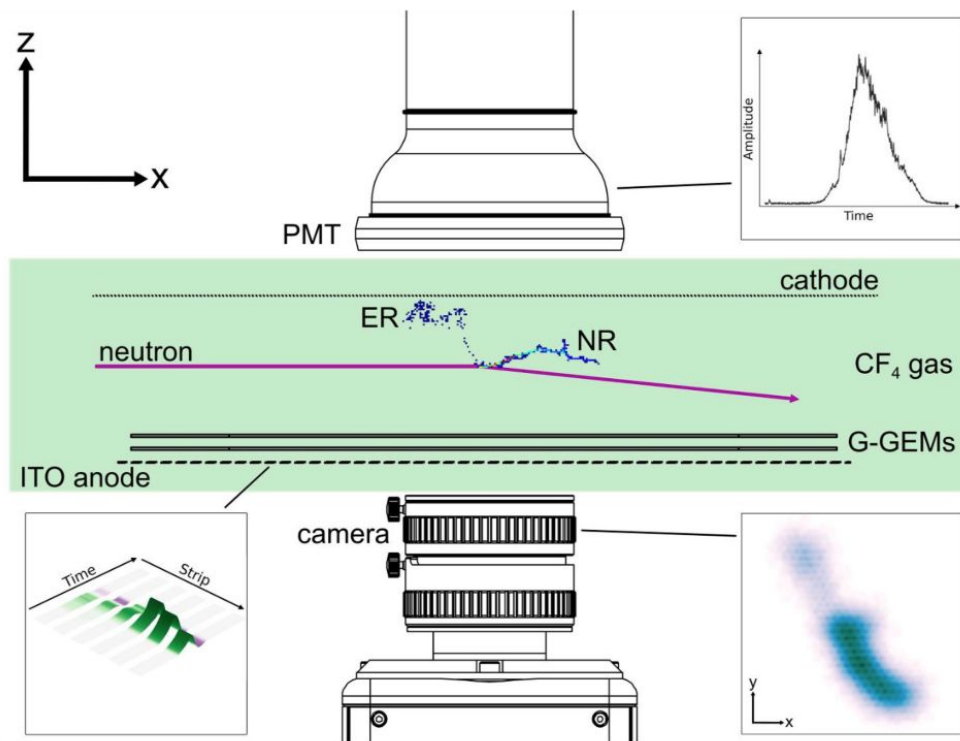


2. Detector response



1. Verify theoretical predictions: The MIGDAL experiment

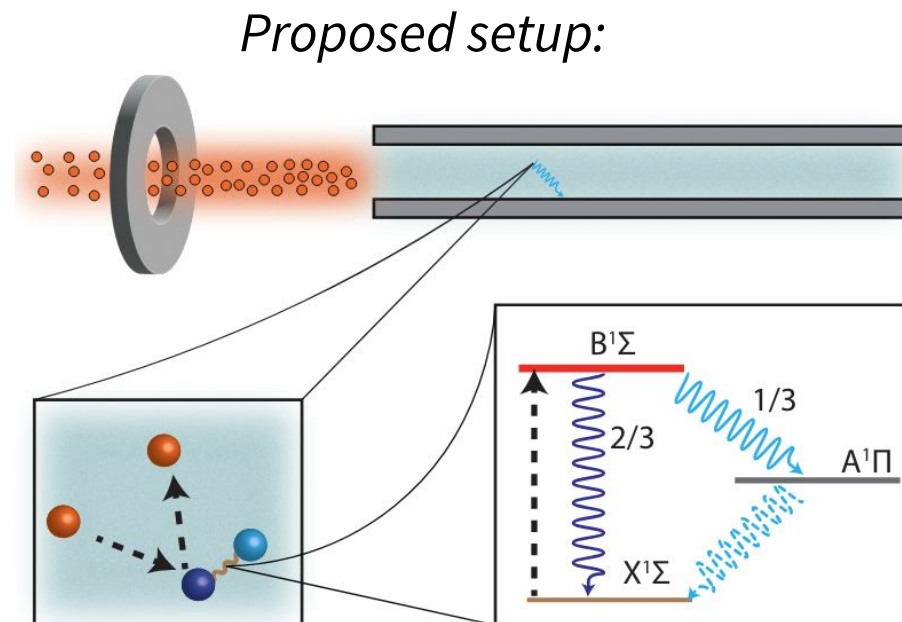
- ‘High’ energy neutron recoils (DD, DT)
- Low-pressure CF_4 gas
- Aim to observe a Migdal event topology
- Setup is operational at RAL



Xu et al. [arXiv:2307.12952](https://arxiv.org/abs/2307.12952)

1. Verify theoretical predictions: Molecular Migdal

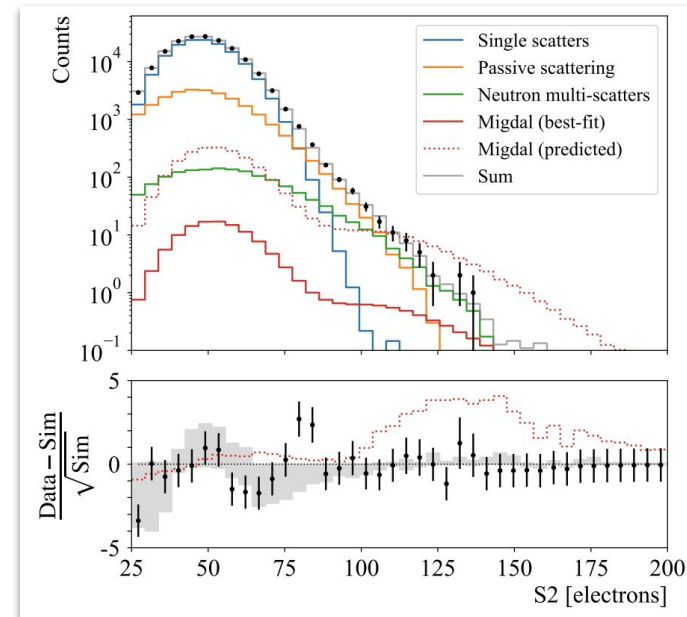
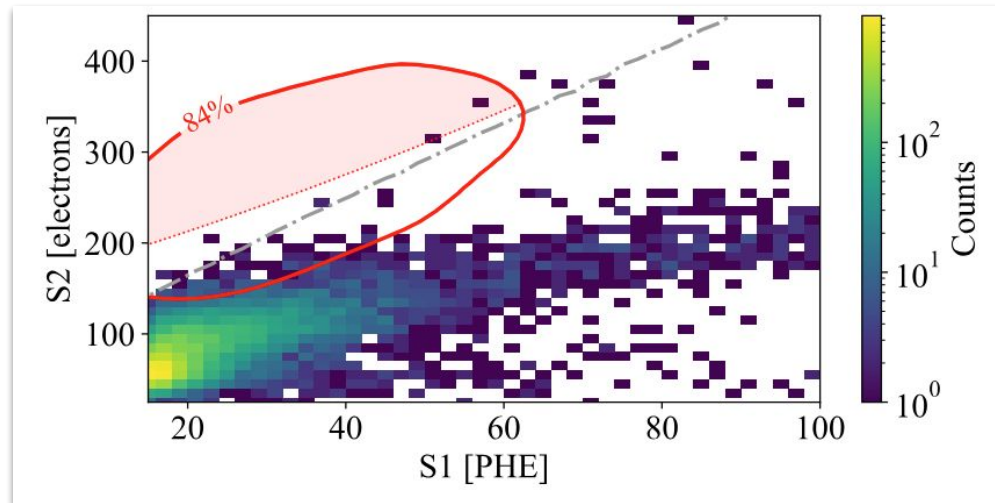
- Spallation neutron source (flux $\sim 10^8/\text{cm}^2/\text{s}$)
- Low-pressure CO gas
- Aim to observe a Migdal excitation
- Can have 5 sigma within hours



Y. Kahn et al. [arXiv:2403.08866](https://arxiv.org/abs/2403.08866)

2. Calibrating the detector response to the Migdal effect

Livermore group dedicated measurement
(DT generator 14 MeV neutrons, pick out 7 keV NR based on angle):

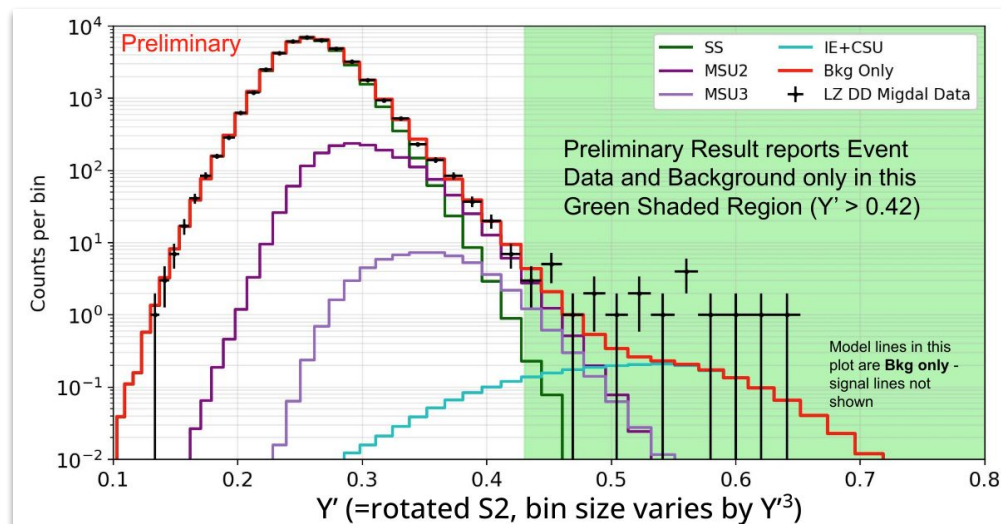
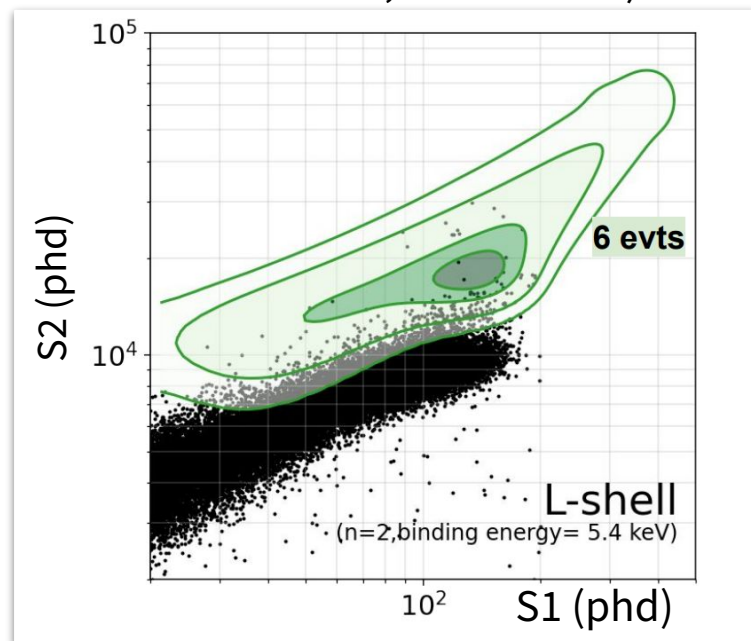


*Number of Migdal events
consistent with zero*

Xu et al. [arXiv:2307.12952](https://arxiv.org/abs/2307.12952)

2. Calibrating the detector response to the Migdal effect

LZ *in situ* measurement (DD generator
2.45 MeV neutrons, >20 keV NR):

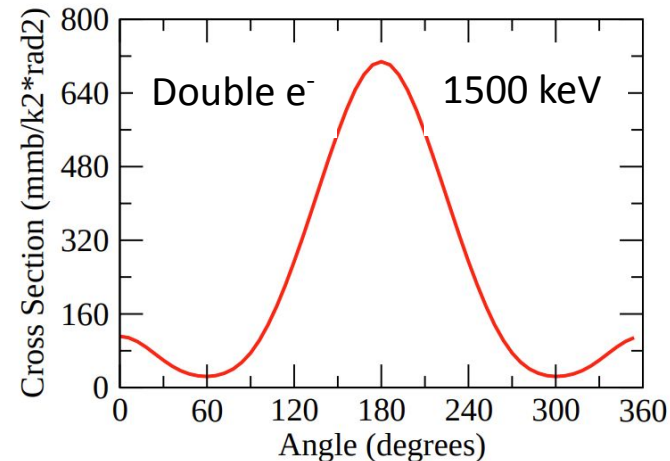
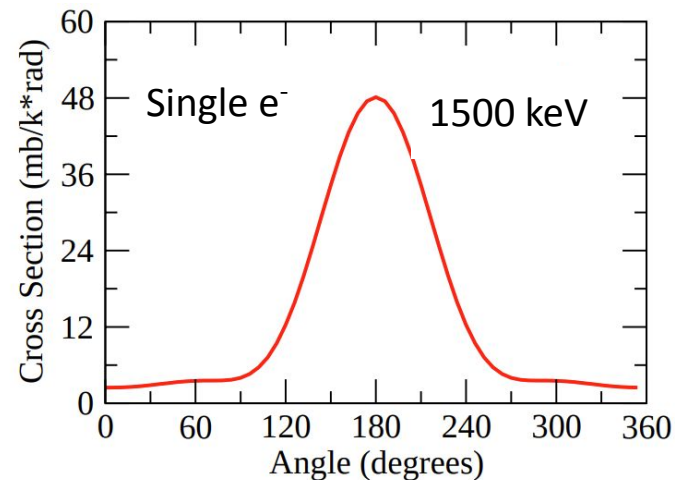
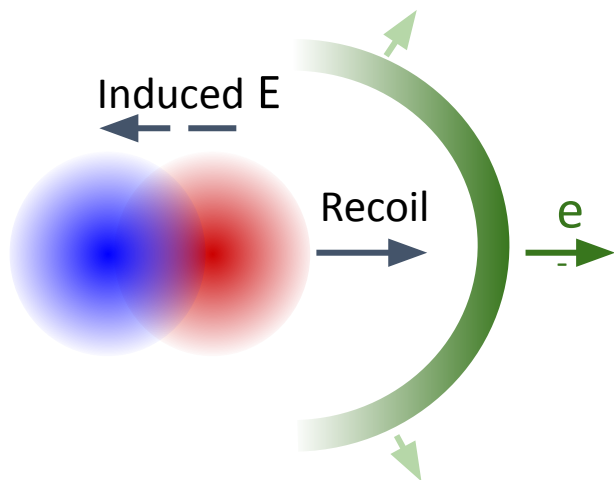


Bang (LZ Collaboration) [UCLADM2023 talk](#)



Directional Migdal Effect?

- **Predictions for neutron scattering on He**
 Single ionization has forward-only e
 Double ionization has slight backward e

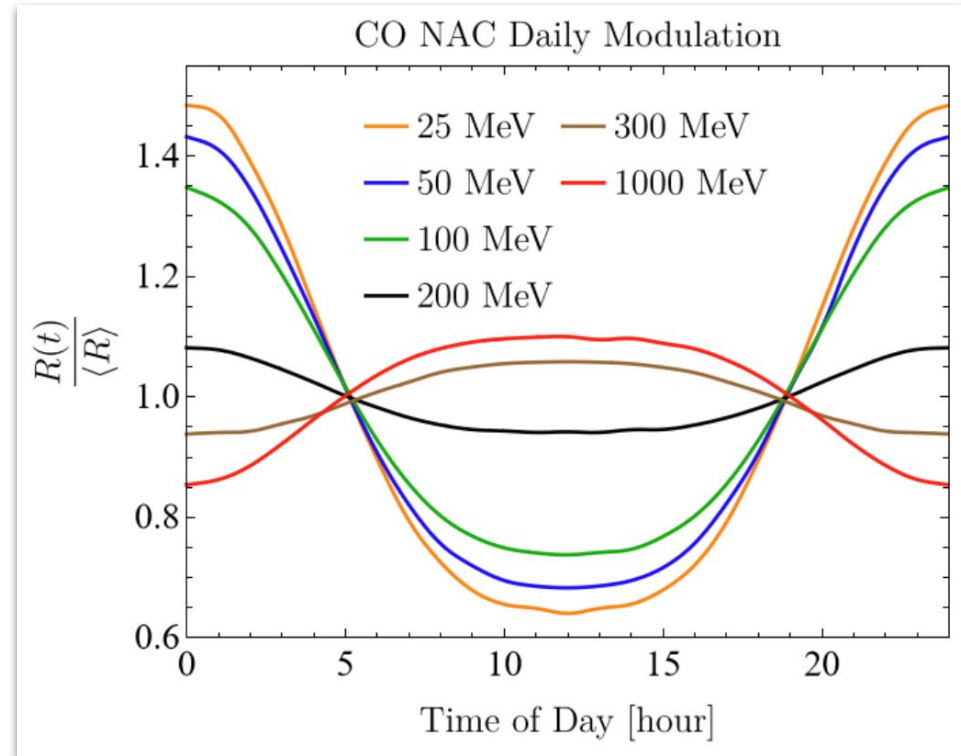


Pindzola et al. [J. Phys. B 53 \(2020\)](#)



Migdal in molecules

- **Hard**, only computed for simple molecules
- The probability depends on the molecular axis \rightarrow indirect/statistical directional information
- Non-adiabatic coupling of ground states to excited states provide another (much larger) contribution to Migdal excitation

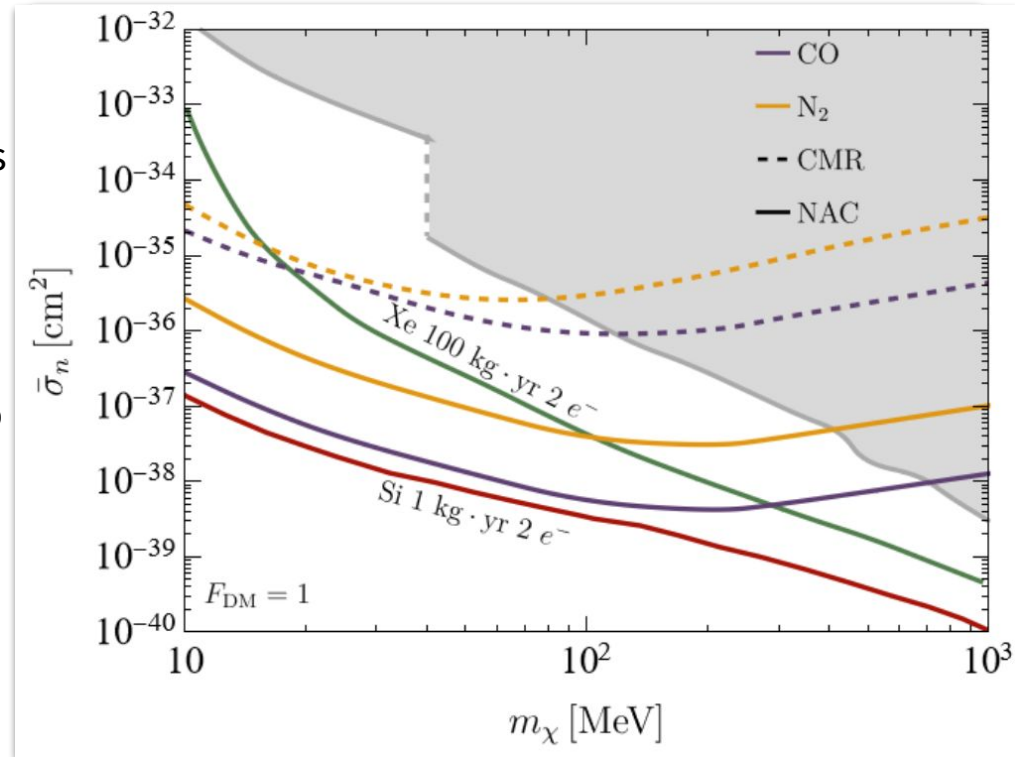


Blanco et al. [arXiv:2208.09002](https://arxiv.org/abs/2208.09002)



Migdal in molecules

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Blanco et al. [arXiv:2208.09002](https://arxiv.org/abs/2208.09002)



Summary

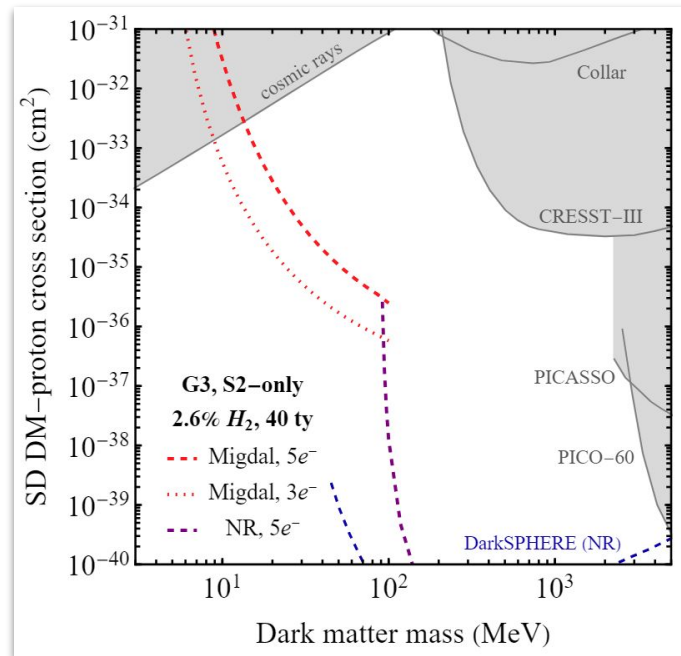
- The Migdal effect allows access to lighter DM, especially when used in concert with H_2 doping
- It's important to both verify experimental predictions *and* calibrate detector responses \rightarrow experimental determinations of both are underway
- Directional nature of the Migdal effect, especially in molecules, is interesting \rightarrow more investigation needed

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~/code\$

<https://github.com/jaydenn/nuMigdalCalc>

<https://github.com/jaydenn/thinNEST>

<https://github.com/jaydenn/MigdalMC>

