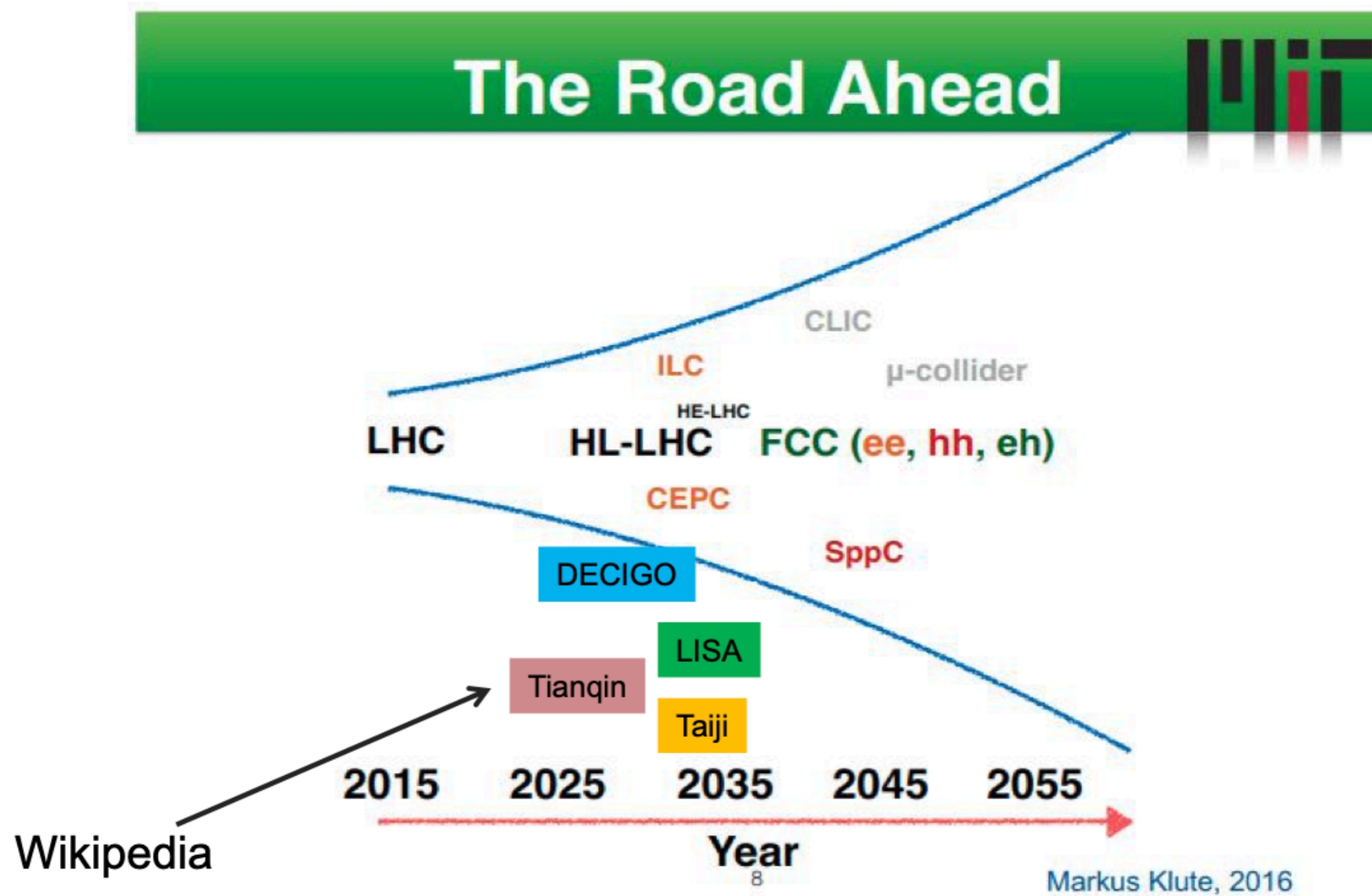


BSM Physics  
at  
Gravitational Wave Detectors

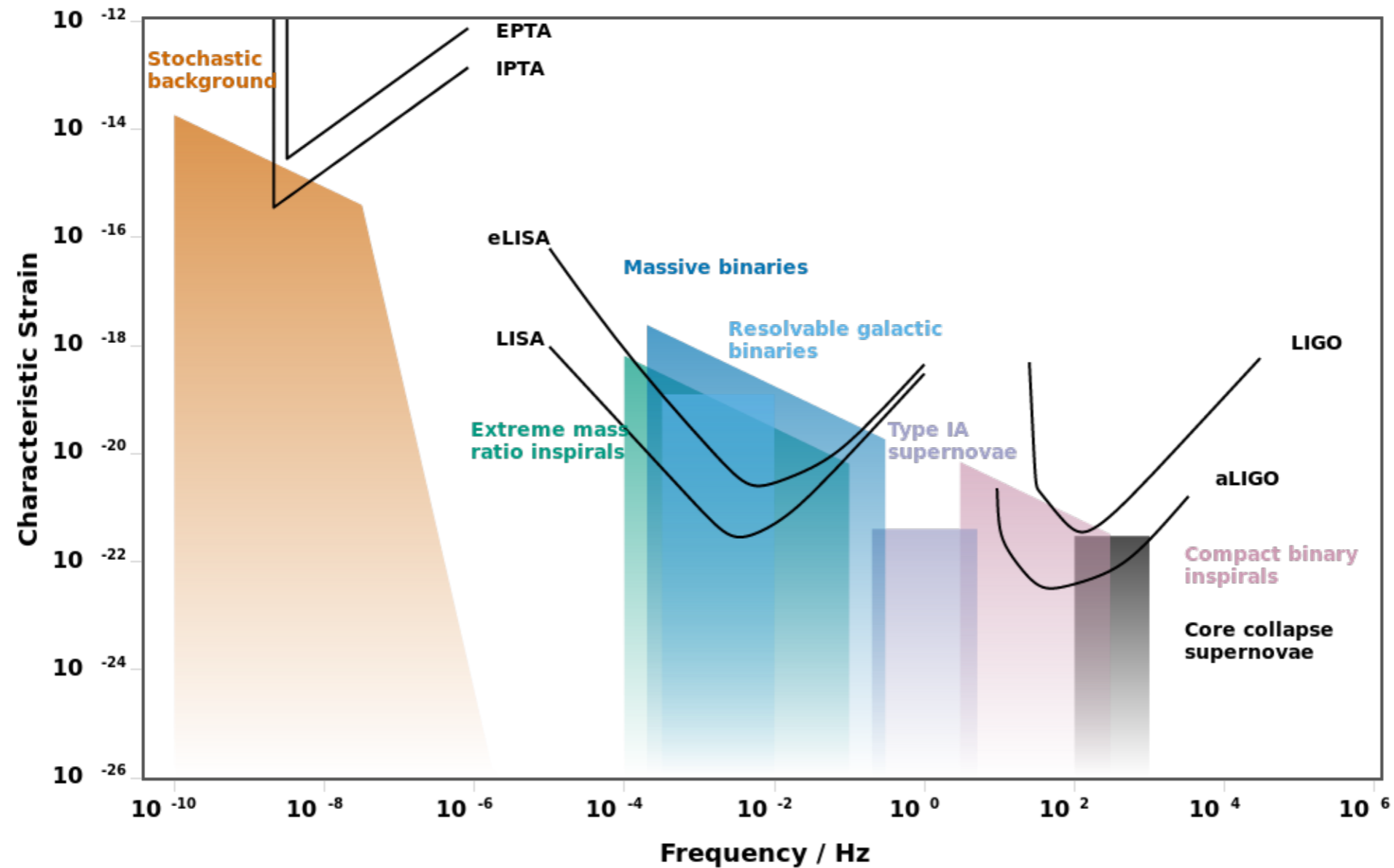
CETUP\* Workshop 2024

Kuver Sinha  
University of Oklahoma

# Data's coming, folks



# Data's coming, folks



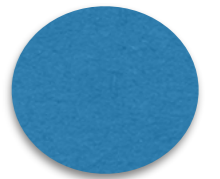
How do we leverage this to explore BSM physics?

# BSM choices

---



graviton



Do you want to study BSM at the source?

or (and)

Do you want to study BSM in what happens on the way?



*BSM at the Source*

# BSM at Source

---



Source itself is due to BSM physics (phase transitions)

Source is astrophysical, BSM exchange deforms signal

Source is astrophysical, probes BSM in its environment

Source is astrophysical, serves as a clock (multimessenger)

# Source: Phase Transition

---

Take the simplest template (xSM) and obtain robust GW predictions

mass resummation in thermal field theory

modeling of relativistic hydrodynamics for sound waves in plasma

*needs a lot of work*

H. Guo, J.No, F. Hajkarim, **KS**, G. White (JHEP06 2021)

H. Guo, **KS**, G. White, D. Vagie (JHEP06 2021)

H. Guo, **KS**, G. White, D. Vagie (JCAP01 2021)

Take various particle physics models and obtain GW predictions

deformed Higgs sectors, extra scalars, SSB of gauge groups, etc.

connect to dark sectors, baryogenesis, flavor physics, etc.

typically use fit functions for GW spectrum

*lots of interesting work by our community!*

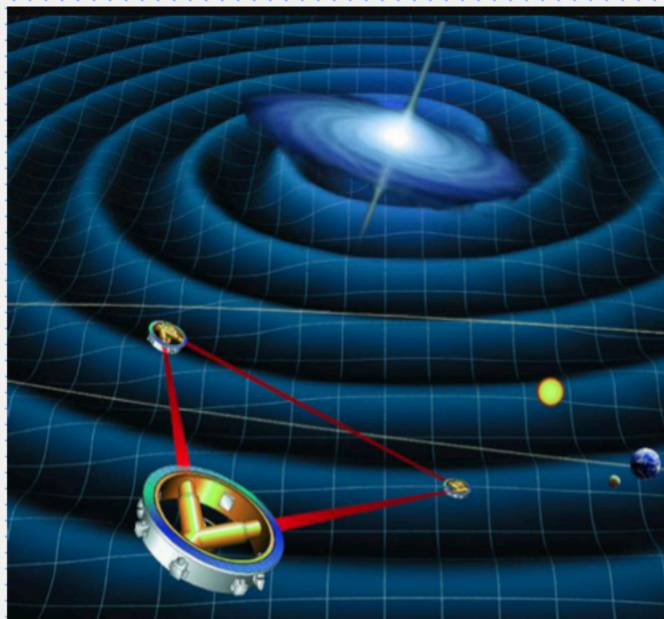
A. Alves, T. Ghosh, D. Goncalves, H. Guo, **KS** (JHEP03 2020)

A. Alves, T. Ghosh, H. Guo, **KS** (JHEP04 2019)

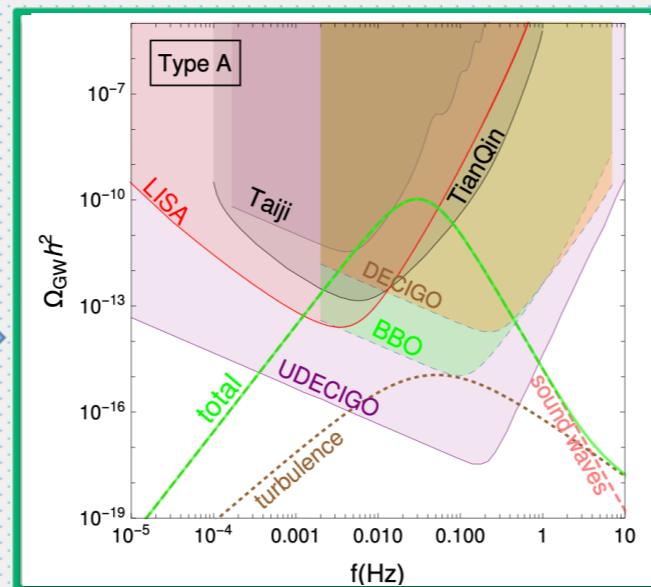
A. Alves, T. Ghosh, H. Guo, **KS** (JHEP12 2018)

# Workflow: Phase Transitions

theoretical calculation of gravitational wave spectrum and detector simulation



LIGO, LISA, Taiji, Tianqin...



Gravitational Wave Spectrum

$\alpha$   
 $\beta$   
 $v_w$   
 $T_*$   
 $g_s$   
 ...

Phase Transition Parameters

Standard Model of Elementary Particles					
three generations of matter (fermions)			interactions / force carriers (bosons)		
I	II	III			
mass $\approx 2.2 \text{ MeV}/c^2$ charge $2/3$ spin $1/2$ <b>u</b> up	mass $\approx 1.28 \text{ GeV}/c^2$ charge $2/3$ spin $1/2$ <b>c</b> charm	mass $\approx 173.1 \text{ GeV}/c^2$ charge $2/3$ spin $1/2$ <b>t</b> top	mass 0 charge 0 spin 1 <b>g</b> gluon	mass $\approx 124.97 \text{ GeV}/c^2$ charge 0 spin 0 <b>H</b> higgs	
mass $\approx 4.7 \text{ MeV}/c^2$ charge $-1/3$ spin $1/2$ <b>d</b> down	mass $\approx 96 \text{ MeV}/c^2$ charge $-1/3$ spin $1/2$ <b>s</b> strange	mass $\approx 4.18 \text{ GeV}/c^2$ charge $-1/3$ spin $1/2$ <b>b</b> bottom	mass 0 charge 0 spin 1 <b><math>\gamma</math></b> photon	<b>BSM</b>	
mass $\approx 0.511 \text{ MeV}/c^2$ charge $-1$ spin $1/2$ <b>e</b> electron	mass $\approx 105.66 \text{ MeV}/c^2$ charge $-1$ spin $1/2$ <b><math>\mu</math></b> muon	mass $\approx 1.7768 \text{ GeV}/c^2$ charge $-1$ spin $1/2$ <b><math>\tau</math></b> tau	mass $\approx 91.19 \text{ GeV}/c^2$ charge 0 spin 1 <b>Z</b> Z boson	Gauge bosons	
mass $< 1.0 \text{ eV}/c^2$ charge 0 spin $1/2$ <b><math>\nu_e</math></b> electron neutrino	mass $< 0.17 \text{ MeV}/c^2$ charge 0 spin $1/2$ <b><math>\nu_\mu</math></b> muon neutrino	mass $< 18.2 \text{ MeV}/c^2$ charge 0 spin $1/2$ <b><math>\nu_\tau</math></b> tau neutrino	mass $\approx 80.39 \text{ GeV}/c^2$ charge $\pm 1$ spin 1 <b>W</b> W boson	Vector bosons	
			SCALAR BOSONS		

Particle Physics Model

data analysis, constraints or discovery (parameter estimation)

# Uncertainties in Phase Transition Calculations

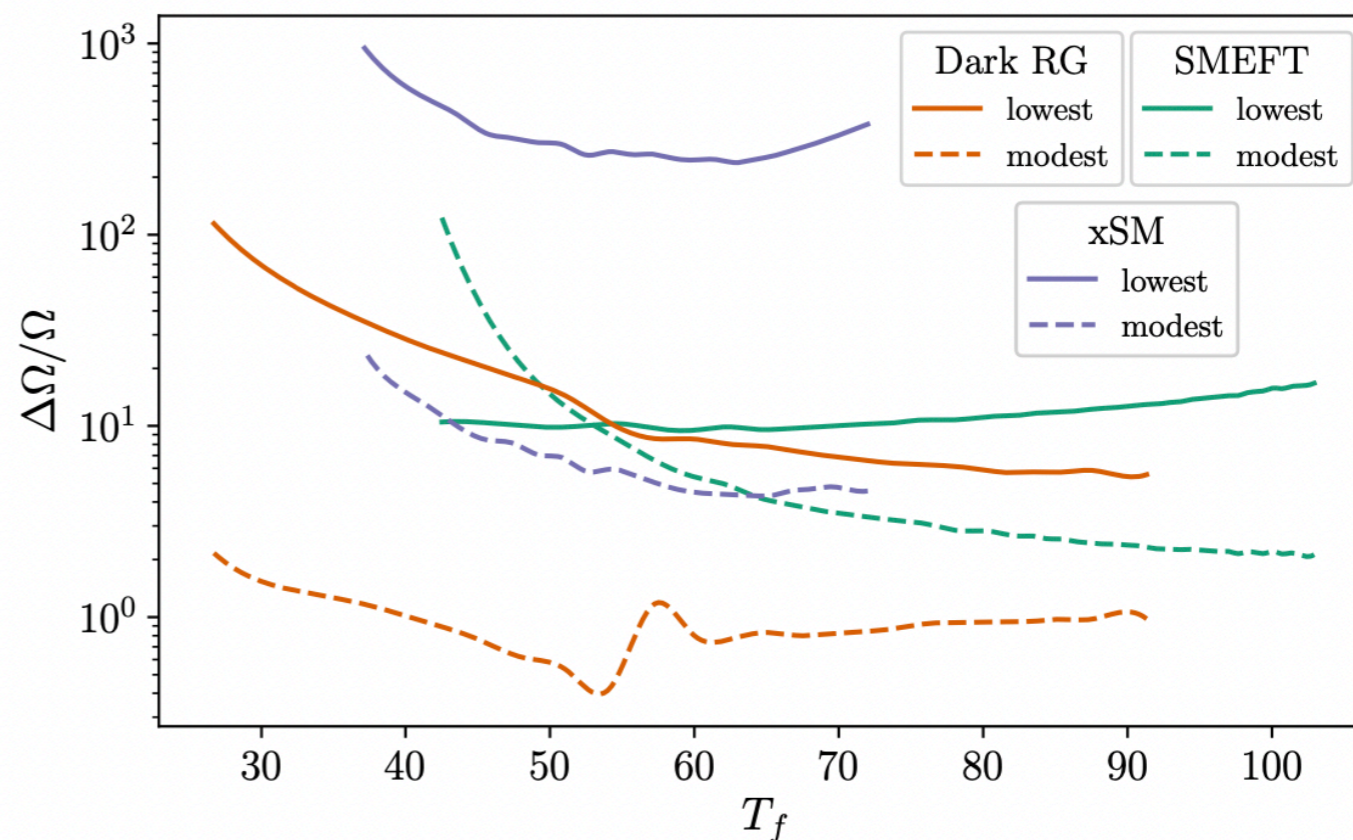


$\Delta\Omega_{\text{GW}}/\Omega_{\text{GW}}$	4d approach	3d approach
RG scale dependence	$\mathcal{O}(10^2 - 10^3)$	$\mathcal{O}(10^0 - 10^1)$
Gauge dependence	$\mathcal{O}(10^1)$	$\mathcal{O}(10^{-3})$
High- $T$ approximation	$\mathcal{O}(10^{-1} - 10^0)$	$\mathcal{O}(10^0 - 10^2)$
Higher loop orders	unknown	$\mathcal{O}(10^0 - 10^1)$
Nucleation corrections	unknown	$\mathcal{O}(10^{-1} - 10^0)$
Nonperturbative corrections	unknown	unknown

Croon, Gould, Schicho, Tenkanen, White, JHEP04(2021)055

Effect	Range of error (medium)	Range of error (low)	Type of error
Transition temperature	$\mathcal{O}(10^{-4} - 10^1)$	$\mathcal{O}(10^{-1} - 10^0)$	Random
Mean bubble separation	$\mathcal{O}(0 - 10^{-1})$	$\mathcal{O}(10^{-1} - 10^0)$	Suppression
Fluid velocity	$\mathcal{O}(10^{-2} - 10^0)$	$\mathcal{O}(10^{-2} - 10^0)$	Random
Finite lifetime	$\mathcal{O}(10^{-3} - 10^{-1})$	$\mathcal{O}(10^1 - 10^3)$	Enhancement
Vorticity effects	$\mathcal{O}(10^{-1} - 10^0)$	—	Random

$v_w = 0.92$



H. Guo, J.No, F. Hajkarim, **KS**, G. White (JHEP06 2021)

H. Guo, **KS**, G. White, D. Vagie (JHEP06 2021)

H. Guo, **KS**, G. White, D. Vagie (JCAP01 2021)



# Precision GW Calculations

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## False vacuum fraction

H. Guo, **KS**, G. White, D. Vagie (JHEP06 2021)

The false vacuum fraction at  $t > t_c$  in an expanding universe is defined as

$$g(t_c, t) = \exp \left[ -\frac{4\pi}{3} \int_{t_c}^t dt' p(t') a^3(t') r(t', t)^3 \right] \equiv \exp [-I(t)], \quad (2.16)$$

where  $I(t)$  represents the volume of nucleated bubbles per comoving volume, double counting the overlapped space between bubbles and virtual bubbles within others [112]. The comoving radius of a bubble nucleated at  $t'$  and measured at  $t$  is

$$r(t', t) = \int_{t'}^t dt'' \frac{v_w}{a(t'')} = v_w (\eta' - \eta), \quad (2.17)$$

## False vacuum fraction - function of temperature

$$r(T', T) = \frac{v_w}{a_c} \int_T^{T'} \frac{dT''}{T''} \frac{1}{\gamma H(T'')} \left( \frac{T_c}{T''} \right)^{-1/\gamma}, \quad (2.24)$$

$$I(T) = \frac{4\pi}{3} \int_T^{T_c} \frac{dT'}{T'} \frac{1}{\gamma H(T')} \bar{p}_0 T'^4 \exp \left[ -\frac{S_3(T')}{T'} \right] \left( \frac{T_c}{T'} \right)^{3/\gamma} [a_c r(T', T)]^3, \quad (2.25)$$

with  $g(T_c, T) = \exp [-I(T)]$ .

# Precision GW Calculations

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## Percolation temperature

H. Guo, **KS**, G. White, D. Vagie (JHEP06 2021)

With the false vacuum fraction now defined as a function of temperature, the percolation temperature occurs when the false vacuum fraction is 70% of the total volume, i.e., when

$$g(T_p) = 0.7. \quad (2.26)$$

Similarly, the temperature when the phase transition ends occurs at the time when the volume of nucleated bubbles equals the comoving volume, i.e.  $I(t_f) = 1$ . This translates into

$$g(T_f) = e^{-1}. \quad (2.27)$$

In most cases, the percolation temperature calculated from Eq. 2.26 should roughly coincide with the final temperature calculated from Eq. 2.27 and depend on  $v_w$  and  $\Delta V$ .

## Bubble number density

The evolution of the mean bubble density per proper volume is determined by

$$\frac{d [n_b a^3(t)]}{dt} = p(t) g(t_c, t) a^3(t), \quad (2.28)$$

which begins at  $n_b(t_c) = 0$  and includes all the bubbles ever formed. We then transform the above result into an integral over temperature:

$$n_b(T) = \left(\frac{T}{T_c}\right)^{3/\gamma} \int_T^{T_c} \frac{dT'}{T'} \frac{1}{\gamma H(T')} \bar{p}_0 T'^4 \exp\left[-\frac{S_3(T')}{T'}\right] g(T_c, T') \left(\frac{T_c}{T'}\right)^{3/\gamma}. \quad (2.29)$$

# Precision GW Calculations

---

## Calculation of mean bubble separation

The mean bubble separation  $R_*$  is related to the mean bubble number density and is given by

$$R_* = \left( \frac{1}{n_b} \right)^{1/3}. \quad (2.31)$$

## Calculation of $\beta$

$$R_*(\eta) = \frac{a(\eta)}{a(\eta_f)} (8\pi)^{1/3} \frac{v_w}{\beta(v_w)}, \quad (2.38)$$

where  $R_{*,c} = R_*/a(\eta)$  and  $\beta_c = a(\eta_f)\beta$ . The above result can be transformed into a function of temperature using a relation similar to Eq. 2.21 to give

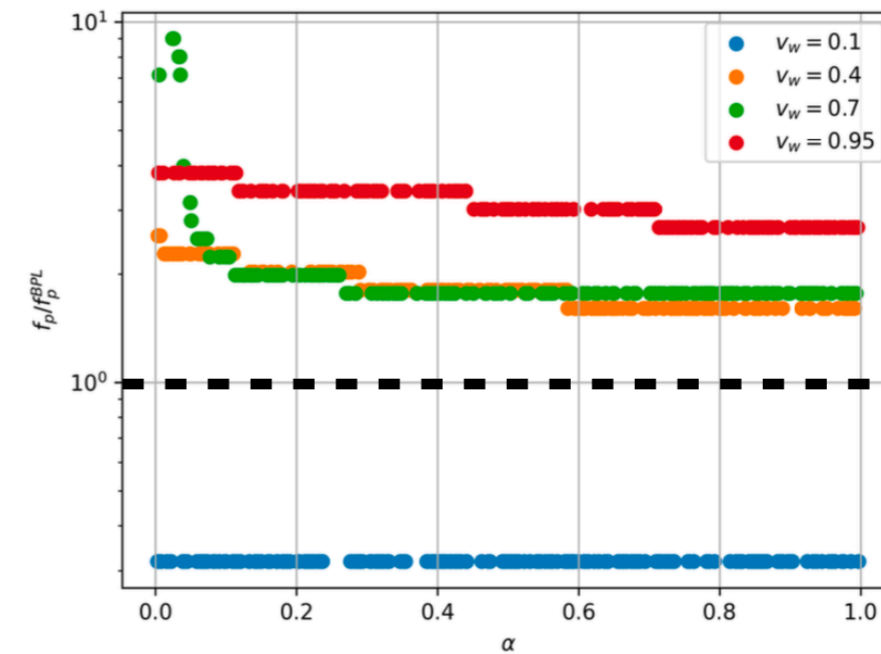
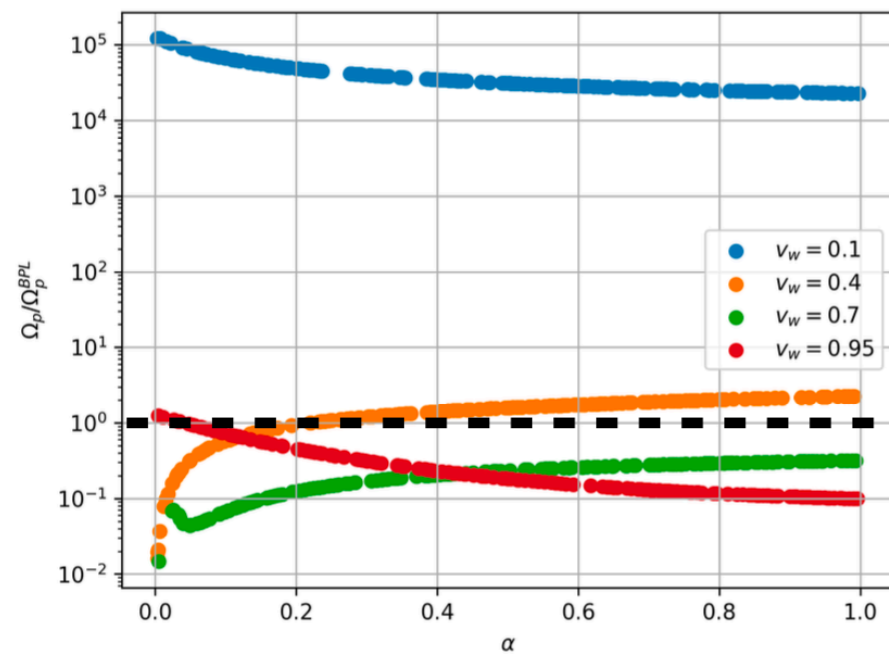
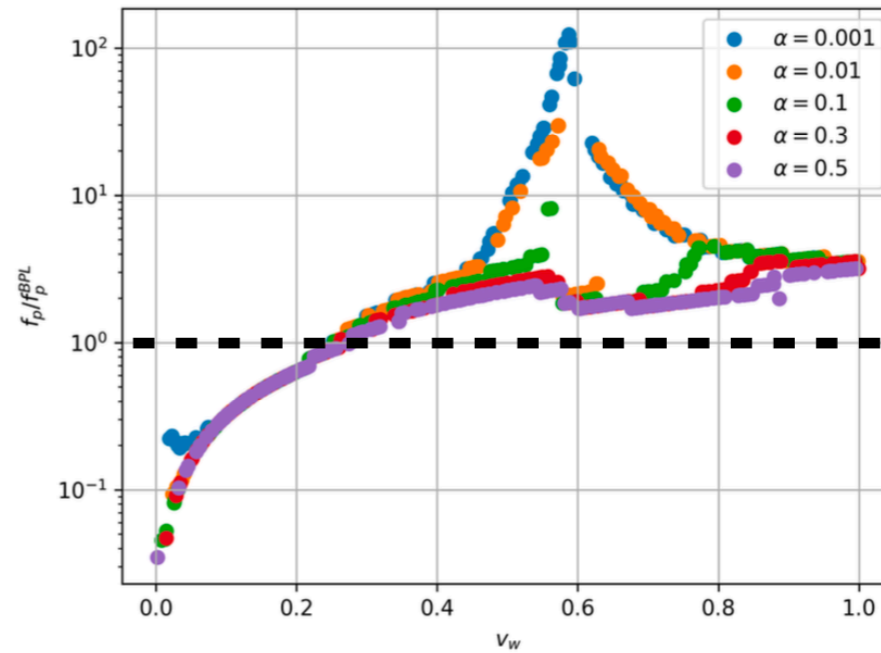
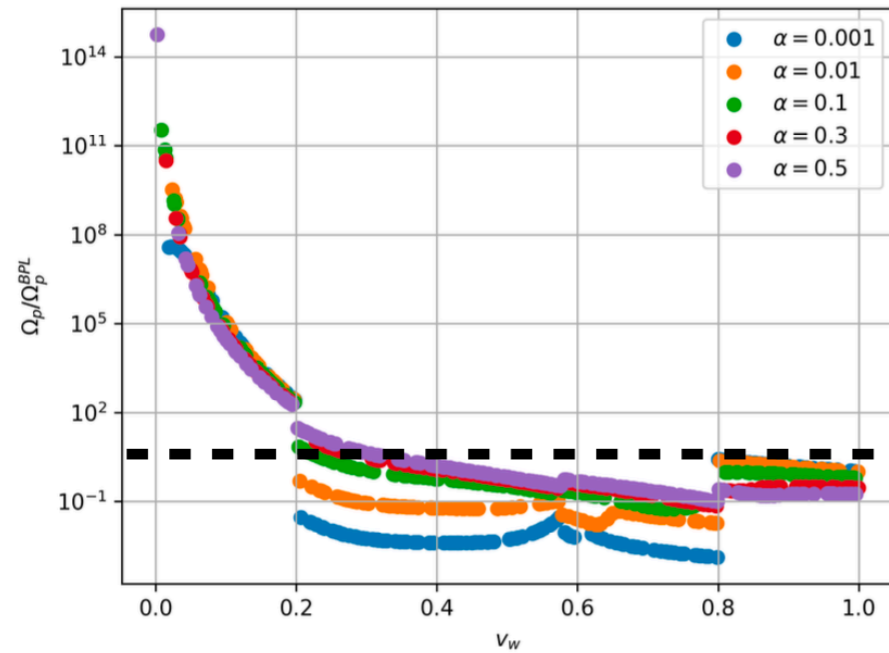
$$\frac{a(\eta)}{a(\eta_f)} = \left( \frac{T_f}{T} \right)^{1/\gamma}. \quad (2.39)$$

The procedure to calculate the inverse time duration of the phase transition at  $T_f$  for a fixed  $v_w$  is

1. Find  $T_f$  from the false vacuum fraction  $g(T_c, T)$  for when  $I(T_f) = 1$  ;
2. Calculate  $n_b(T_f)$  ;
3. Use  $R_*(T_f) = \left( \frac{1}{n_b(T_f)} \right)^{1/3}$  ;
4. Solve Eq. 2.38 using Eq. 2.39 to get  $\beta(v_w)$ .



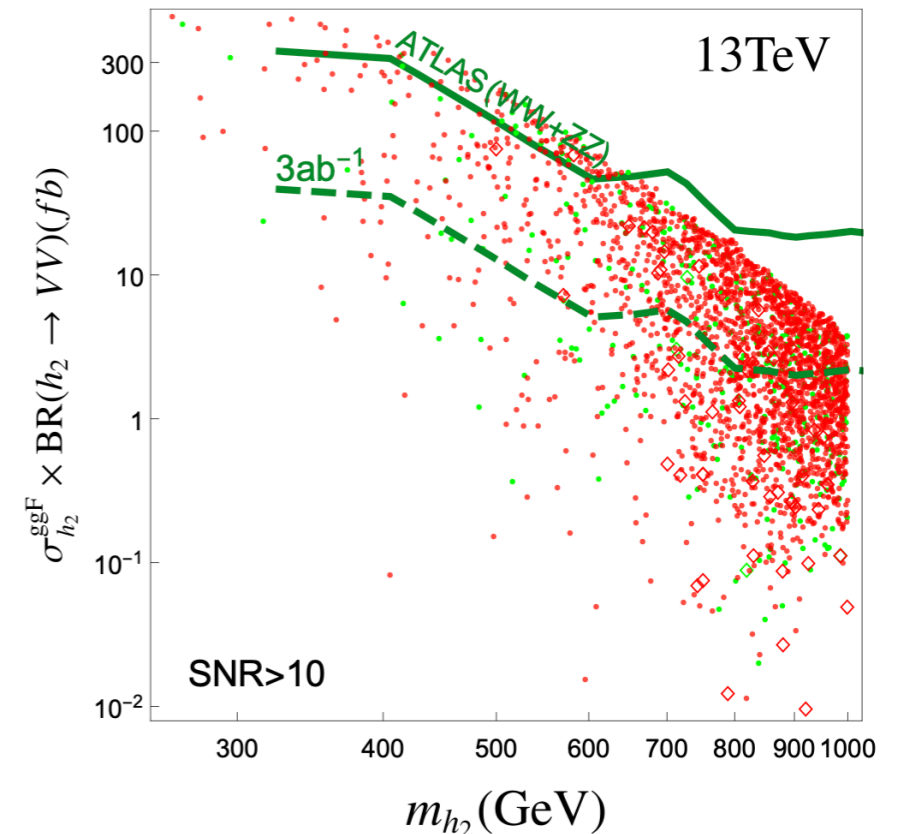
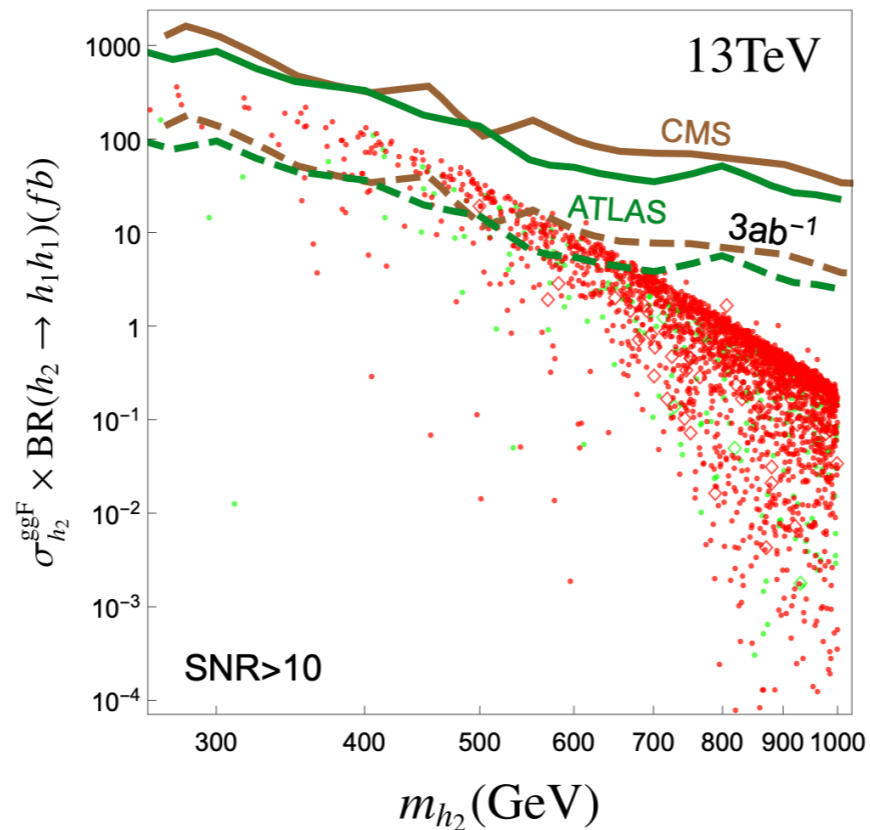
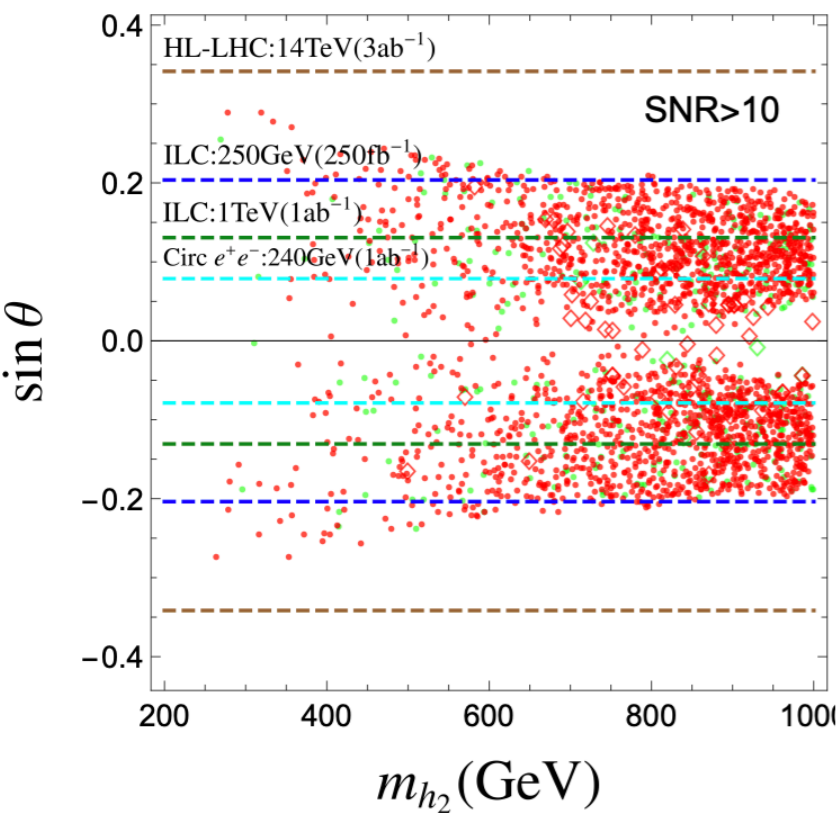
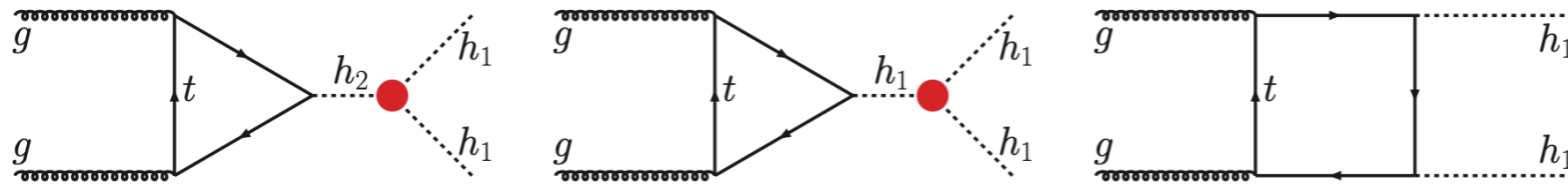
# Uncertainties in Phase Transition Calculations



# Complementarity

$$V(H, S) = -\mu^2 H^\dagger H + \lambda(H^\dagger H)^2 + \frac{a_1}{2} H^\dagger H S + \frac{a_2}{2} H^\dagger H S^2 + \frac{b_2}{2} S^2 + \frac{b_3}{3} S^3 + \frac{b_4}{4} S^4$$

- A. Alves, T. Ghosh, D. Goncalves, H. Guo, **KS** (PLB818 2021)
- A. Alves, T. Ghosh, D. Goncalves, H. Guo, **KS** (JHEP03 2020)
- A. Alves, T. Ghosh, H. Guo, **KS** (JHEP04 2019)
- A. Alves, T. Ghosh, H. Guo, **KS** (JHEP12 2018)



# BSM at Source

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Source itself is due to BSM physics (phase transitions)

Source is astrophysical, BSM exchange deforms signal

Source is astrophysical, probes BSM in its environment

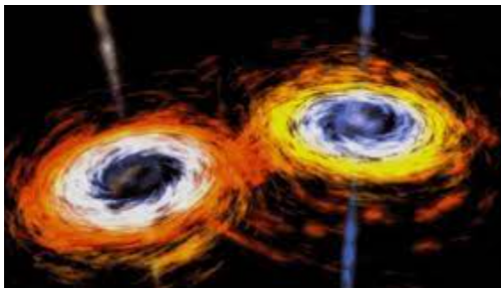
Source is astrophysical, serves as a clock (multimessenger)

# Binary Inspiral

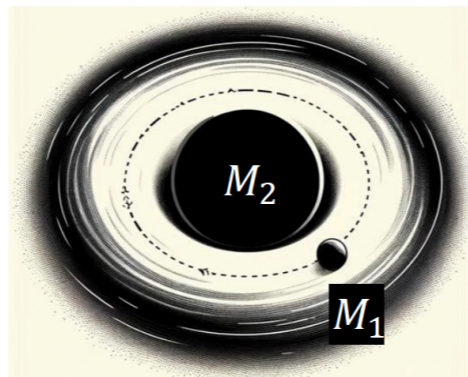
Binary inspirals can serve as probes of light dark mediators, under the assumption that they accumulate dark charge

The wavelength of the mediator that can be probed is primarily fixed by the length scale of the binary system

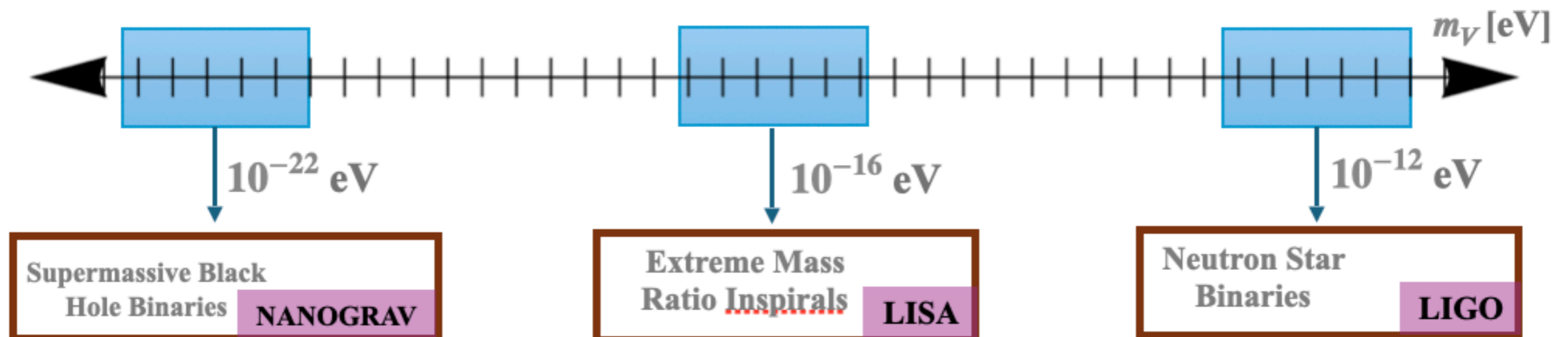
Dror, Lehmann, Profumo (PRD104 2021)



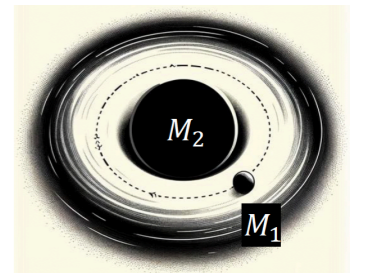
Bhalla, KS, Xu (2024)



Dror, Laha, Opferkuch (PRD102, 2020)  
Kopp, Laha, Opferkuch, Shepherd (JHEP 11, 2018)  
Croon, Nelson, Sun, Walker (APJL 858,2018)



# EMRIs, Dark Forces



$$|\vec{F}_{\text{total}}| = \frac{GM_1M_2}{r^2} [1 + \tilde{\alpha}' e^{-m_V r} (1 + m_V r)],$$

time evolution of orbital frequency

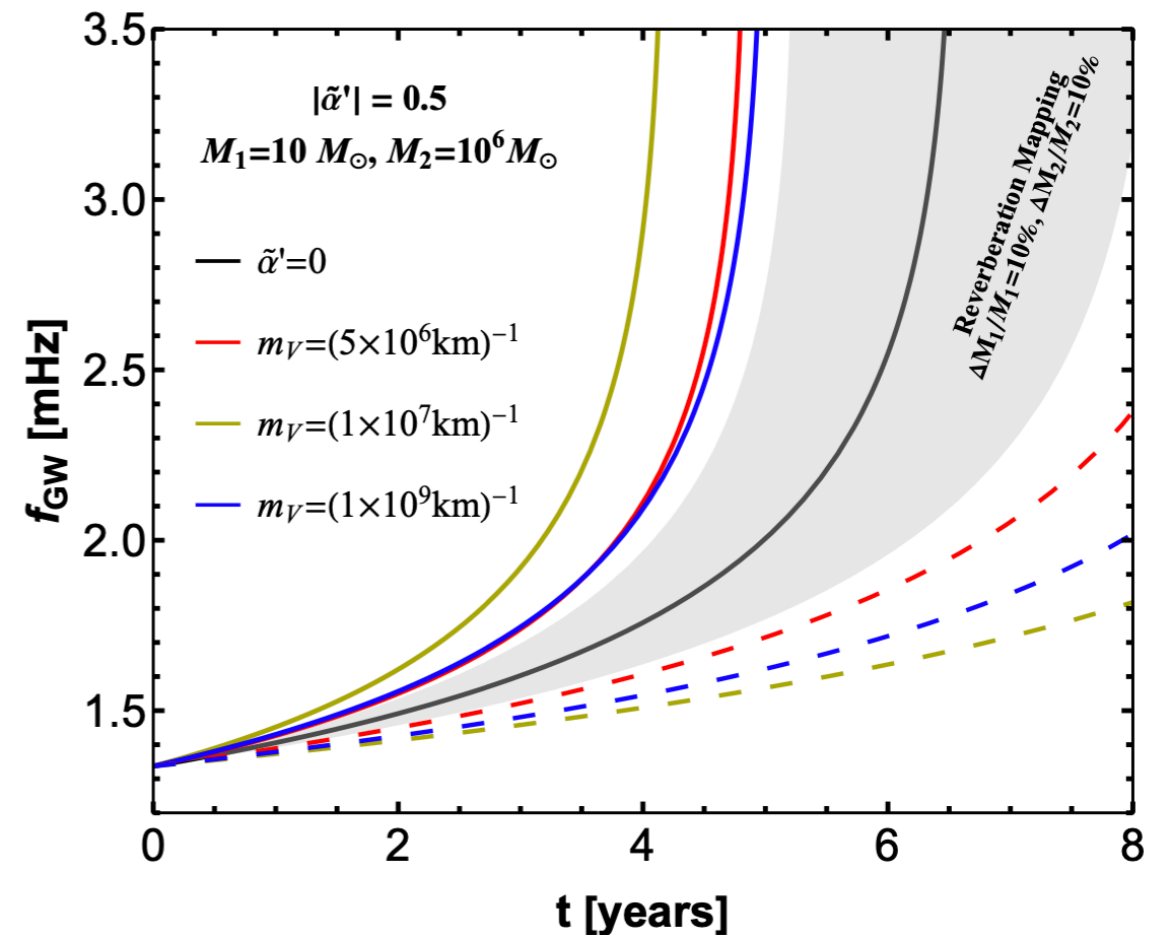
$$\frac{d\omega}{dt} = -\frac{32}{5} G \mu \omega^5 r^2 g \mathcal{N}^{-1}.$$

$$g = -\frac{3 + \tilde{\alpha}' e^{-m_V r} (3 + m_V r (3 + m_V r))}{1 + \tilde{\alpha}' e^{-m_V r} (1 + m_V r (1 - m_V r))}$$

Multimessenger studies needed since rescaling the binary component masses can mimic the dark force

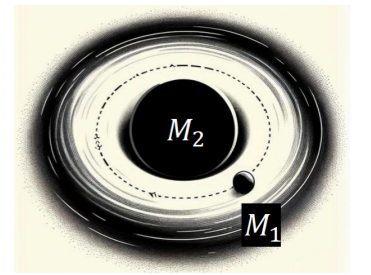
$$F_{\text{TOTAL}} = \frac{GM_1' M_2'}{r^2}$$

Reverberation mapping, dynamical tracers





# EMRIs, Dark Forces

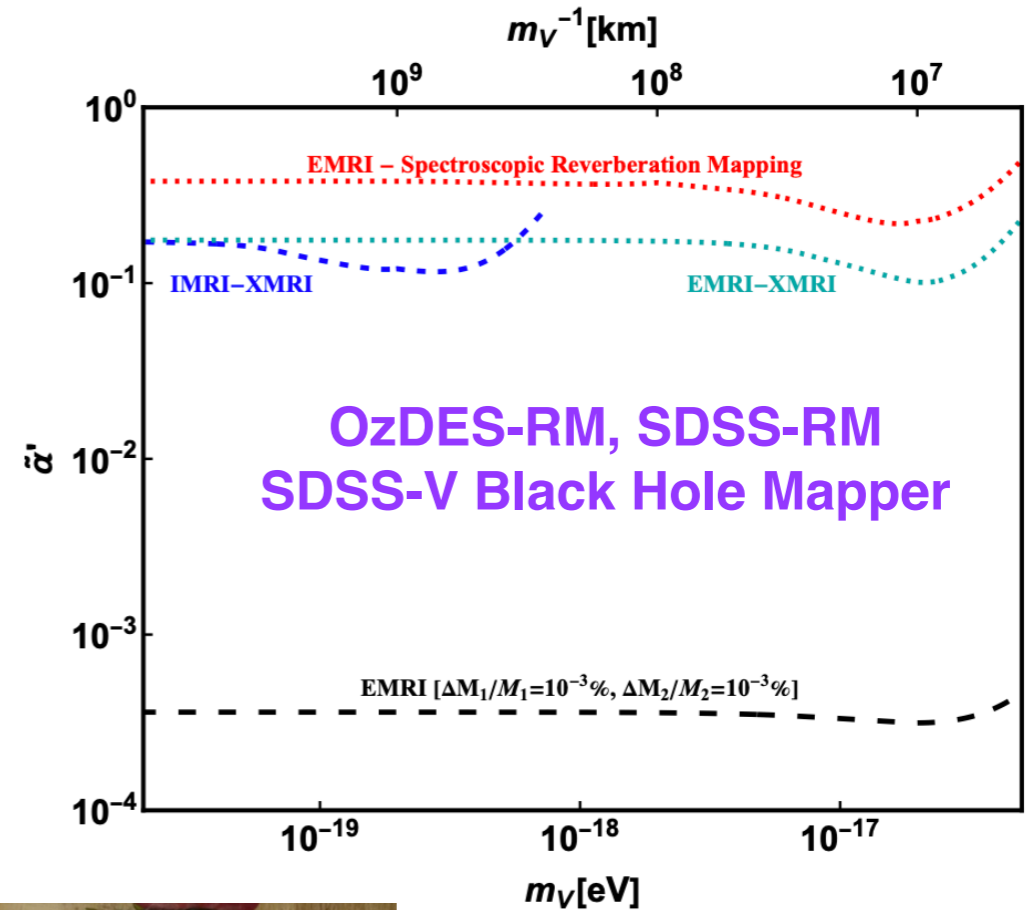
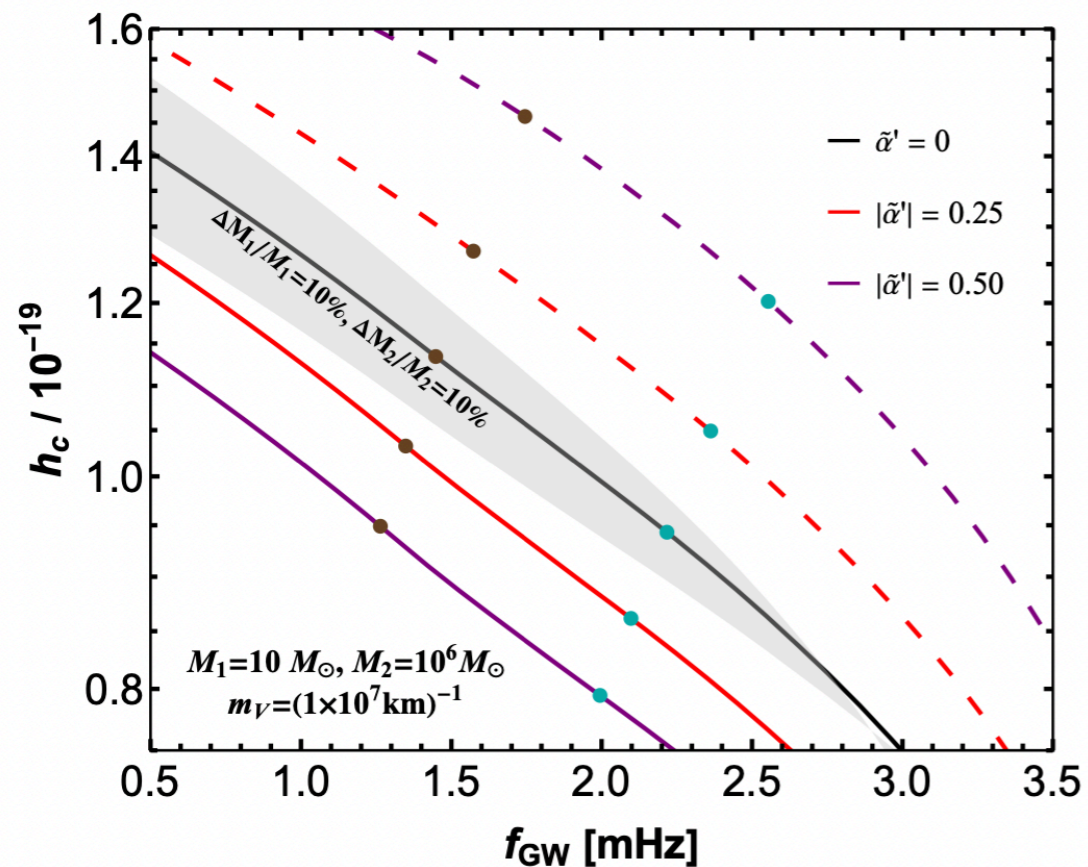


The rms amplitude of the GW emitted for the dominant  $m=2$  mode

$$h_{o,2} = \sqrt{\frac{32}{5}} \frac{\eta G M_2}{d_L} (G M_2 \omega)^{2/3} \mathcal{H}_{o,2}$$

$d_L$  is the luminosity distance from Earth

$$h_{c,m} \equiv h_{o,m} \sqrt{2f_{\text{GW},m}^2 / \dot{f}_{\text{GW},m}}$$



**Badal Bhalla**

# BSM at Source

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Source itself is due to BSM physics (phase transitions)

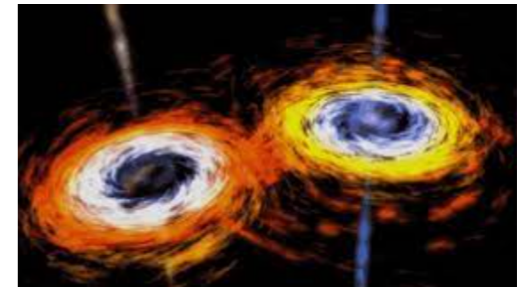
Source is astrophysical, BSM exchange deforms signal

Source is astrophysical, probes BSM in its environment

Source is astrophysical, serves as a clock (multimessenger)

# Binary Probes Environment

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A stellar black hole or neutron star will accumulate a dark matter spike around it

The spike distorts the GW waveform from binary inspiral: “dark dressed black holes”

**Kavanaugh, Bertone et.al. (2020 - )**

SMBH binaries exist at the centers of merging galaxies

*In a sense, you can think of NANOGrav is an instrument for probing galactic centers*

SMBH binaries inspire an “existence problem”: why do they exist and how did they get so close?

The seed problem (exacerbated by JWST) and the final parsec problem

Can you speed up accretion? How about bigger seeds? PBH seeds don't work...

Final parsec: dynamical friction increased by SIDM? BEC 3-body encounters?

**Bromley, Sandick, Shams Es Haghi (2023)**

**Alvarez, Cline, Dewar (2024)**



# BSM at Source

---



Source itself is due to BSM physics (phase transitions)

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# Neutron Star Mergers

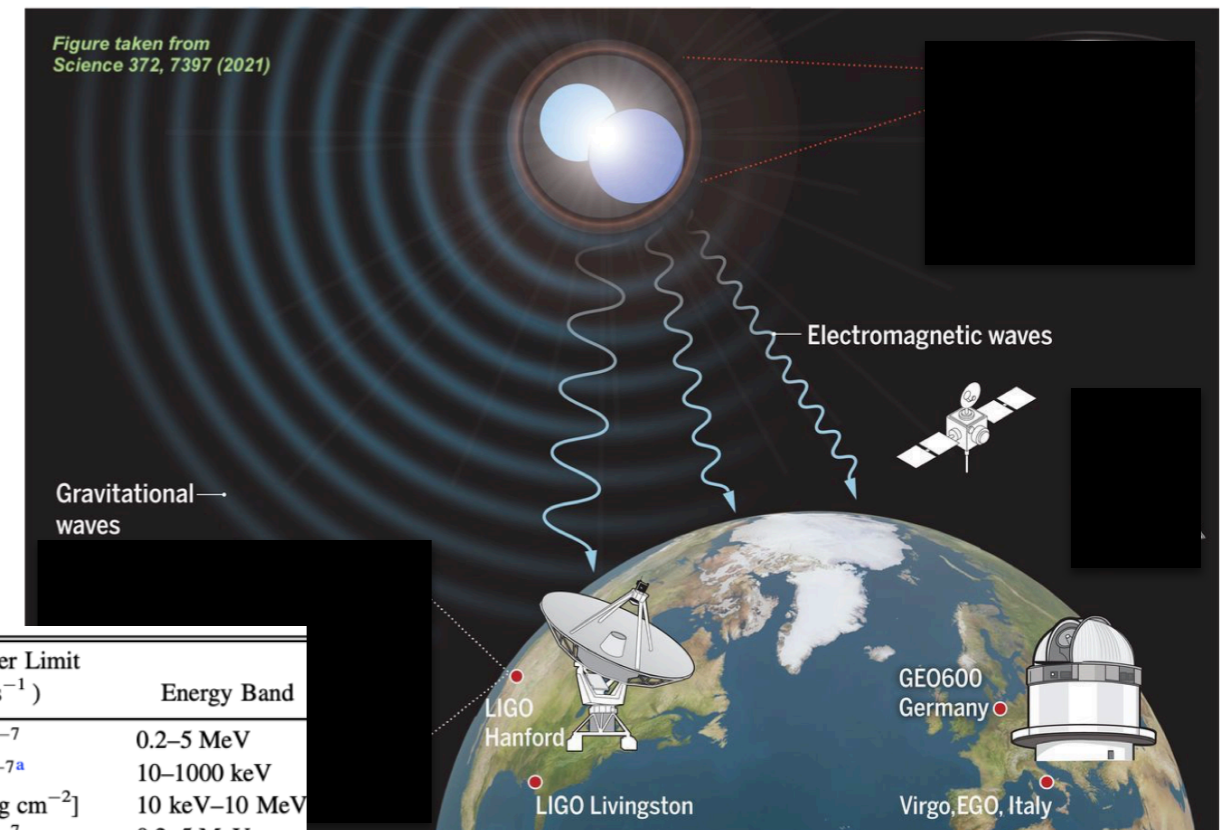


GW signal sets an alarm clock  $t=0$

If your BSM signal has time dependence from moment of emission (eg due to decay lifetime), use multiessenger studies

The energy of your emission dictates facility you want to use

## Multi-messenger Observation of Binary Neutron Star Merger GW170817



Observatory	UT Date	Time since GW Trigger	90% Flux Upper Limit ( $\text{erg cm}^{-2} \text{s}^{-1}$ )	Energy Band
<i>Insight</i> -HXMT/HE	Aug 17 12:34:24 UTC	-400 s	$3.7 \times 10^{-7}$	0.2–5 MeV
CALET CGBM	Aug 17 12:41:04 UTC	0.0	$1.3 \times 10^{-7a}$	10–1000 keV
Konus-Wind	Aug 17 12:41:04.446 UTC	0.0	$3.0 \times 10^{-7}$ [ $\text{erg cm}^{-2}$ ]	10 keV–10 MeV
<i>Insight</i> -HXMT/HE	Aug 17 12:41:04.446 UTC	0.0	$3.7 \times 10^{-7}$	0.2–5 MeV
<i>Insight</i> -HXMT/HE	Aug 17 12:41:06.30 UTC	1.85 s	$6.6 \times 10^{-7}$	0.2–5 MeV
<i>Insight</i> -HXMT/HE	Aug 17 12:46:04 UTC	300 s	$1.5 \times 10^{-7}$	0.2–5 MeV
AGILE-GRID	Aug 17 12:56:41 UTC	0.011 days	$3.9 \times 10^{-9}$	0.03–3 GeV
<i>Fermi</i> -LAT	Aug 17 13:00:14 UTC	0.013 days	$4.0 \times 10^{-10}$	0.1–1 GeV
H.E.S.S.	Aug 17 17:59 UTC	0.22 days	$3.9 \times 10^{-12}$	0.28–2.31 TeV
HAWC	Aug 17 20:53:14–Aug 17 22:55:00 UTC	0.342 days + 0.425 days	$1.7 \times 10^{-10}$	4–100 TeV
<i>Fermi</i> -GBM	Aug 16 12:41:06–Aug 18 12:41:06 UTC	$\pm 1.0$ days	$(8.0\text{--}9.9) \times 10^{-10}$	20–100 keV
NTEGRAL IBIS/ISGRI	Aug 18 12:45:10–Aug 23 03:22:34 UTC	1–5.7 days	$2.0 \times 10^{-11}$	20–80 keV
INTEGRAL IBIS/ISGRI	Aug 18 12:45:10–Aug 23 03:22:34 UTC	1–5.7 days	$3.6 \times 10^{-11}$	80–300 keV
INTEGRAL IBIS/PICsIT	Aug 18 12:45:10–Aug 23 03:22:34 UTC	1–5.7 days	$0.9 \times 10^{-10}$	468–572 keV
INTEGRAL IBIS/PICsIT	Aug 18 12:45:10–Aug 23 03:22:34 UTC	1–5.7 days	$4.4 \times 10^{-10}$	572–1196 keV
INTEGRAL SPI	Aug 18 12:45:10–Aug 23 03:22:34 UTC	1–5.7 days	$2.4 \times 10^{-10}$	300–500 keV
INTEGRAL SPI	Aug 18 12:45:10–Aug 23 03:22:34 UTC	1–5.7 days	$7.0 \times 10^{-10}$	500–1000 keV
INTEGRAL SPI	Aug 18 12:45:10–Aug 23 03:22:34 UTC	1–5.7 days	$1.5 \times 10^{-9}$	1000–2000 keV
INTEGRAL SPI	Aug 18 12:45:10–Aug 23 03:22:34 UTC	1–5.7 days	$2.9 \times 10^{-9}$	2000–4000 keV
H.E.S.S.	Aug 18 17:55 UTC	1.22 days	$3.3 \times 10^{-12}$	0.27–3.27 TeV
H.E.S.S.	Aug 19 17:56 UTC	2.22 days	$1.0 \times 10^{-12}$	0.31–2.88 TeV
H.E.S.S.	Aug 21 + Aug 22 18:15 UTC	4.23 days + 5.23 days	$2.9 \times 10^{-12}$	0.50–5.96 TeV

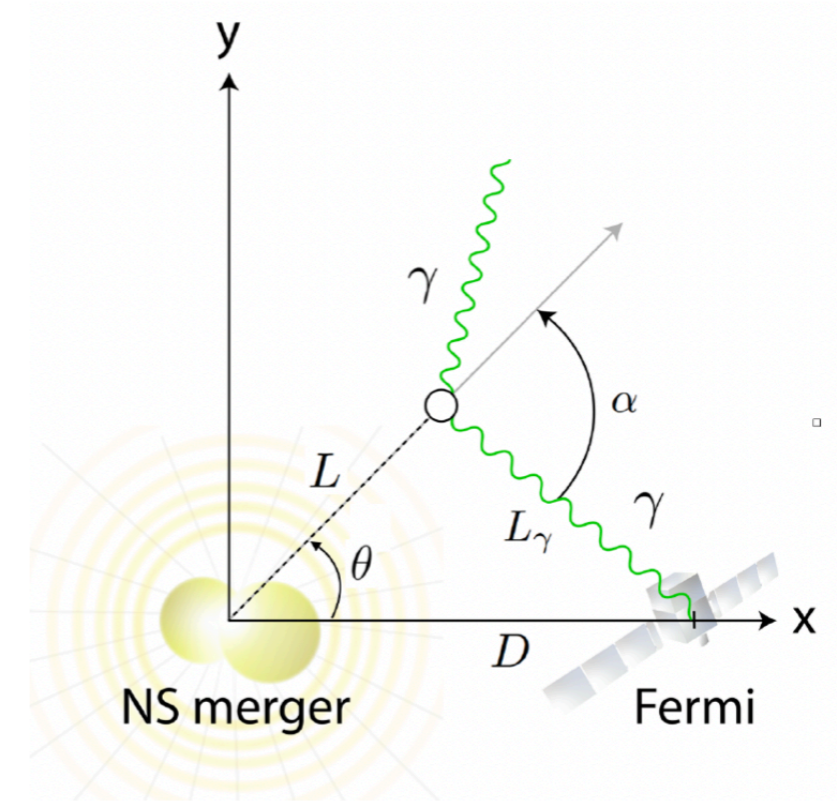
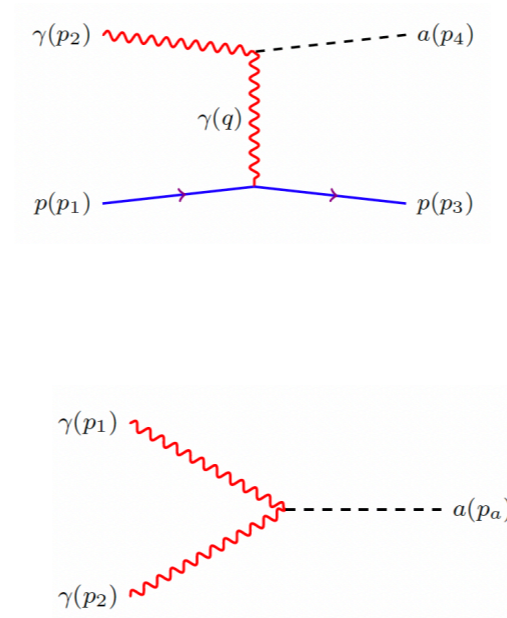
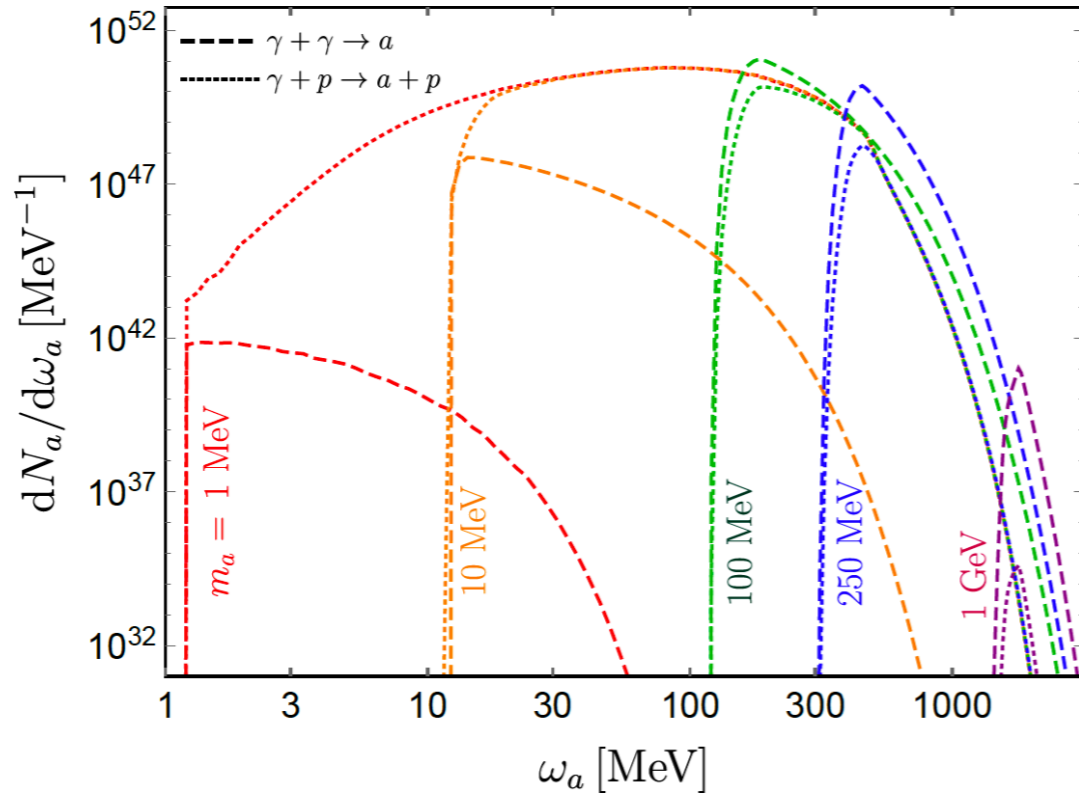
Target: axions

Alford, Fortin, Harris, **KS** (JCAP 07, 2020)

Dev, Fortin, Harris, **KS**, Zhang (JCAP 01, 2022)

Dev, Fortin, Harris, **KS**, Zhang (PRL 132, 2024)

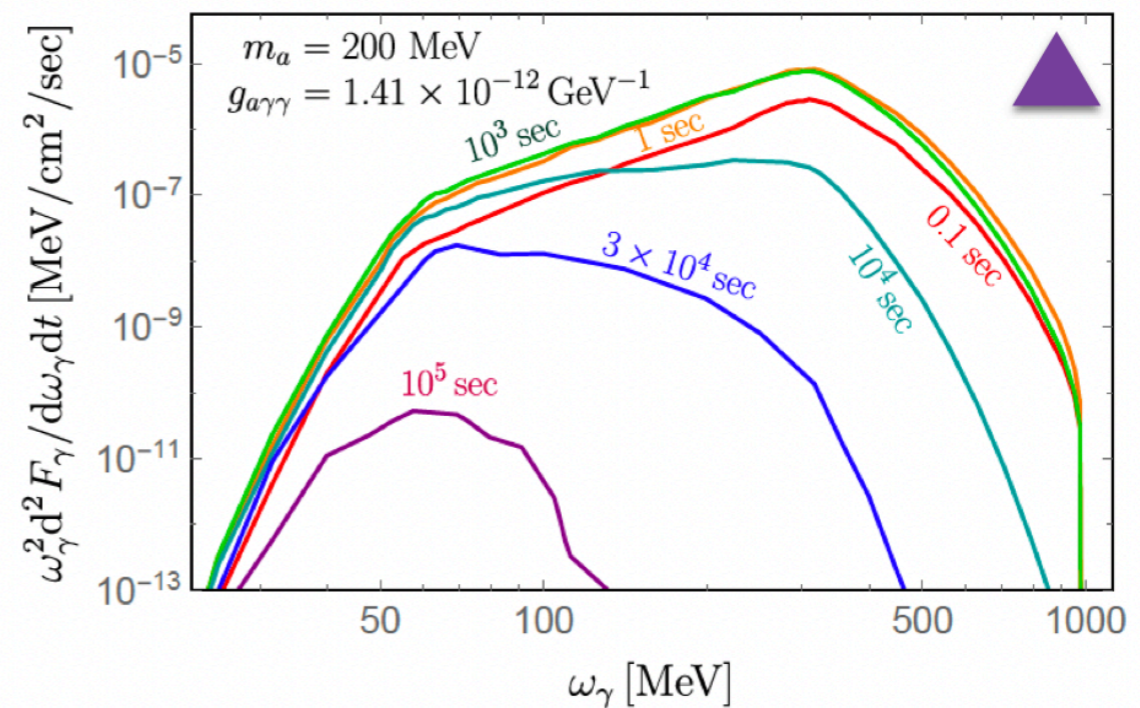
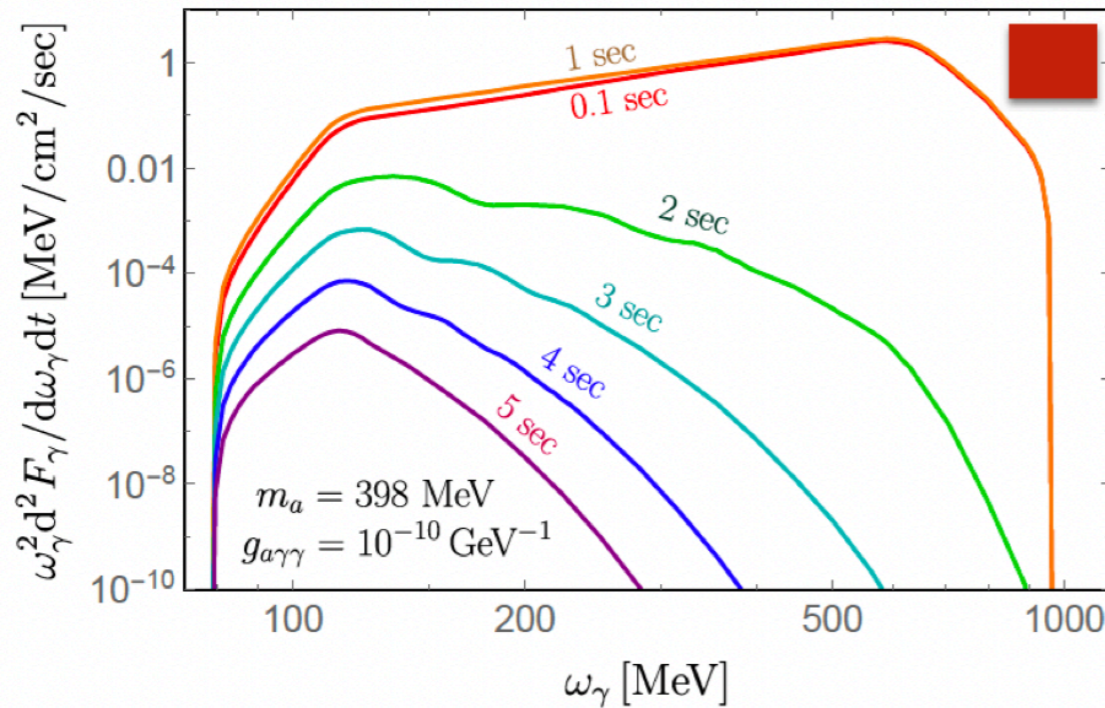
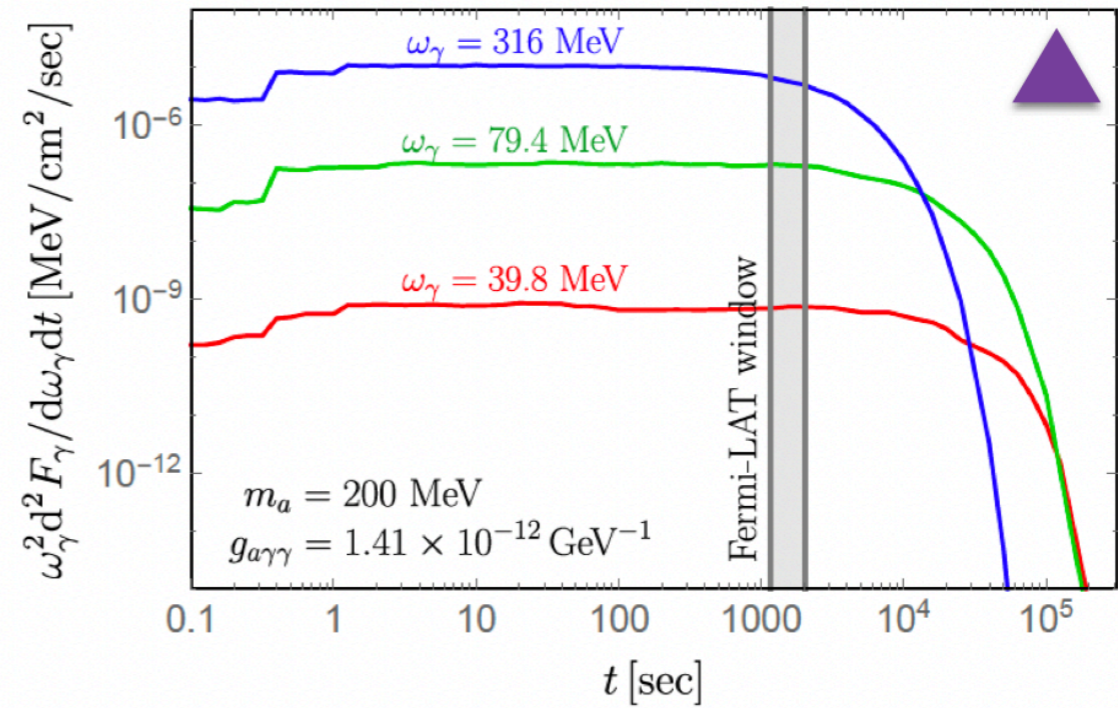
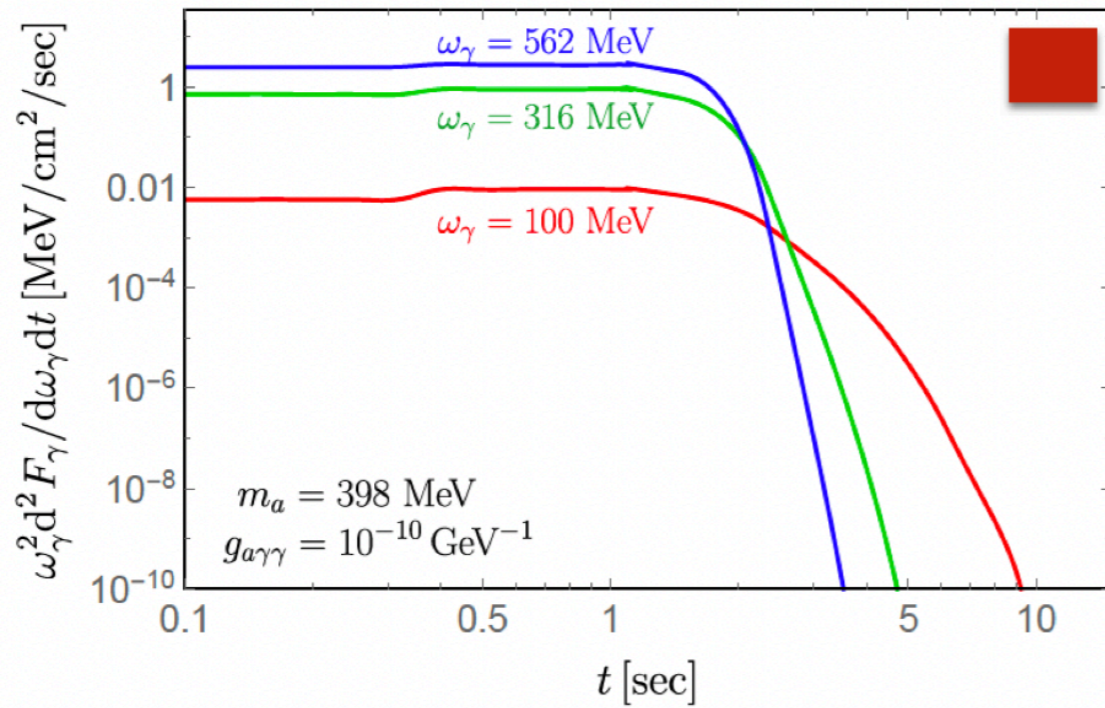
# Neutron Star Mergers



$$\omega_\gamma^2 \frac{d^2 F_\gamma}{d\omega_\gamma dt}(\omega_\gamma, D+t) = \int_{-1}^1 dz \int_0^\infty dL \frac{\omega_\gamma^2}{4\pi D(L_\gamma + Lz)} \frac{d^2 N_a}{d\omega_a dt}(\omega_a, D+t - L/\beta_a - L_\gamma) \text{Jac}(\omega_a, \omega_\gamma) \\ \times \frac{m_a^2}{\omega_a^2 (1 - \beta_a z)^2} \frac{\exp(-L/\ell_a)}{\ell_a} \Theta(L - R_\star) \Theta(L - D/\sqrt{1 - z^2}).$$



# Neutron Star Mergers

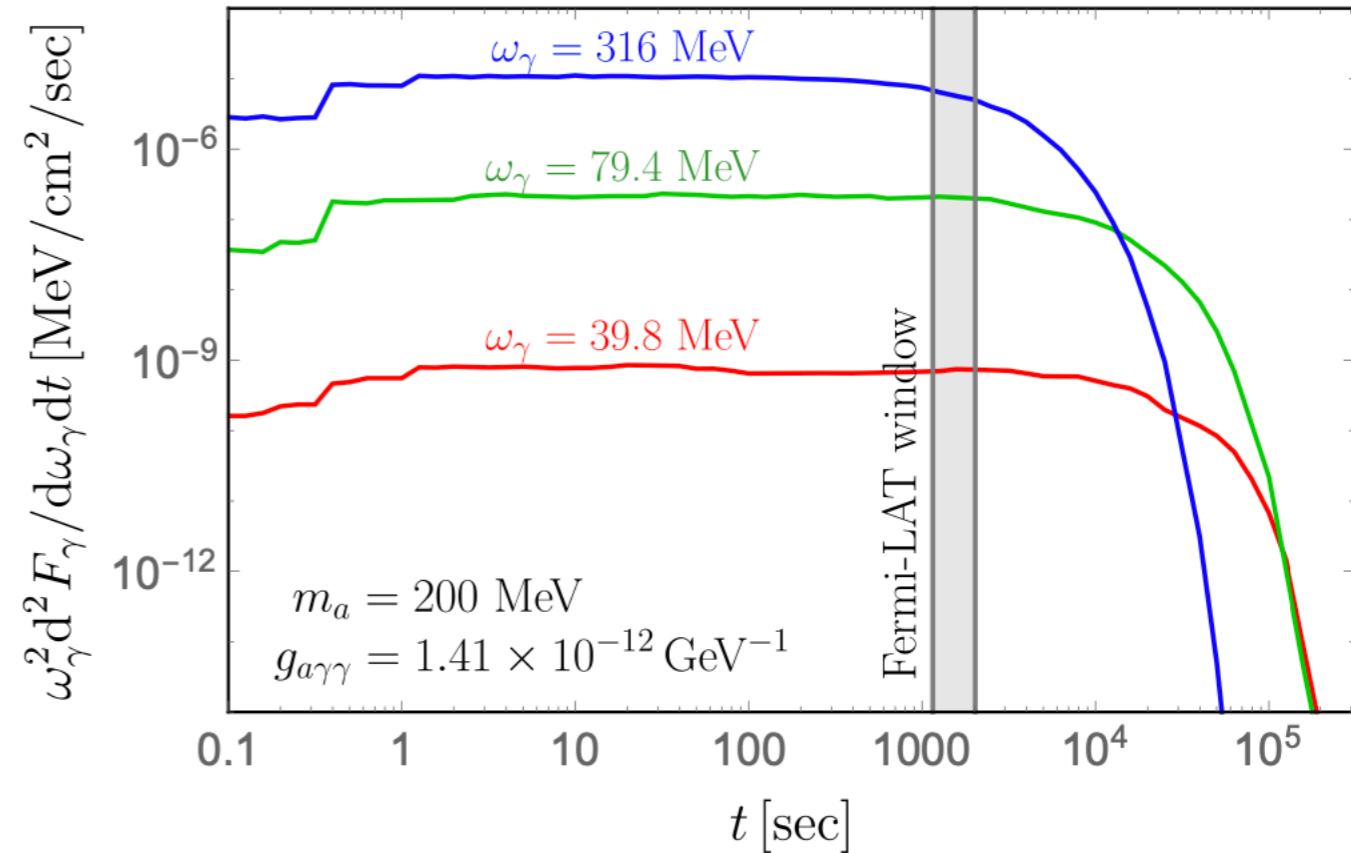
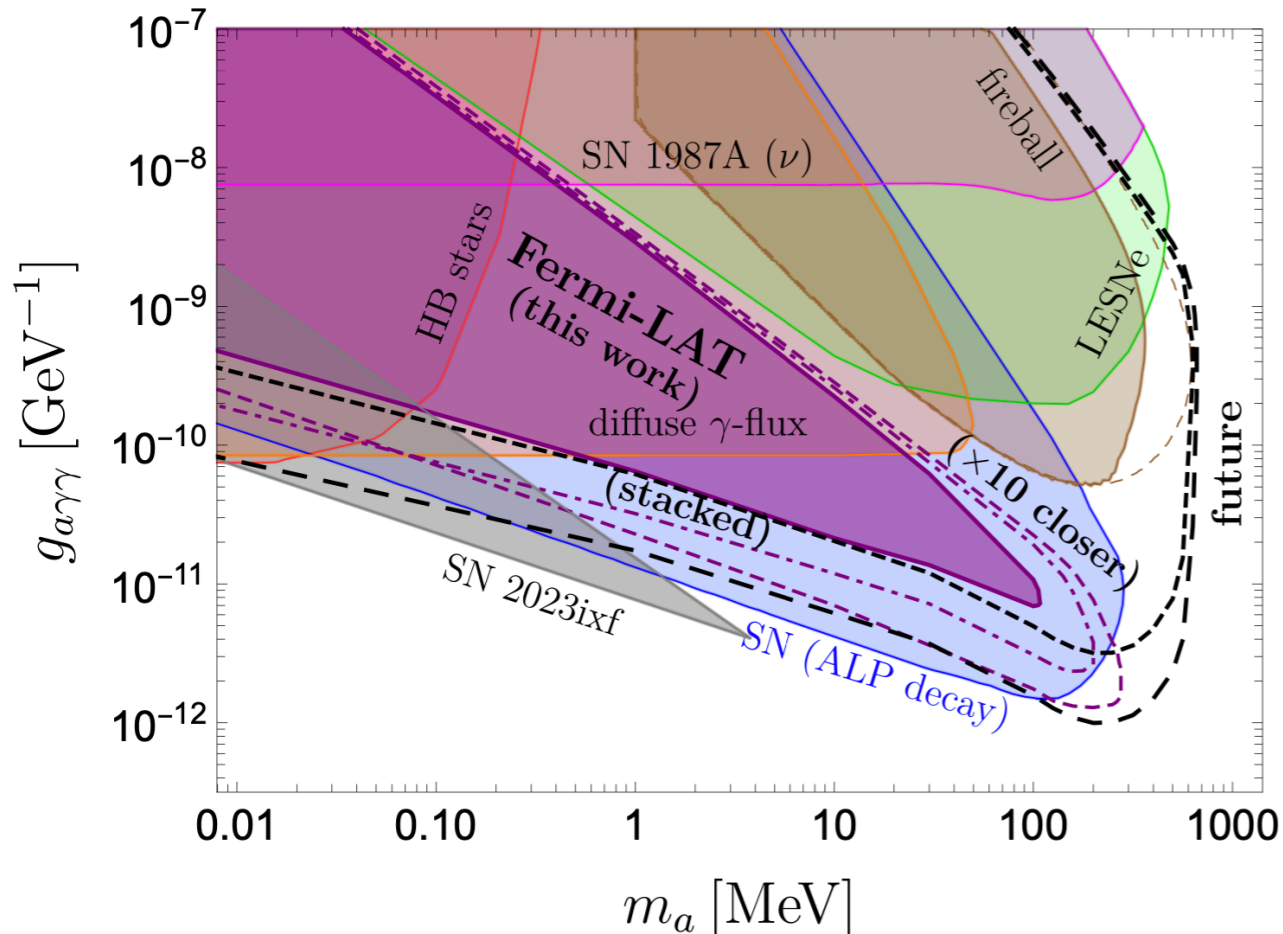
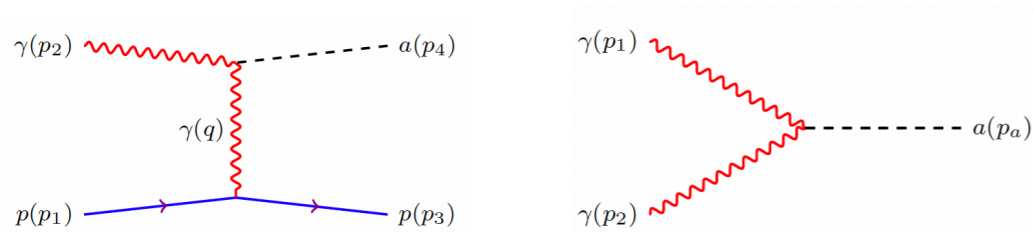


# Neutron Star Mergers



Multimessenger is key

Localization of source is important



you're looking at a baby magnetar

generally, you want to look at near-Earth, hot, young magnetars if you want to constrain axions

Fortin, Harris, **KS**, + various (2017-2024)

Gau, Hajkarim, Fortin, Harris, **KS** (JCAP 07, 2020)

Diamond, Marques-Tavares (2024)



# White Dwarf Mergers



- Total white dwarf binaries in Milky Way:  $\sim 5 \times 10^8$
- Total with  $f_{\text{GW}} > 10^{-4}$  Hz:  $\sim 6 \times 10^7$
- Total individually resolvable:  $\sim 10^3 - 10^4$

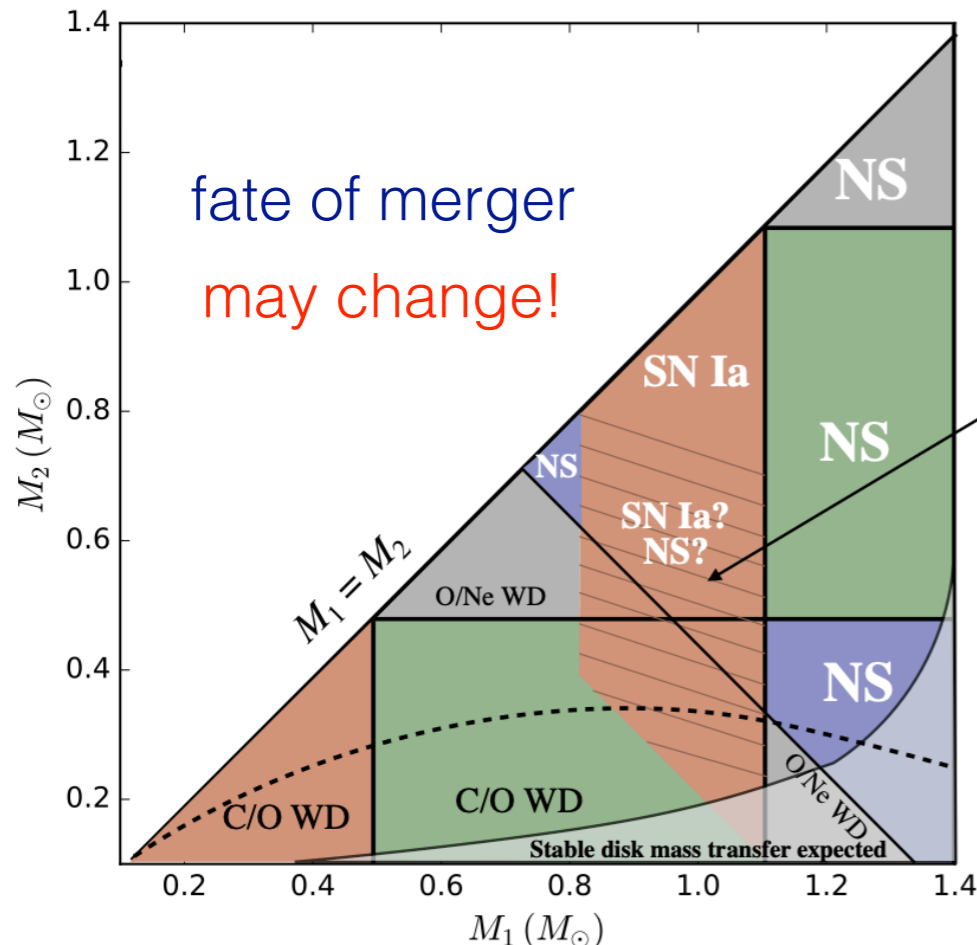
e.g., Nelemans+2001, Ruiter+2010, Nissanke+2012, Lamberts+2019, Breivik+2020



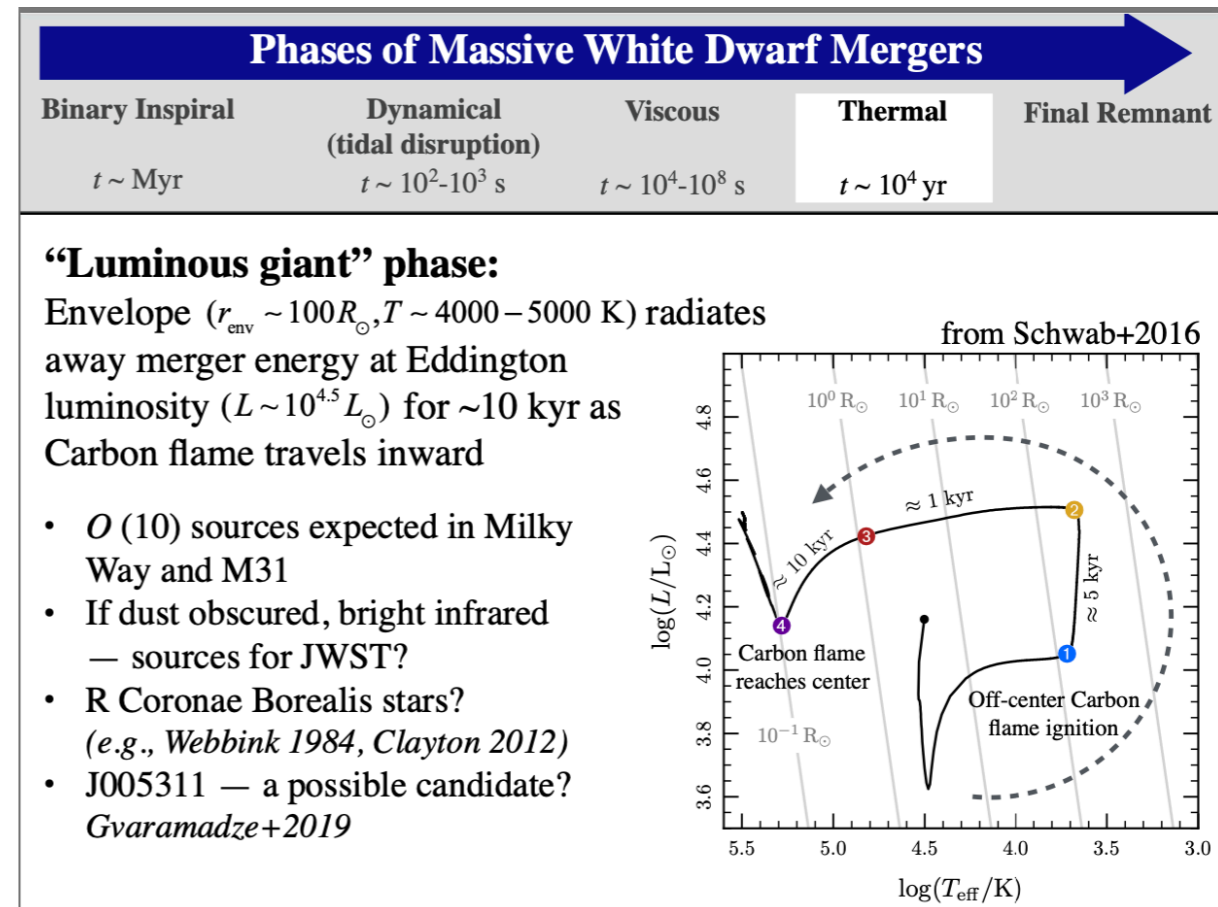
TJ Gehrman -  
the stellar physics guru

Dev, Fortin, Harris, **KS**, Walsh, Zhang (in progress)

Gehrman, Sandick, **KS**, Walsh, Xu (in progress)



Shen et. al. (2015)



Kremer et. al. (2023)

# White Dwarf Mergers



GW signal sets an alarm clock  $t=0$

look for *disappearance*

We discuss the prospect of identifying a white dwarf binary merger by monitoring disappearance of its nearly monochromatic gravitational wave. For a ten-year operation of the laser interferometer space antenna (LISA), the chance probability of observing such an event is roughly estimated to be 20%. By simply using short-term coherent signal integrations, we might determine the merger time with an accuracy of  $\sim 3$ -10 days. Also considering its expected sky localizability  $\sim 0.1$ -0.01deg<sup>2</sup>, LISA might make an interesting contribution to the multi-messenger study on a merger event.

Seto (2024)

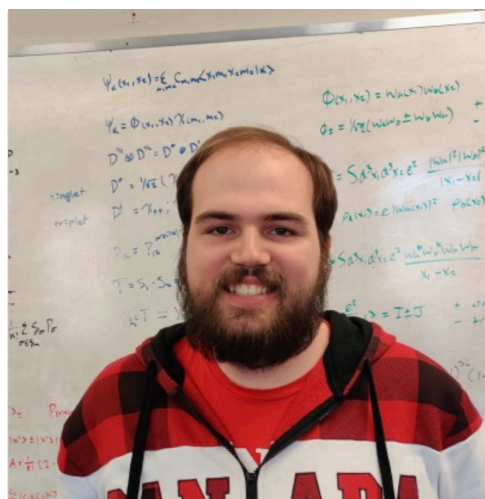
you're looking at a baby white dwarf!

or a baby super-Chandrasekhar mass star!

$$\frac{L_a}{L} \sim 1.6 \times 10^{-4} \left( \frac{g_{aee}}{10^{-13}} \right)^2 \left( \frac{M_{WD}}{1M} \right) \left( \frac{T_c}{10^7 K} \right)^4$$

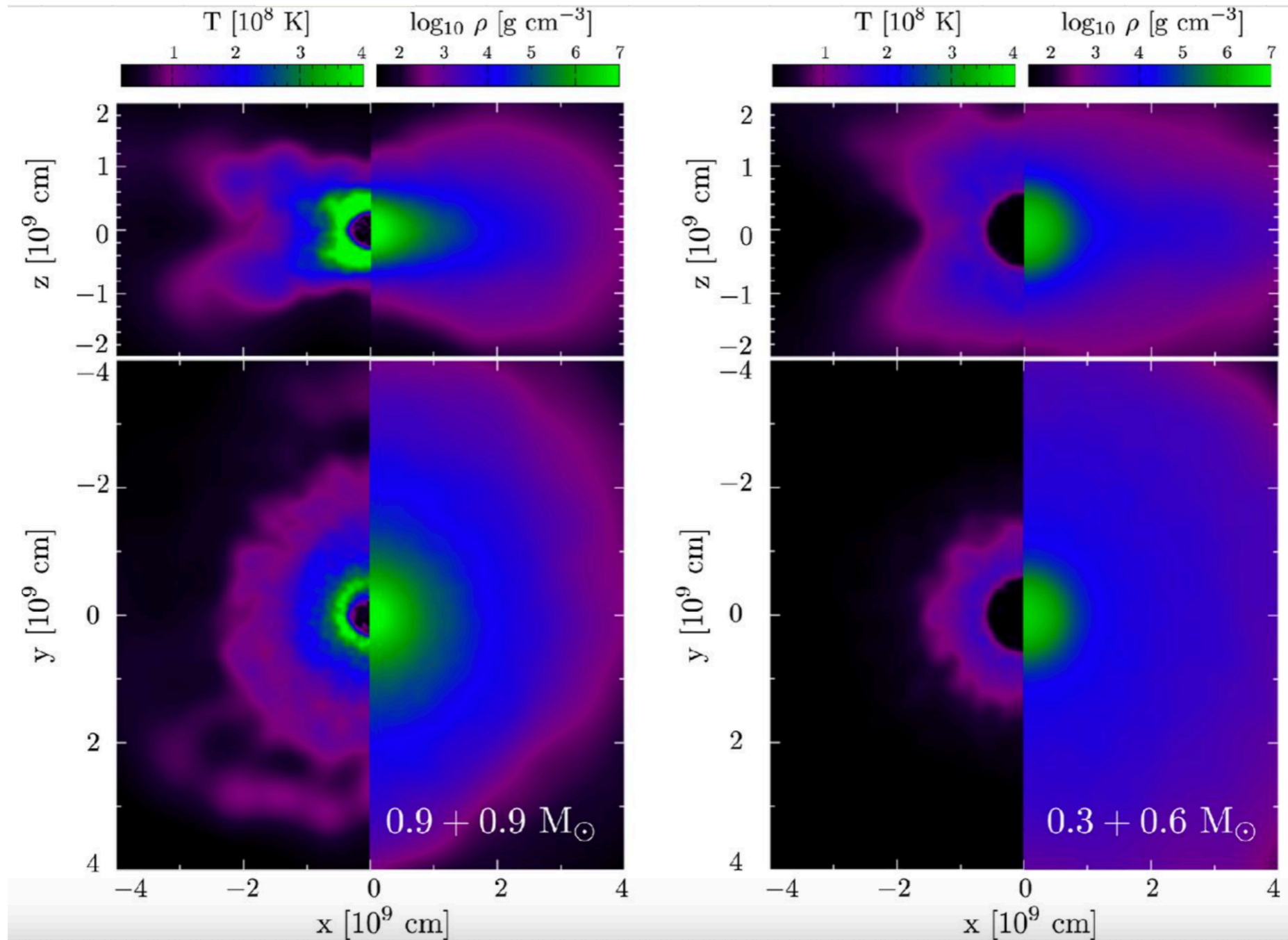
Gehrman, Sandick, **KS**, Walsh, Xu (in progress)

Dev, Fortin, Harris, **KS**, Walsh, Zhang (in progress)



Teddy Walsh

# White Dwarf Mergers





*BSM on the way*

# BSM on the way

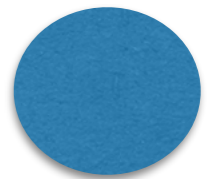
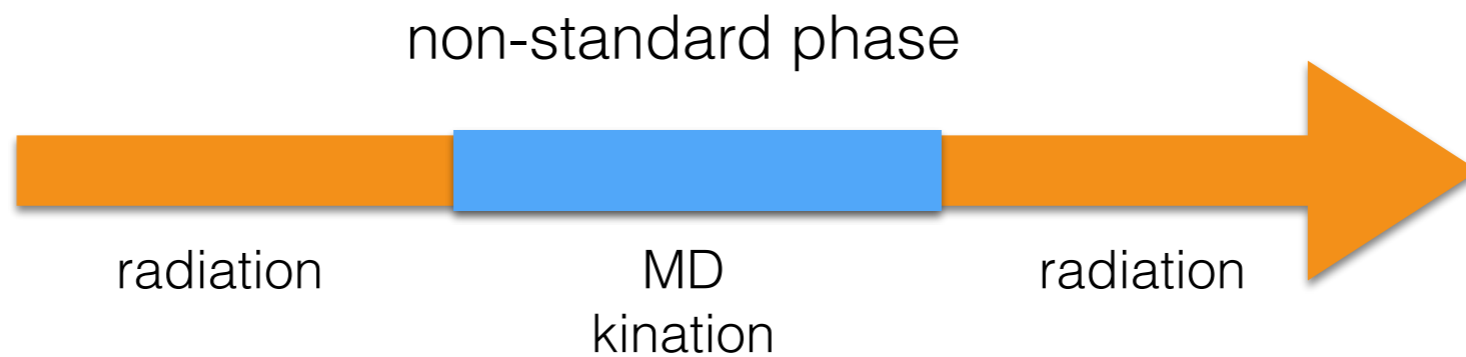
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Source is BSM, deformation due to new cosmology

Source is astrophysical, deformation due to new stuff

# Gameplan

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Insert favorite early Universe

BSM source:

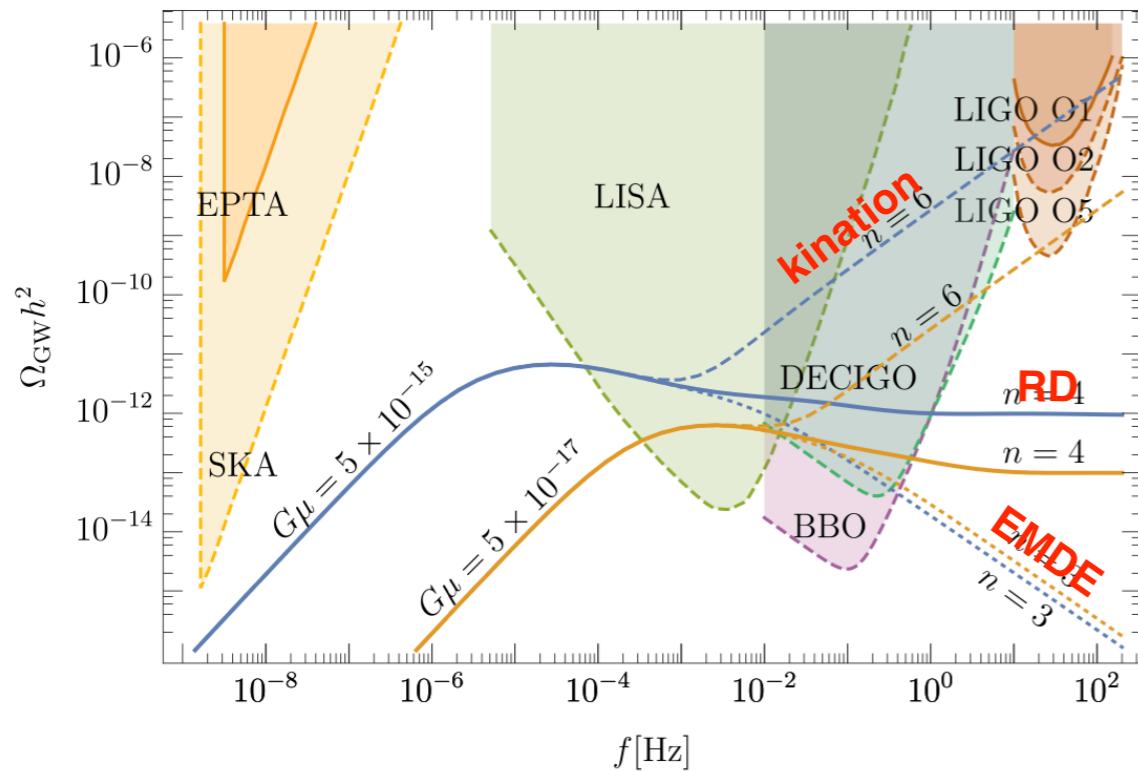
cosmic strings  
phase transitions  
2nd order GWs

cosmological distance

deformed GW  
waveform

# Study Non-Standard Histories

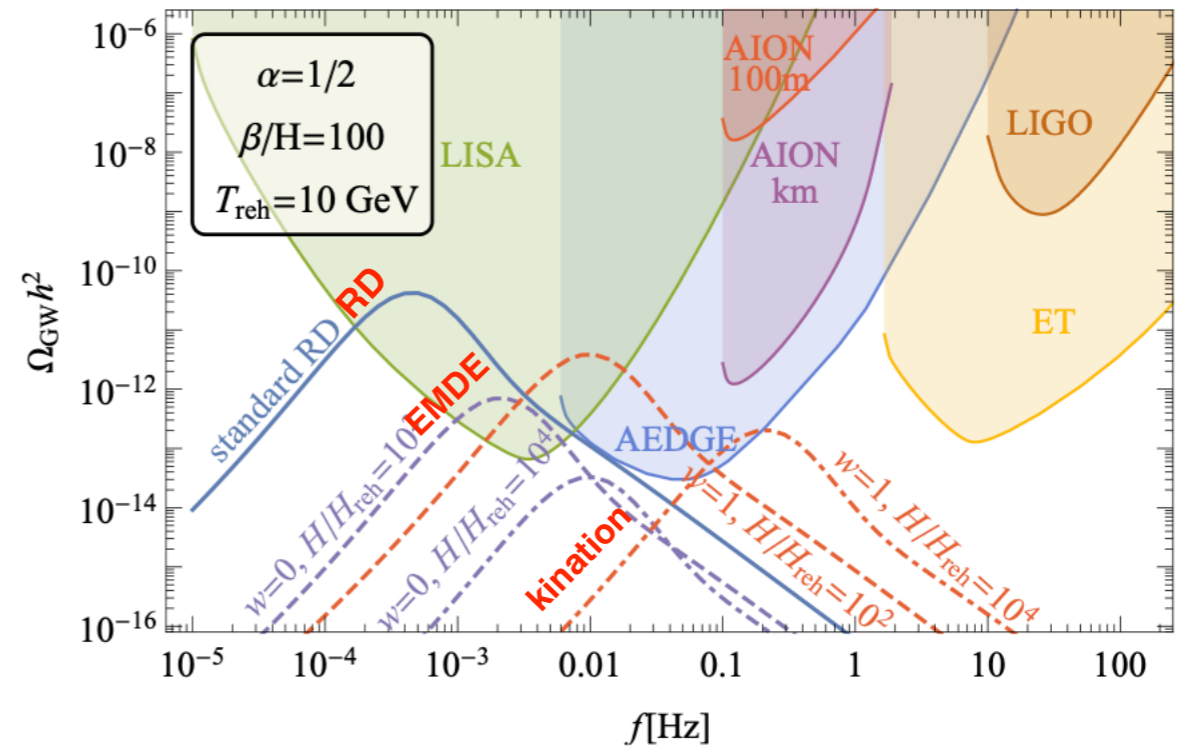
example: source = cosmic strings



**Cui, Lewicki, Morrissey, Wells (2016)**

**Gouttenoire, Servant, Simakachorn (2020)**

example: source = phase transition



**Figuroa et. al. (2020)**

source = primordial GWs, induced GWs, etc.

**Bernal, Hajkarim (2018)**

**Domenec et. al. (2020)**

Personally, I only trust modifications of the causal  $k^3$  tail. It is universal

# BSM on the way

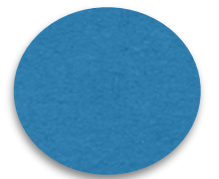
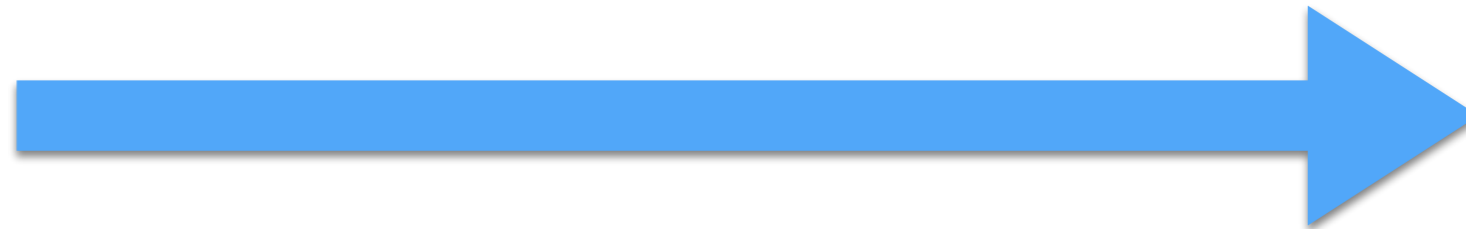
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Source is BSM, deformation due to new cosmology

Source is astrophysical, deformation due to new stuff

# Gameplan

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massive graviton  
modified GR  
extra dimensions

dark matter

Insert favorite late Universe  
astrophysical source:

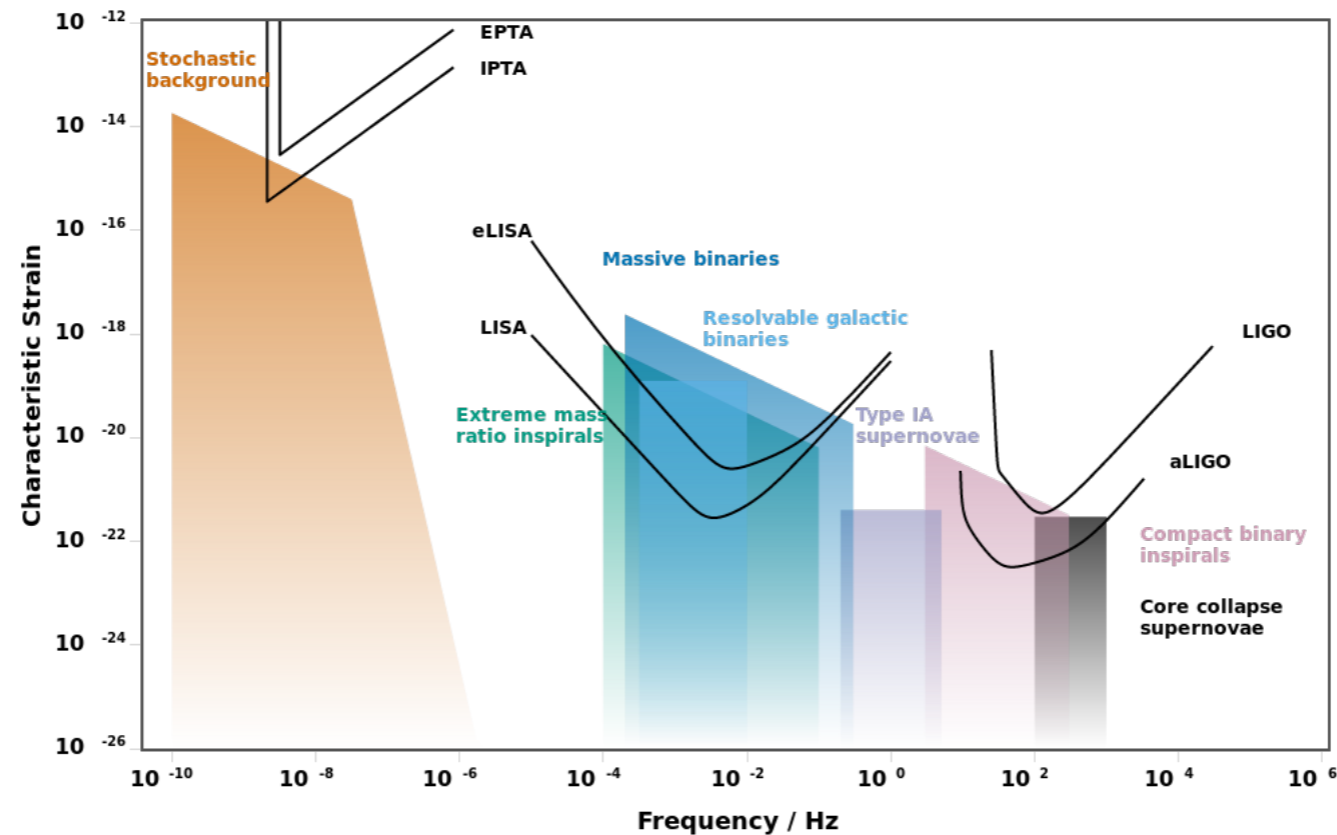
NS merger  
BH merger  
EMRI

deformed GW  
waveform

**Check out Tao Xu's talk**

# Invitation

Low f GW



High f GW

N. Aggarwal et. al. (2020)

V. Domcke et. al. (2020-)



Secular drift of pulsars?

DeRocco, Dror (2023)

SMBH inspirals

PBH + baryogenesis + dark matter

TJ Gehrman, Shams, **KS**, Xu (*JCAP* 03 2024)

TJ Gehrman, Shams, **KS**, Xu (*JCAP* 02 2023)

TJ Gehrman, Shams, **KS**, Xu (*JCAP* 10 2023)

Reheating

Easter, Giblin, Lim (2006)