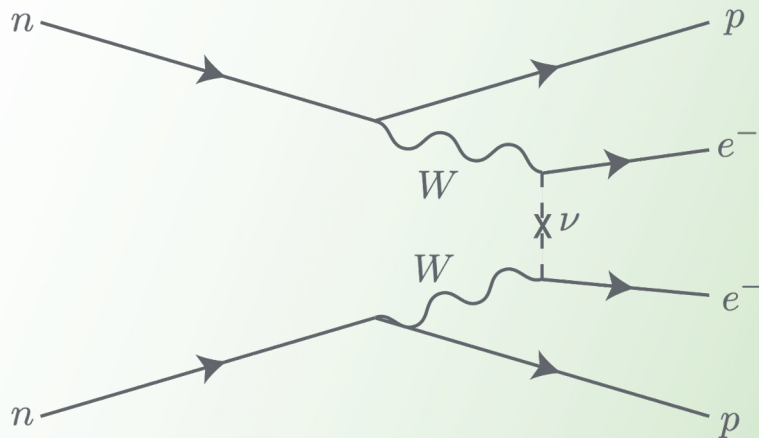
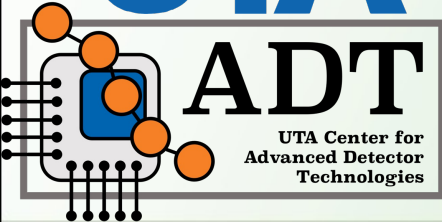


# Overview of Neutrinoless Double Beta Decay

Krishan Mistry



**UTA**



May 15 2024

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# How did the Universe come to be?

- Standard Model is our best theory but it has some shortfalls
- Neutrinos are one of the least understood particles in the SM and may give some clues

Neutrino mass mechanism  
Antimatter-matter asymmetry  
Dark Matter/Energy

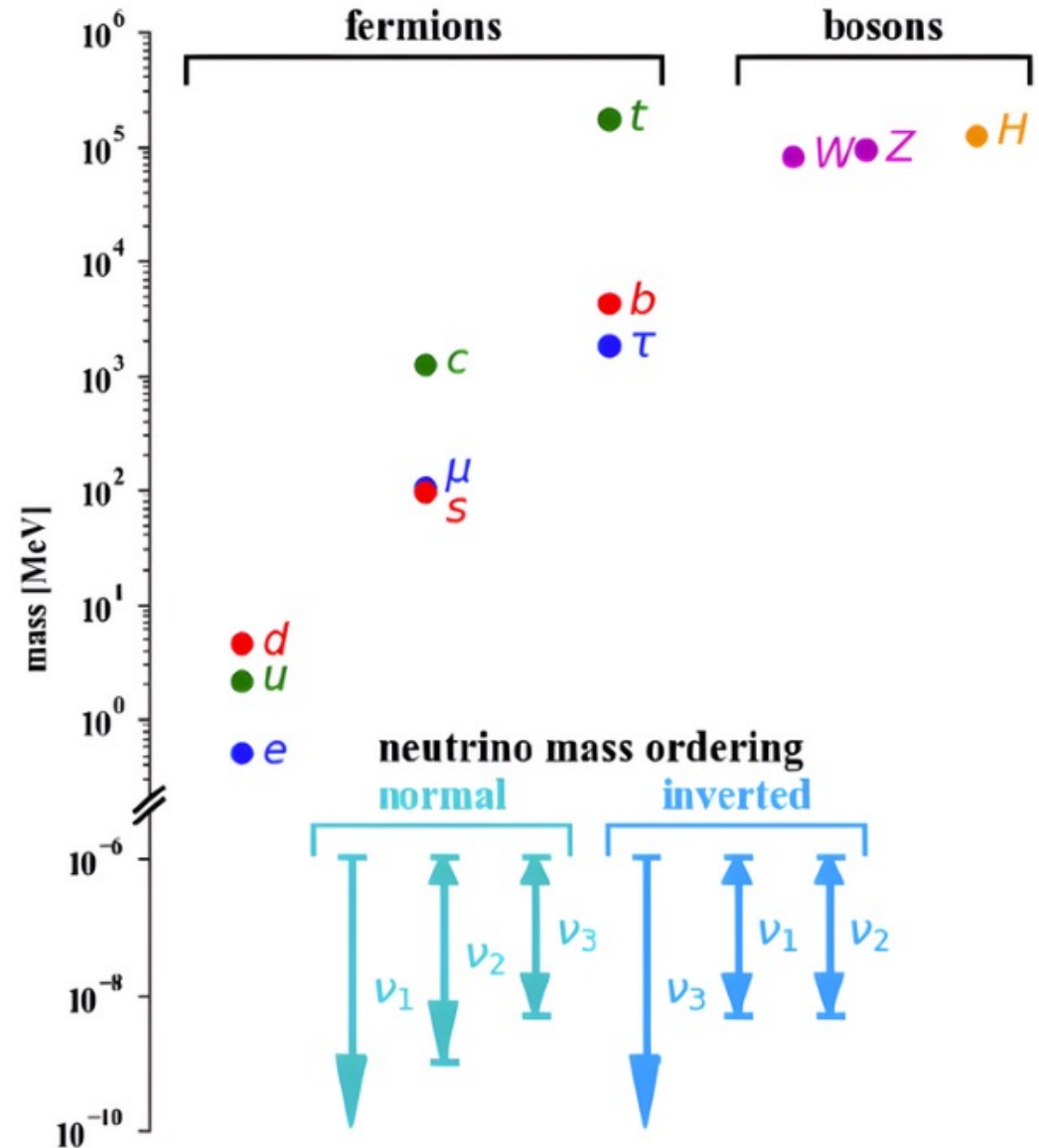


Grand Unified Theory

Quantum Gravity

# $\nu$ 's have mass and it's really small!

- Standard Model includes massless neutrinos
- Discovery of neutrino oscillations means they have mass
  - Significantly smaller scale to the regular fermions
- Fine-tuning of the SM, new mass mechanism, new physics?



# Adding a mass term

- If we include mass mechanism like the other fermions, we add a right-handed (but sterile) neutrino:

$$-L_D = m_D (\bar{\nu}_L \nu_R + \bar{\nu}_R \nu_L), \quad m_D = y v / \sqrt{2}$$

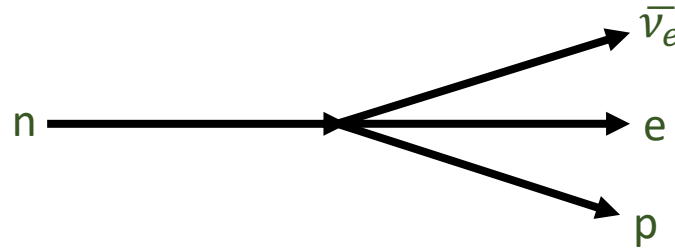
Yukawa coupling

Expectation value of Higgs  
after EW symmetry breaking

- Yukawa coupling constant has to be extremely small ( $\sim 10^{-12}$ )
  - Fine-tuning and seems unnatural
- Doesn't get us any closer to solving any of the big questions

# Rewind History: Fermi Beta Decay

- Fermi's theory of beta decay (1930s) was first developed assuming a point-like interaction between fermions



- We later found out that the mediator bosons were at much higher energy scale than the MeV scale energies probed
- Fermi's description was just a low-energy manifestation of the Standard Model
- Electroweak interactions at a higher physics scale

# SM is a low-energy effective field theory (EFT)

$$L = L_{SM} + \frac{1}{E_{new}} L_1 + \frac{1}{E_{new}^2} L_2 + \dots$$

The only dimension-5 operator we can add obeying SM gauge symmetry

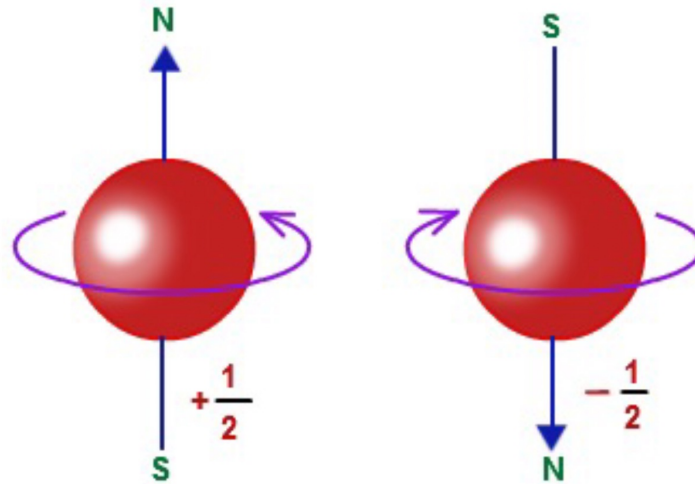
$$\frac{L_1}{E_{new}} = y_{ij} \frac{v^i H v^j H}{E_{new}}$$

Weinberg  
1979

- Term has one function: makes Majorana neutrinos with mass suppressed by new physics scale  $E_{new}$
- Also makes the theory non-renormalizable implying there must be something else at high scale too

# The Majorana Neutrino

- Ettore Majorana realized for neutral fermions you can impose the condition:  $\nu^c = \nu$ 
  - Neutrino is the only fermion that you can impose this condition



Behaves like matter

Behaves like antimatter

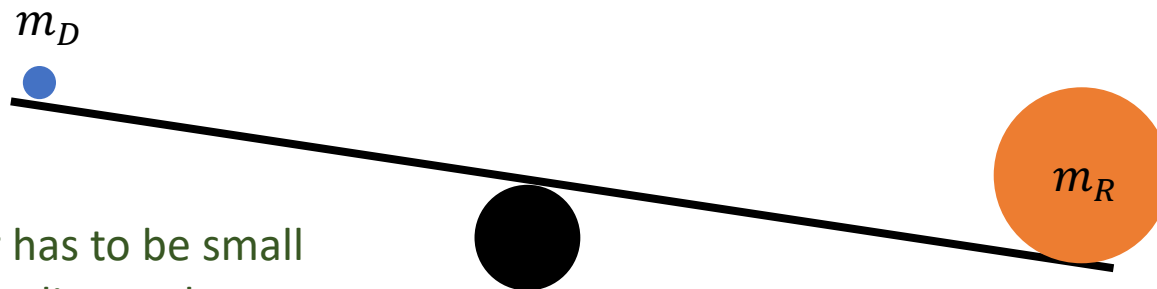
- A Majorana neutrino introduces processes that violate lepton number by two units

# Majorana mass generation mechanism (Seesaw Type I)

$$-L_{D+R} = m_D (\overline{\nu}_L \nu_R + \overline{\nu}_R \nu_L) + \frac{1}{2} m_R (\overline{\nu}_R (\nu_R)^c + \overline{(\nu_R)^c} \nu_R)$$

Dirac Mass term

Right-handed Majorana term



$m_D$  no longer has to be small  
 $\rightarrow$  Yukawa coupling no longer  
 has to be unnaturally small

$m_R \gg m_D$  as no longer  
 fixed to EW scale

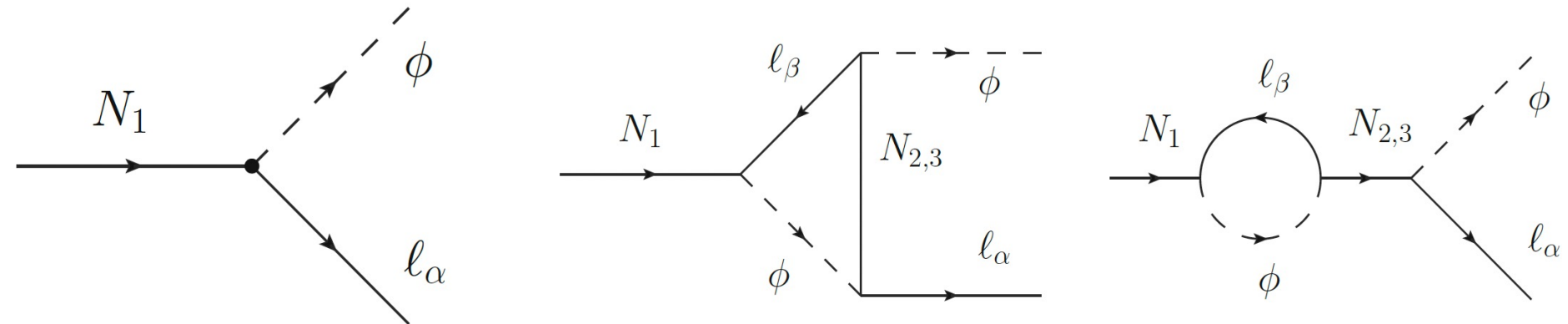
- Definite mass states of Dirac + right-handed Majorana mass results in a left-handed Majorana neutrino of mass  $m_D^2/m_R$   
 $\rightarrow$  We have a more natural way to explain the neutrino mass
- Integration of the heavy field out below the mass scale  $m_R$  returns the Weinberg operator



# Leptogenesis

Fukugita and Yanagida, Phys, Lett., B174:45,1986

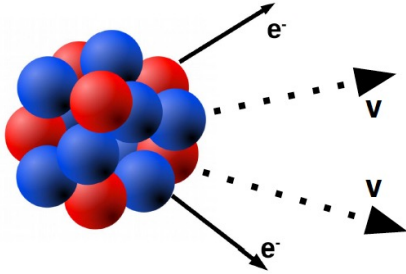
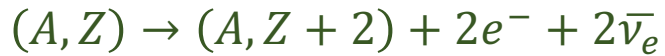
- Introduce a heavy Majorana neutrino (typically around GUT scale)
  - Decays to leptons+Higgs:  $l_\alpha \phi$  and  $\overline{l}_\alpha \overline{\phi}$
  - If rate of interaction is slower than universe expansion, we depart from thermal equilibrium
  - We can drive one decay process more than the other creating LNV
- Sphaleron process then generates the baryon asymmetry from LNV
- Sakharov conditions to explain antimatter-matter asymmetry: BNV, BSM CPV, thermal equilibrium



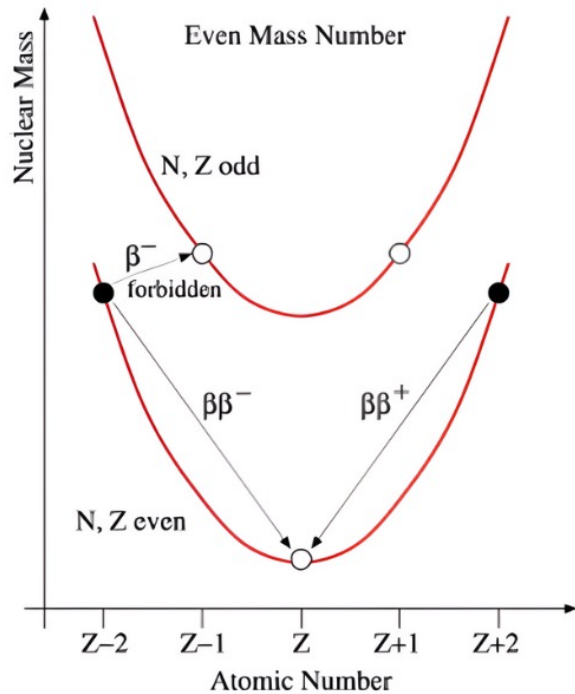
# In a nutshell, Majorana neutrinos:

1. Violate lepton number conservation
2. Neither matter or antimatter, but something else (Majorana fermion)
3. The SM with a Majorana term is non-renormalizable  
→ SM is definitely a low-energy effective field theory
4. There are other mass generation mechanisms beyond the Higgs
5. Majorana neutrinos are a prediction of Leptogenesis to explain the antimatter-matter asymmetry

# Double Beta decay ( $2\nu\beta\beta$ )



- A known (and measured) SM process
- Even-even nuclei are more stable due to the pairing-force



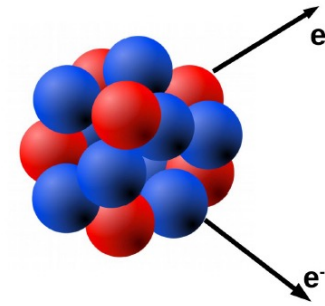
- Transition is mostly to ground state
  - Excited states are suppressed by phase-space
- Second order weak process
  - Half-lives  $\sim 10^{19}$ - $10^{21}$  yr

# Neutrinoless Double Beta decay ( $0\nu\beta\beta$ )

- Majorana neutrinos annihilate giving almost all the energy to the electrons

→ Cannot happen for Dirac neutrino

$$(A, Z) \rightarrow (A, Z + 2) + 2e^{-}$$



$$T_{1/2} = \left[ G \times |M(g_A)|^2 \times m_{\beta\beta}^2 / m_e^2 \right]^{-1}$$

Phase-space factor  
Atomic Physics

Matrix element  
Nuclear Physics

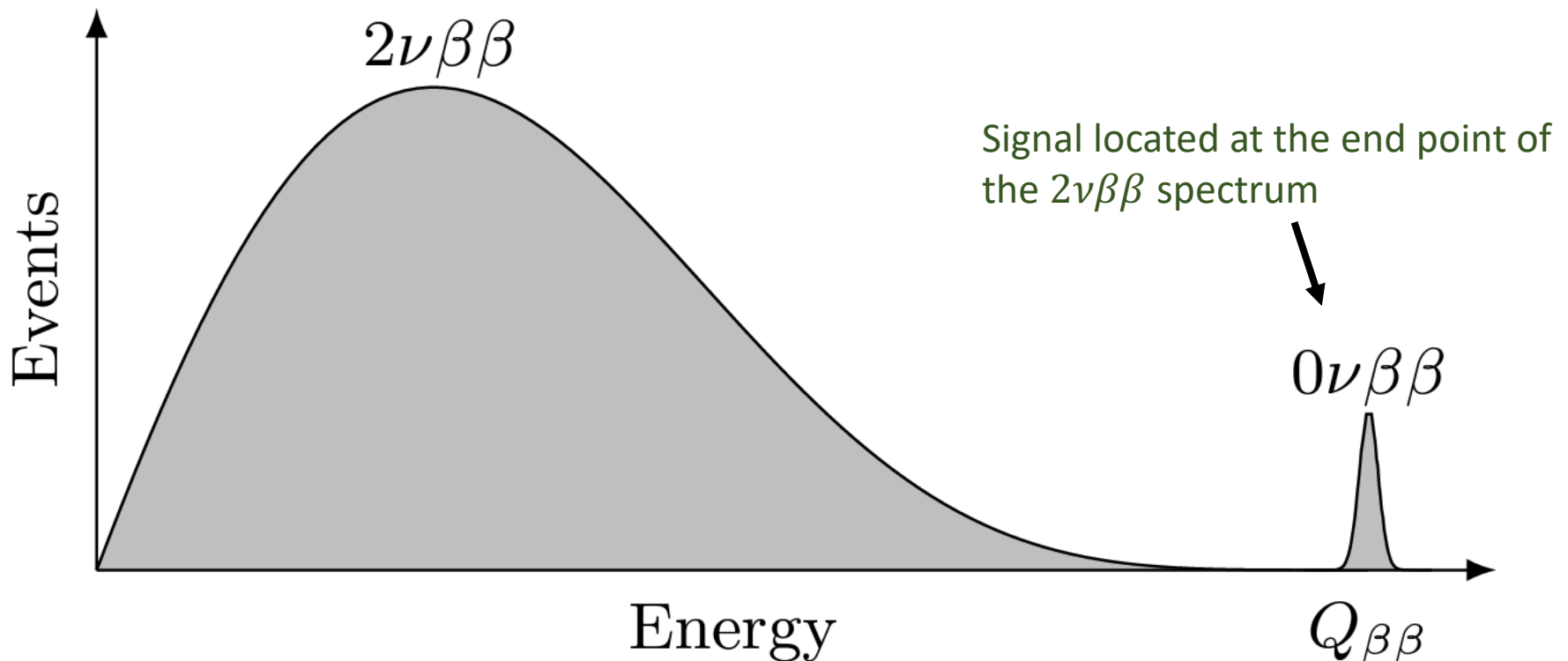
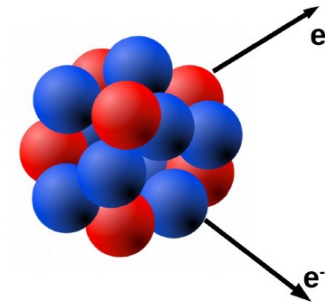
Effective mass of neutrino  
Particle Physics

Your choice of double-beta  
decay isotope

# Neutrinoless Double Beta decay ( $0\nu\beta\beta$ )

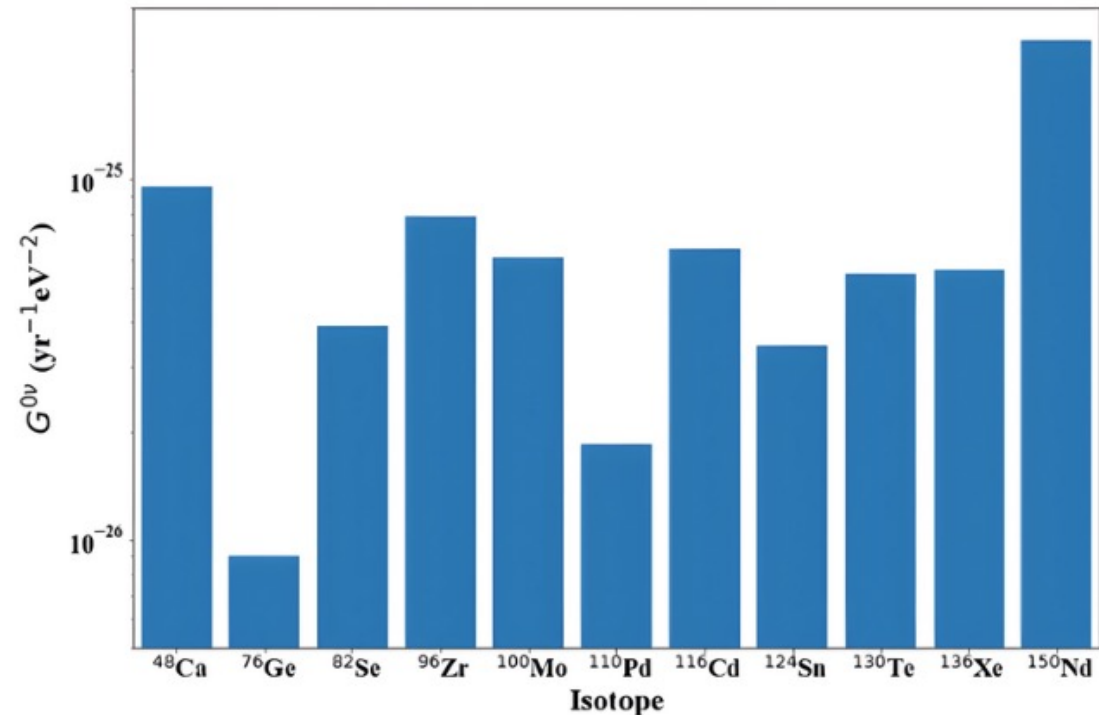
- Majorana neutrinos annihilate giving almost all the energy to the electrons

→ Cannot happen for Dirac neutrino



# Phase Space Factor: $G$

- Factor accounts for the atomic physics relating to the emitted electrons
- Depends on the  $Q^5$  and  $Z$  of the isotope
- Can be calculated with reasonable accuracy
  - Need good accurate description of the Coulomb field on the decay electron wave-functions



# Nuclear Matrix Elements (NME): $|M^2|$

- Accounts for the structure of the initial and final states of the nucleus
  - Challenging and is one of the largest sources of theoretical uncertainty

$$M = M_{\text{long}} + M_{\text{short}}$$

$$g_A^2 M_{GT} - g_V^2 M_F + g_A^2 M_T$$

Gamow-Teller

Fermi

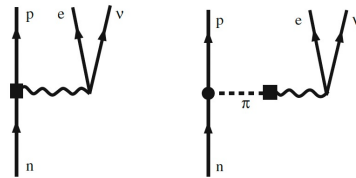
Tensor

$$2g_V^{NN} m_\pi^2 M_{CT}$$

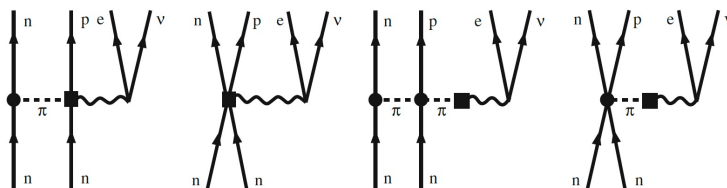
Contact Operator

Weak nucleon currents

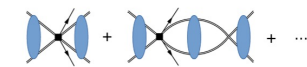
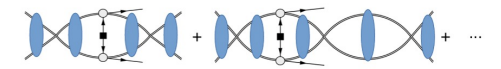
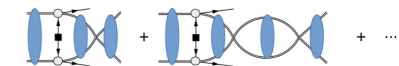
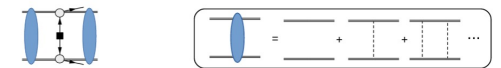
1-body



2-body



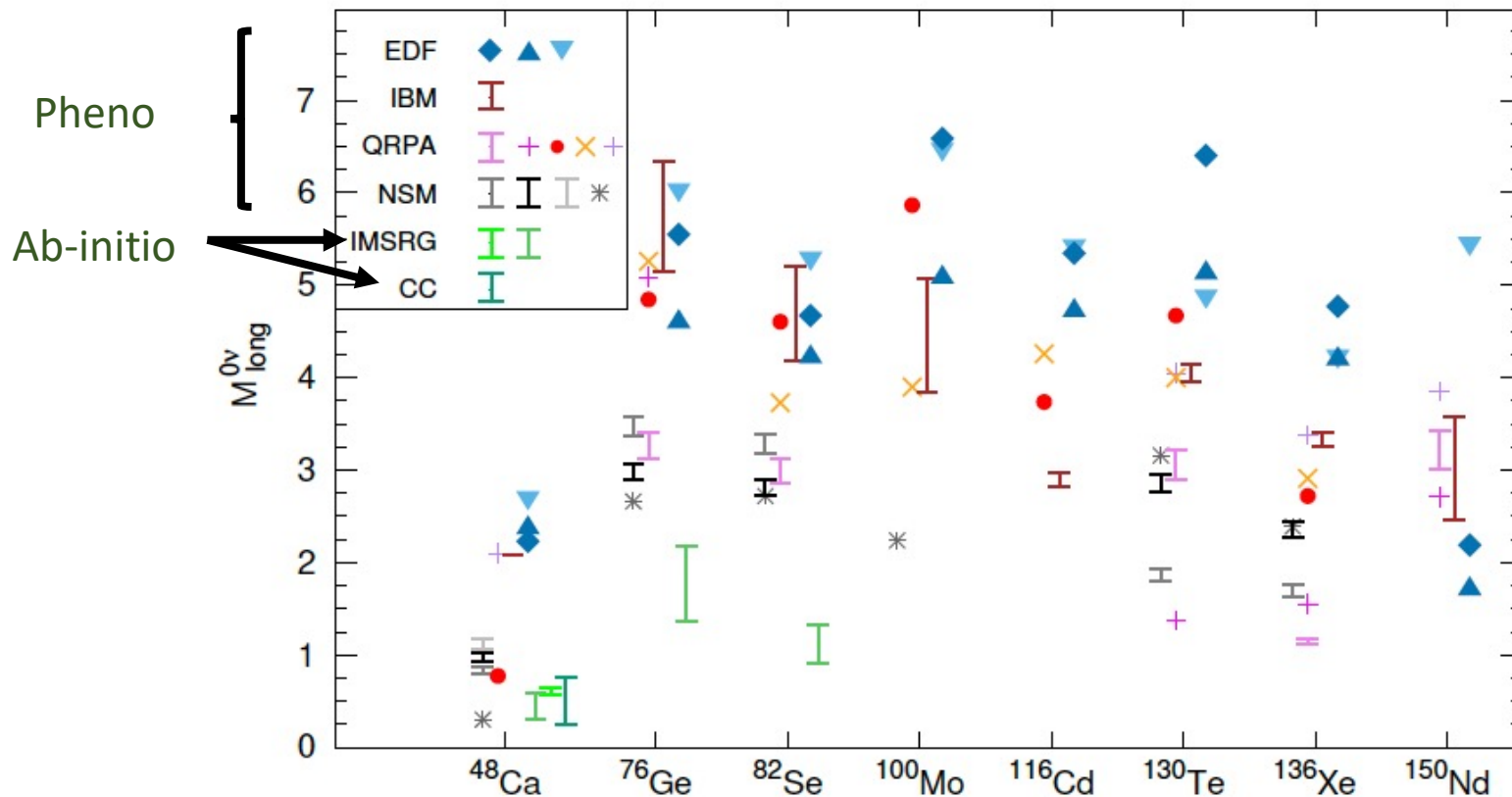
New term added to account for short-range contributions (2018)



Cirigliano, et al, Phys. Rev. Lett. 120, 202001

# Nuclear Matrix Elements (NME): $|M^2|$

- Phenomenological nuclear models have variability, each with different physics approaches
  - Lack of constraining data
  - Spread is dependent on isotope

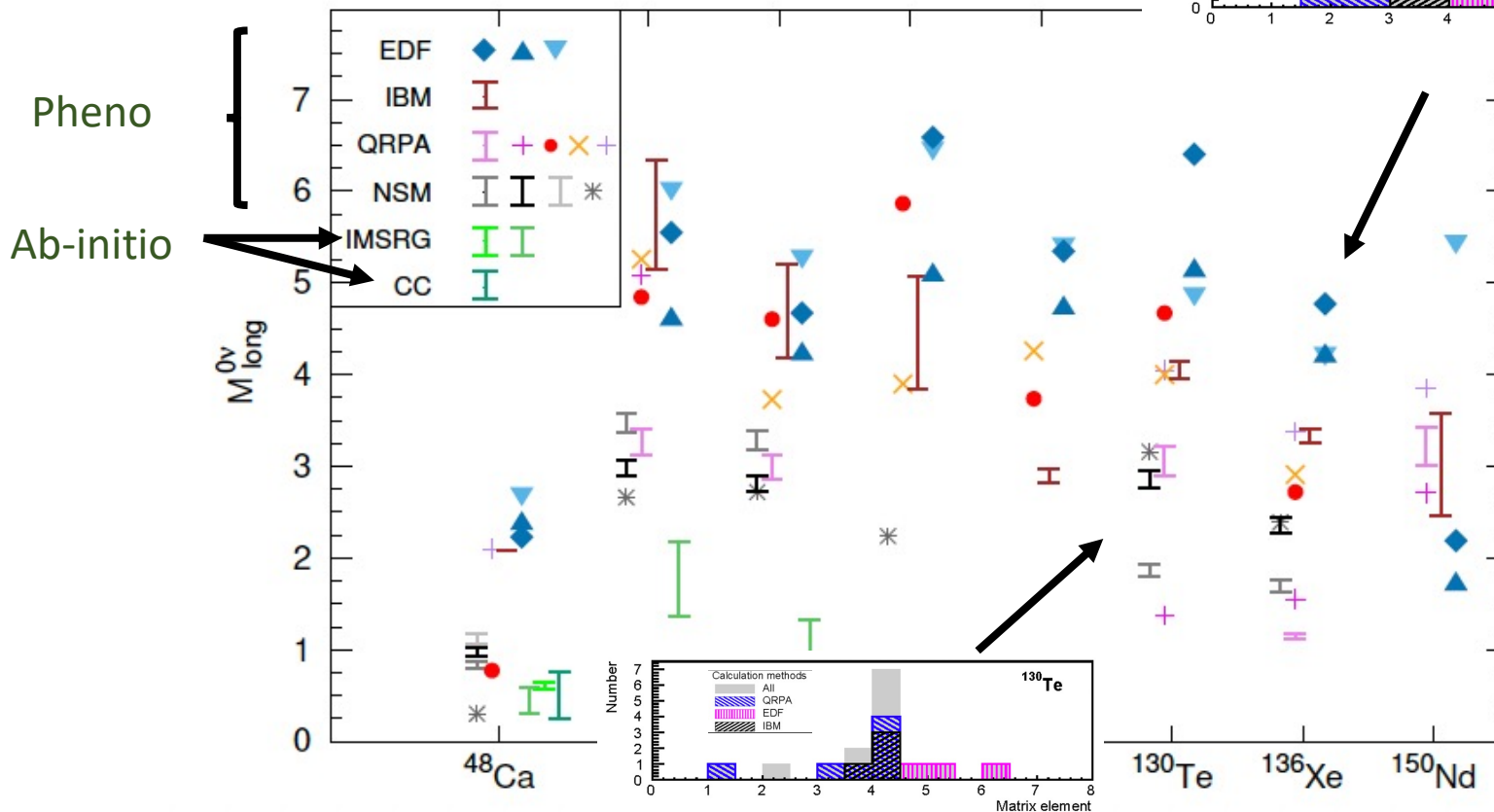
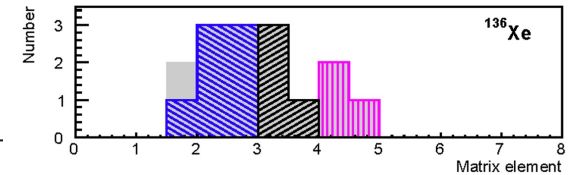




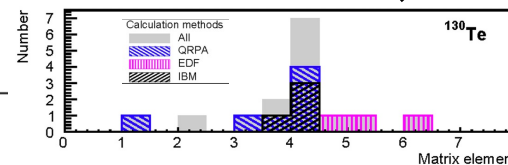
# Nuclear Matrix Elements (NME): $|M^2|$

- Phenomenological nuclear models have variability, each with different physics approaches
  - Lack of constraining data
  - Spread is dependent on isotope

Some clustering of pheno predictions towards a central value

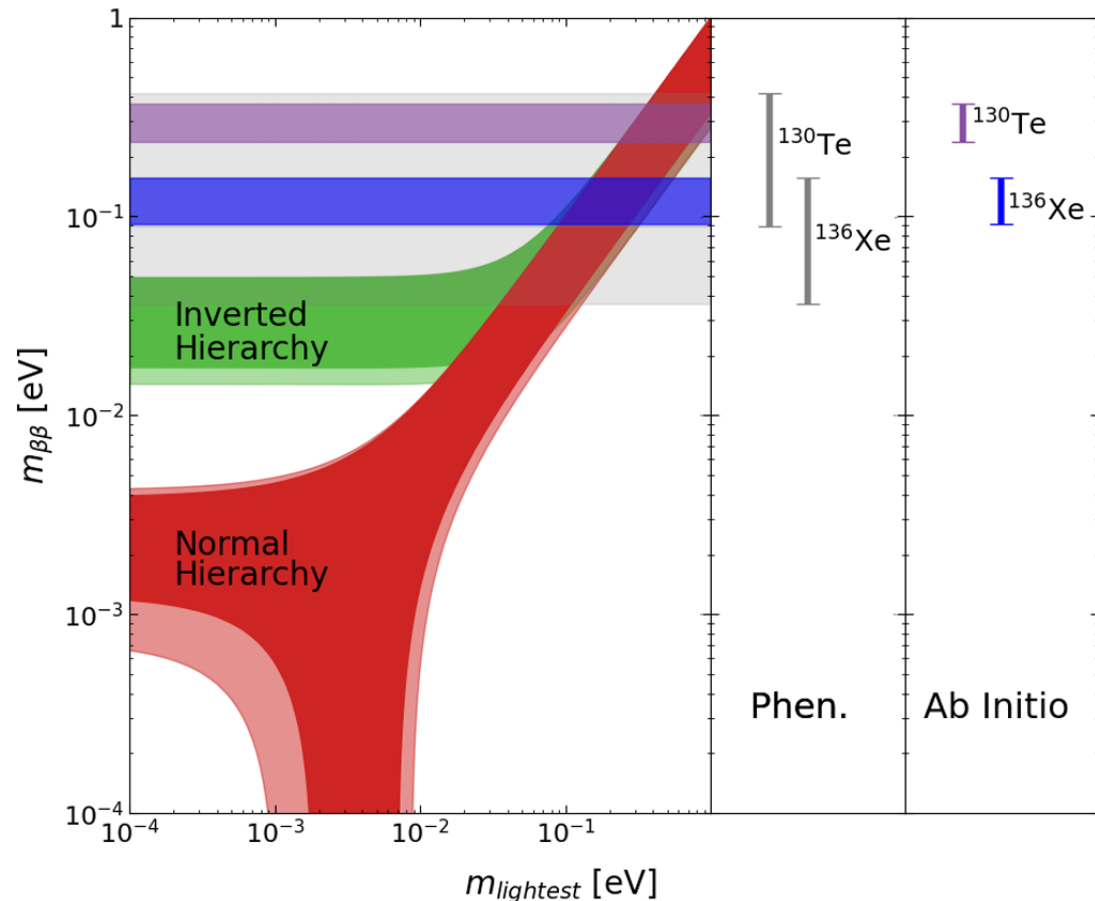


arXiv: 1805.11142



# Recent Ab-initio Calculations

- Recent Ab-initio calculations tend to reduce the NME with reduced uncertainty
  - Better control of  $g_A$  quenching and short-range contributions
- Refinements are still being made to the calculations e.g. higher order terms (IMSRG(3))
- Inverted hierarchy in non-degenerate region may not have been probed yet with current ab-initio estimates



Belley et al, arXiv 2307.15156 (2023)

# $m_{\beta\beta}$ in the minimal mechanism

Minimal mechanism: exchange of light Majorana neutrinos

$$\begin{aligned}
 m_{\beta\beta} &= \left[ \begin{array}{c} \text{Diagram 1: } d_L \rightarrow u_L, d_L \rightarrow u_L, e_L^- \rightarrow e_L^-, e_L^- \rightarrow e_L^-, \nu_1 \\ \text{Diagram 2: } d_L \rightarrow u_L, d_L \rightarrow u_L, e_L^- \rightarrow e_L^-, e_L^- \rightarrow e_L^-, \nu_2 \\ \text{Diagram 3: } d_L \rightarrow u_L, d_L \rightarrow u_L, e_L^- \rightarrow e_L^-, e_L^- \rightarrow e_L^-, \nu_3 \end{array} \right]^2 \\
 &= \left[ (U_{e1})^2 m_1 + (U_{e2})^2 m_2 + (U_{e3})^2 m_3 \right]^2 \\
 &= \left[ c_{12}^2 c_{13}^2 e^{2i\alpha} m_1 + c_{12}^2 s_{12}^2 e^{2i\beta} m_2 + s_{13}^2 m_3 \right]^2
 \end{aligned}$$

# $m_{\beta\beta}$ in the minimal mechanism

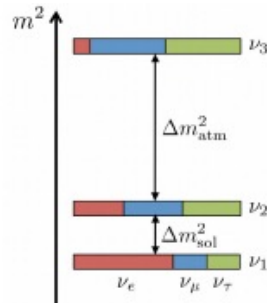
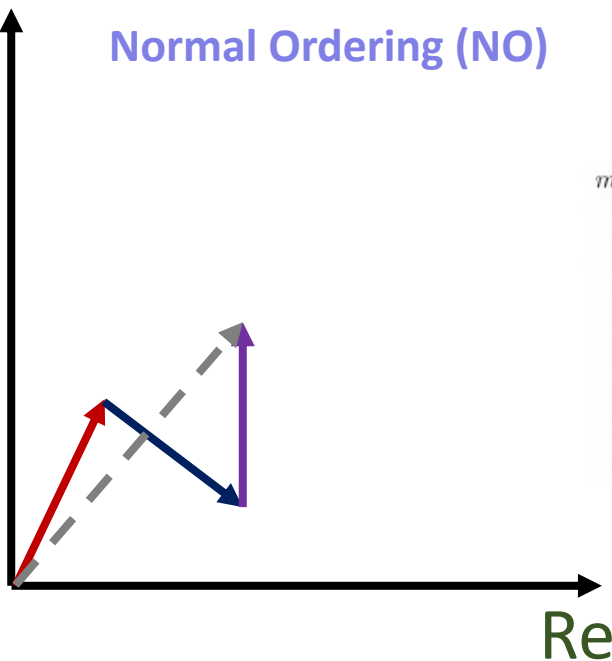
Minimal mechanism: exchange of light Majorana neutrinos

$$m_{\beta\beta} = \left| c_{12}^2 c_{13}^2 e^{2i\alpha} m_1 + c_{12}^2 s_{12}^2 e^{2i\beta} m_2 + s_{13}^2 m_3 \right|^2$$

$\alpha$  and  $\beta$  are unknown CP phases not determinable by neutrino oscillations

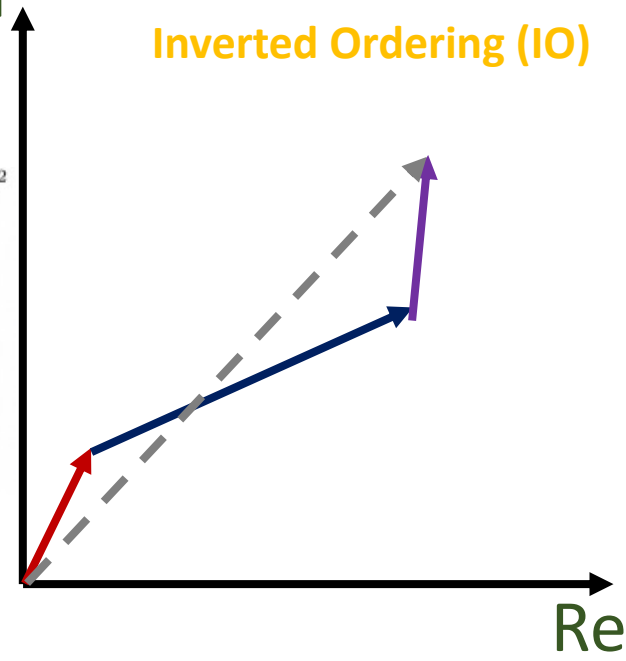
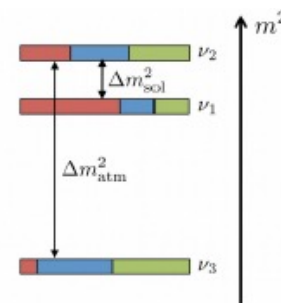
Im

Normal Ordering (NO)



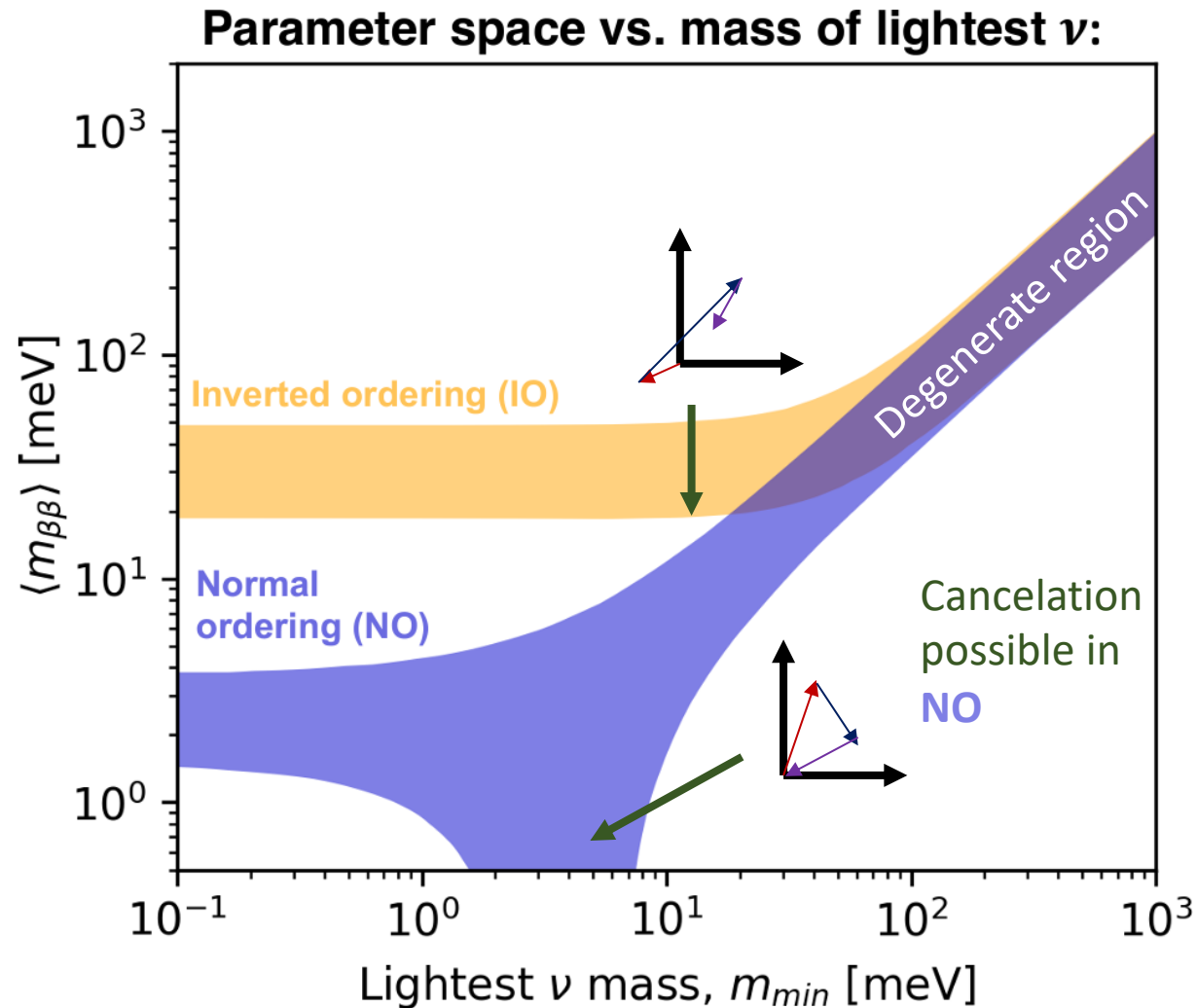
Im

Inverted Ordering (IO)



# $m_{\beta\beta}$ in the minimal mechanism

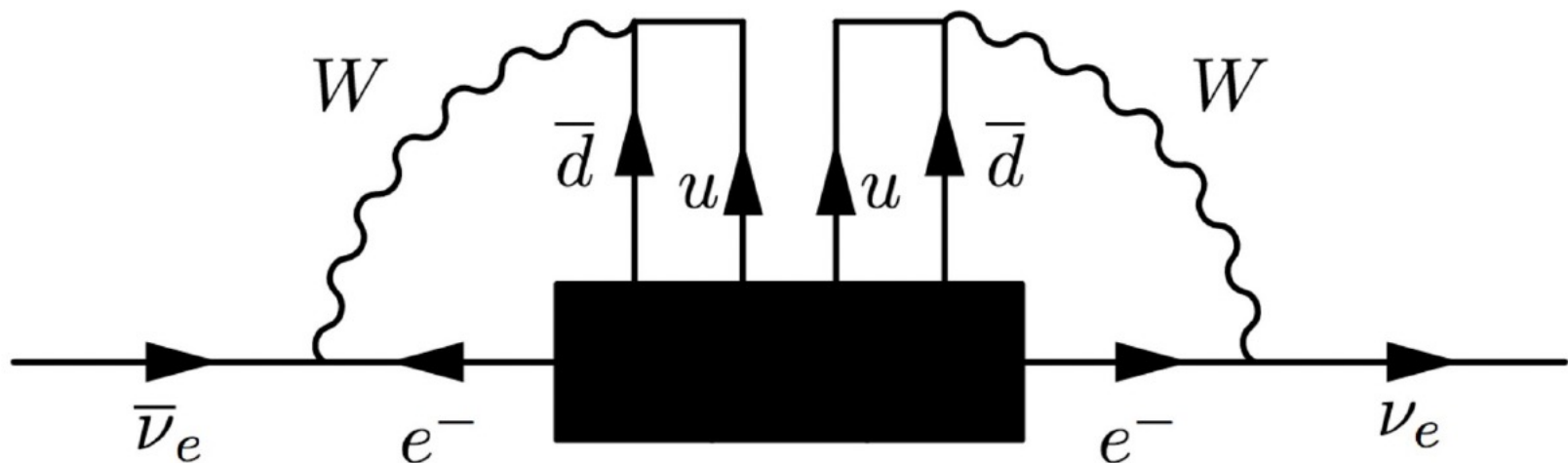
- **NO** and **IO** have different lightest neutrino mass
- Thickness to bands due to uncertainty on phases
- Smallest value of  $m_{\beta\beta}$  in **IO** is  $\sim 20\text{meV}$



# Black Box Theorem (Schechter-Valle)

J. Schechter and J. W. F. Valle  
Phys. Rev. D 25, 2951

- Light Majorana exchange may induce  $0\nu\beta\beta$  and a give source of LNV
  - It may not be the only mechanism driving the process
- Black-box theorem states that for any possible source of LNV that causes  $0\nu\beta\beta$ , we can draw a Feynman diagram enclosing this new physics
  - We still learn neutrinos are Majorana from observing  $0\nu\beta\beta$



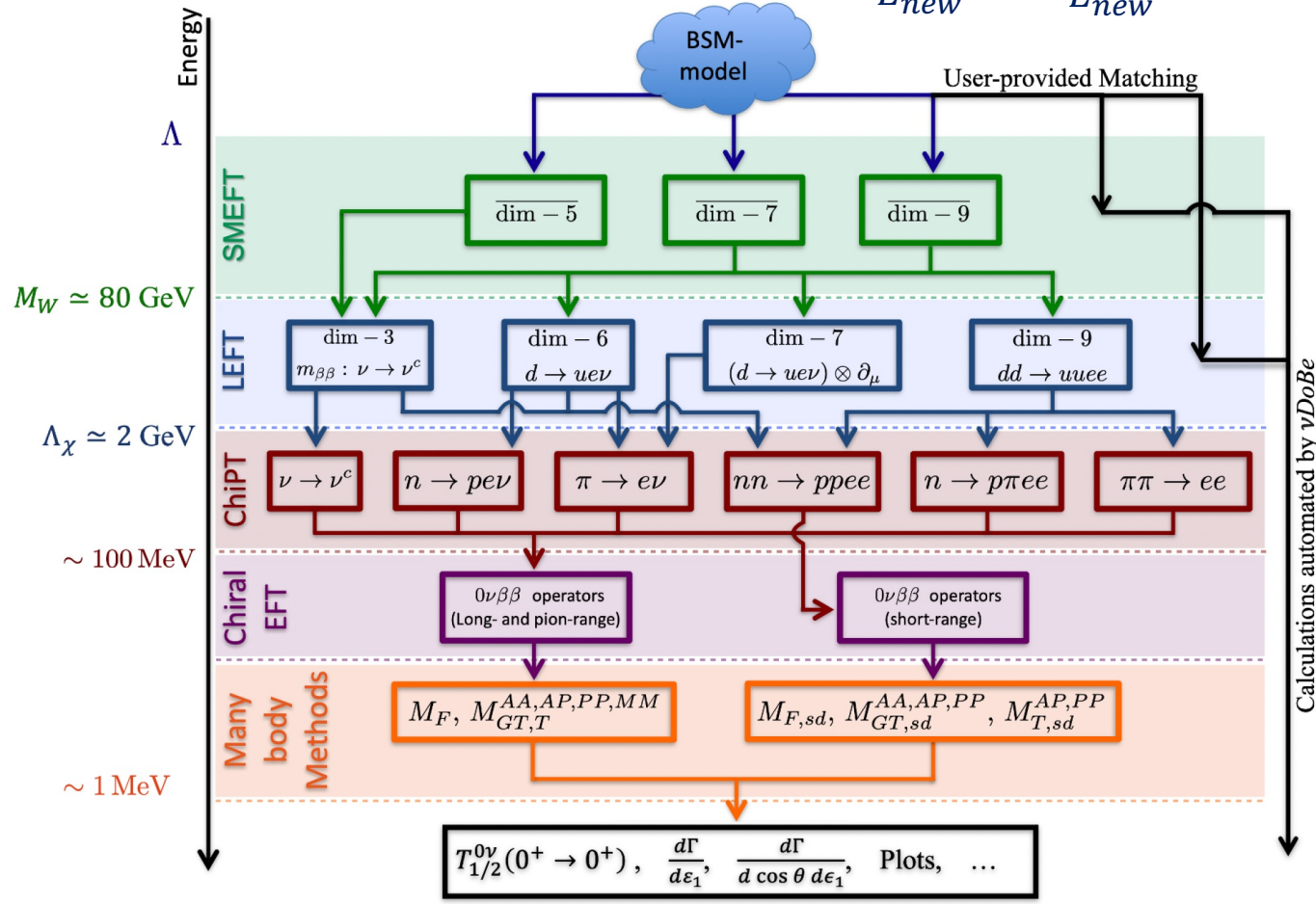
# Decay Rate with higher dim operators

- More general form of the decay rate accounting for LNV physics in an EFT framework

$$L = L_{SM} + \frac{1}{E_{new}} L_1 + \frac{1}{E_{new}^2} L_2 + \dots$$

- Odd operators provide sources of LNV

- Higher order operators can also drive the rate of  $0\nu\beta\beta$ !



Scholer, O., de Vries, J. & Gráf, L. J. *High Energ. Phys.* 2023, 43 (2023).

# Decay Rate with higher dim operators

- More general form of the decay rate accounting for LNV physics in an EFT framework: “Master Formula”

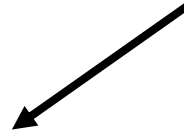
$$T_{1/2} = \left[ g_A^4 \sum_k G_{0k} |\mathcal{A}_k(\{C_i\})|^2 \right]^{-1}$$

Phase-space factor

Sub-amplitudes that depend on:

- NME
- low-energy constants e.g.  $g_V^{NN}$
- Wilson Coefficients ( $C_i$ )

Class	Op. Name	Code Label	Op. Structure	Half-Life Group	SMEFT Dim.
<b>Dim 3</b>					
$\Psi^2$	$\mathcal{O}_{m\beta\beta}$	m_bb	$-\frac{1}{2}m_{ee}\overline{\nu_{L,e}^C}\nu_{L,e}$	$m_{\beta\beta}$	5
<b>Dim 6</b>					
$\Psi^4$	$\mathcal{O}_{SL}^{(6)}$	SL(6)	$[\overline{u}_R d_L][\overline{e}_L \nu_L^C]$	$C_S^{(6)}$	7
	$\mathcal{O}_{SR}^{(6)}$	SR(6)	$[\overline{u}_L d_R][\overline{e}_L \nu_L^C]$	$C_S^{(6)}$	7
	$\mathcal{O}_{VL}^{(6)}$	VL(6)	$[\overline{u}_L \gamma^\mu d_L][\overline{e}_R \gamma_\mu \nu_L^C]$	$C_{VL}^{(6)}$	7
	$\mathcal{O}_{VR}^{(6)}$	VR(6)	$[\overline{u}_R \gamma^\mu d_R][\overline{e}_R \gamma_\mu \nu_L^C]$	$C_{VR}^{(6)}$	7
	$\mathcal{O}_T^{(6)}$	T(6)	$[\overline{u}_L \sigma^{\mu\nu} d_R][\overline{e}_L \sigma_{\mu\nu} \nu_L^C]$	$C_T^{(6)}$	7
<b>Dim 7</b>					
$\Psi^4 \partial$	VL(7)	$\mathcal{O}_{VL}^{(7)}$	$[\overline{u}_L \gamma^\mu d_L][\overline{e}_L \overleftrightarrow{\partial}_\mu \nu_L^C]$	$C_V^{(7)}$	7
	VR(7)	$\mathcal{O}_{VR}^{(7)}$	$[\overline{u}_R \gamma^\mu d_R][\overline{e}_L \overleftrightarrow{\partial}_\mu \nu_L^C]$	$C_V^{(7)}$	7

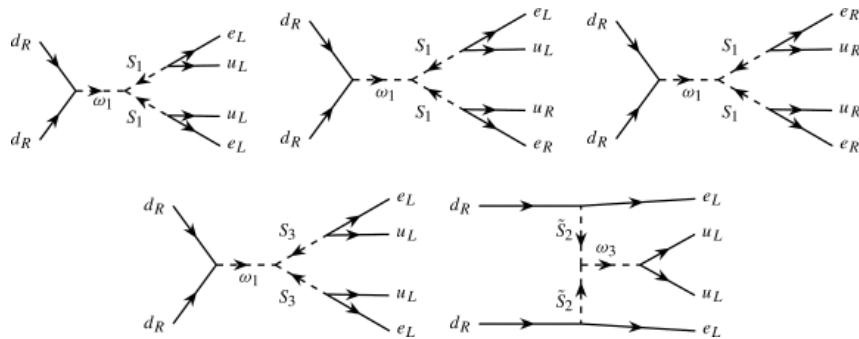




# Testing EFT Models

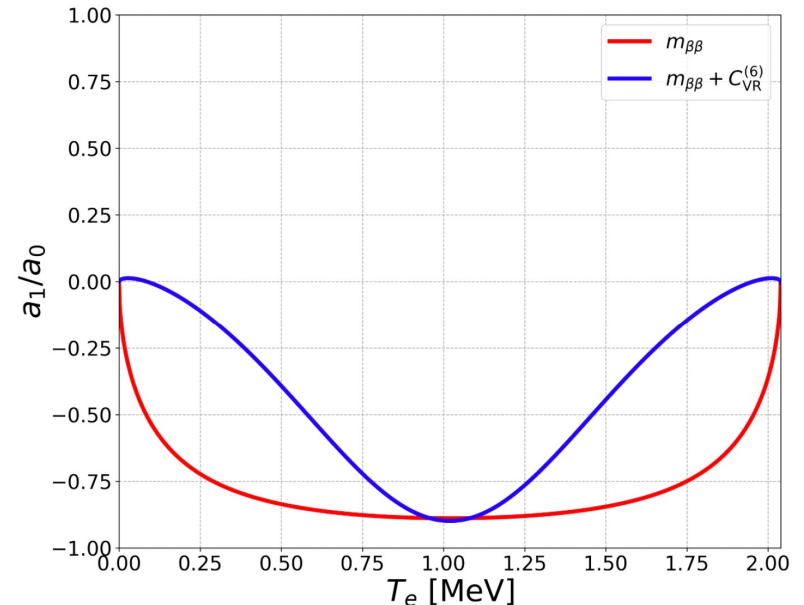
- Electron energy and angular kinematics can be different for your model
- If your detector can resolve the electron tracks, you can tell the difference!

Your favourite LNV theory



Leptoquarks, SUSY, Kaluza Klein,  
LR symmetric couplings, etc

Figure made with  $\nu$ DoBE  $\rightarrow$  generator  
to calculate your EFT event spectra!



[Scholer, O., de Vries, J. & Gráf, L. J. High Energ. Phys. 2023, 43 \(2023\).](#)

# Testing EFT Models

- Electron energy and angular kinematics can be different for your model
- If your detector can resolve the electron tracks, you can tell the difference! e.g. NEXT!

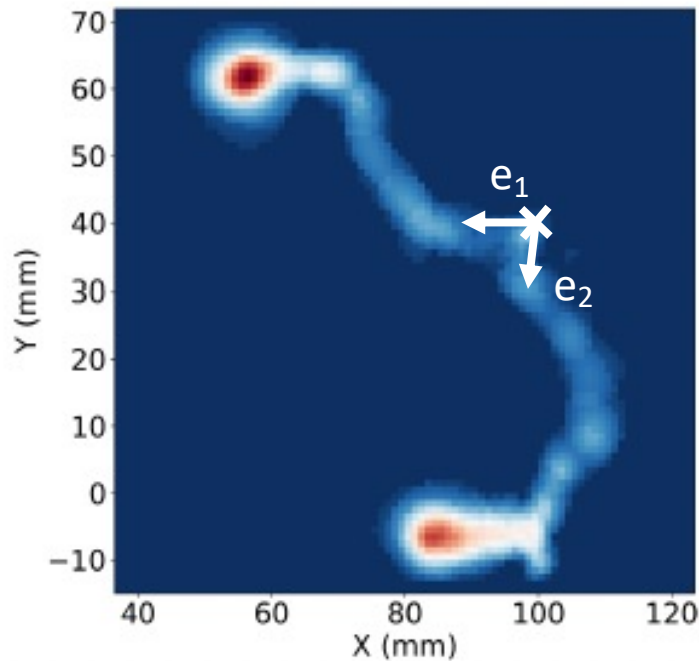
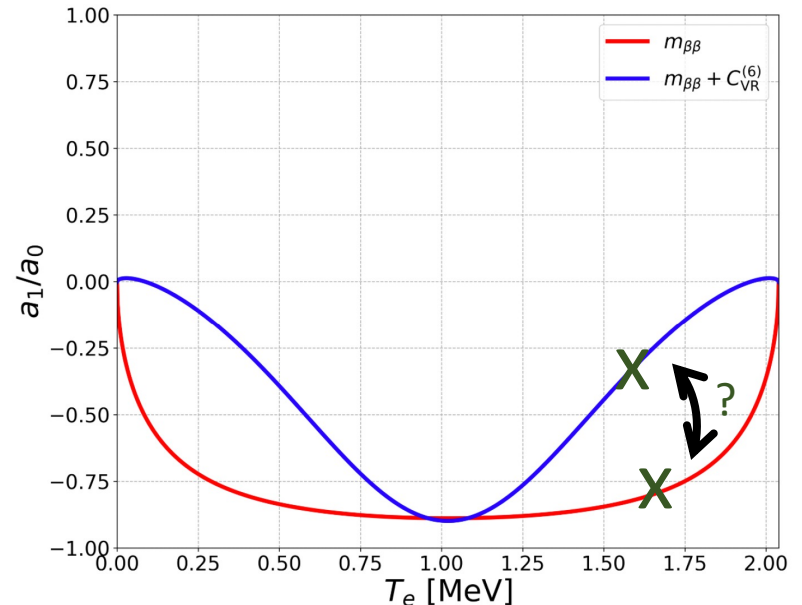


Figure made with  $\nu$ DoBE  $\rightarrow$  generator to calculate your EFT event spectra!



I work on this, so it gets a slide :-)

[Scholer, O., de Vries, J. & Gráf, L. J. High Energ. Phys. 2023, 43 \(2023\).](#)

# Summary

- $0\nu\beta\beta$  is the most sensitive way to probe the Majorana nature of the neutrino
- Majorana neutrinos provide a more natural way to explain the lightness of the neutrino mass, and are a prediction of theories such as leptogenesis
- Significant new theory efforts in the estimation of nuclear matrix elements with uncertainties, including recent ab-initio efforts
- Rich source of lepton number violating physics that could drive  $0\nu\beta\beta$  beyond light-Majorana exchange