

CETUP* 2023

06 July, 2023

Lead/Deadwood Middle School

Radiative corrections in neutrino physics

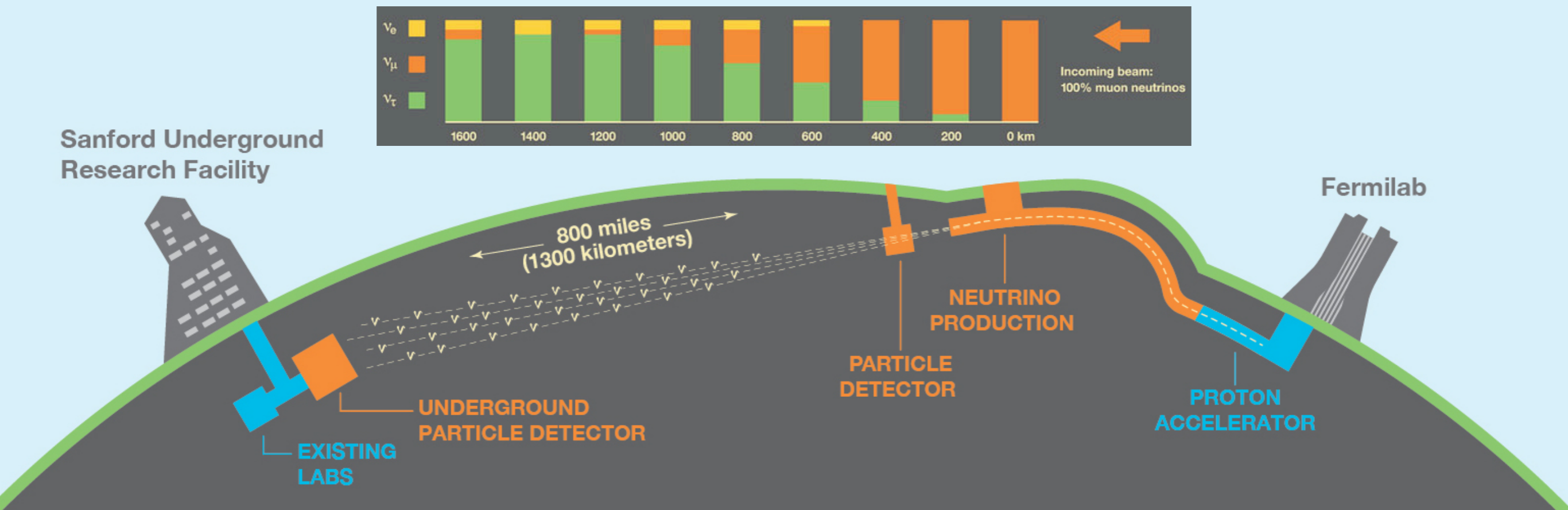


Oleksandr (Sasha) Tomalak

LA-UR-23-27032

Neutrino experiments

- **DUNE** and Hyper-K: leading-edge ν science experiments



- measurement of $\nu_\mu(\bar{\nu}_\mu)$ disappearance and $\nu_e(\bar{\nu}_e)$ appearance

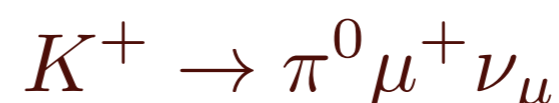
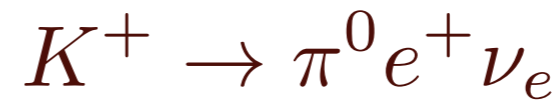
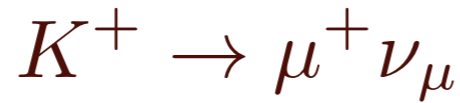
$$N_\nu \sim \int dE_\nu \Phi_\nu(E_\nu) \times \sigma(E_\nu) \times R(E_\nu, E_\nu^{\text{rec}})$$

- near detector: determine flux and cross sections

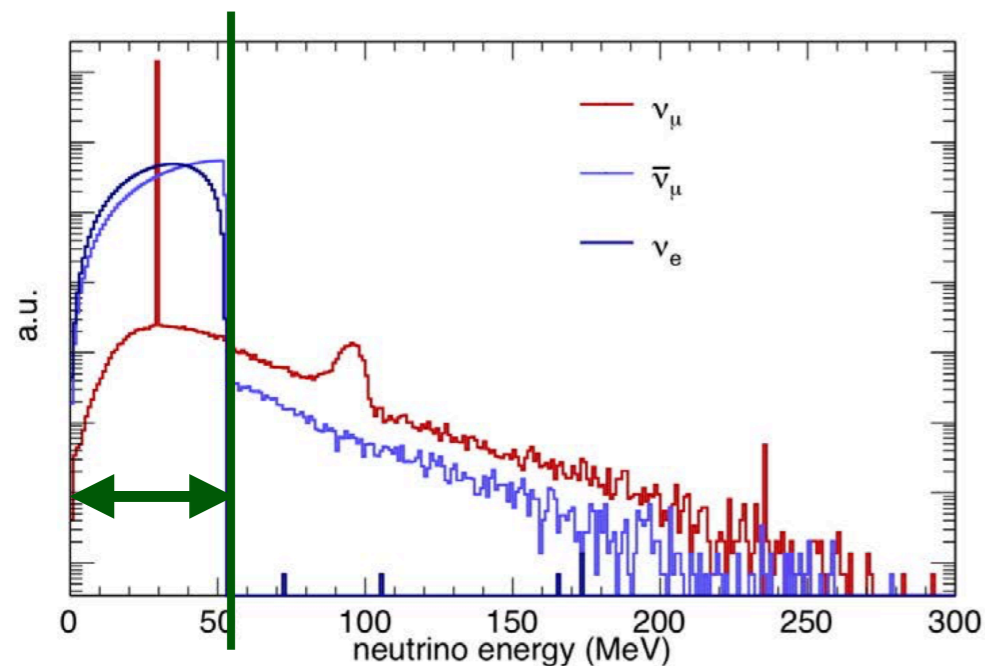
Outline

- 1) artificial neutrino sources
- 2) cross sections on electrons, nucleons, and nuclei
- 3) radiative corrections in neutrino physics
- 4) charged-current scattering on **nucleons**

Artificial neutrinos: accelerator



decay at rest

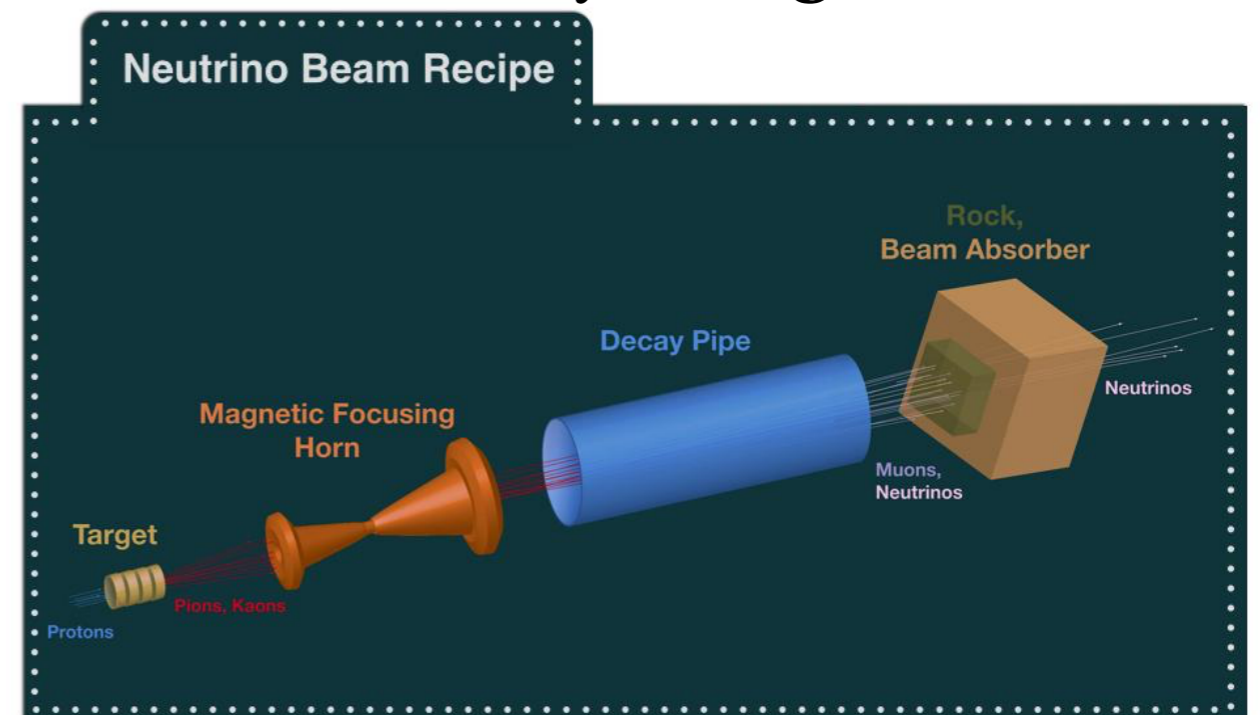


Akimov et al., Science 357 6356, 1123-1126 (2017)

Coherent and CCM

meson decay: monochromatic line

decay in flight



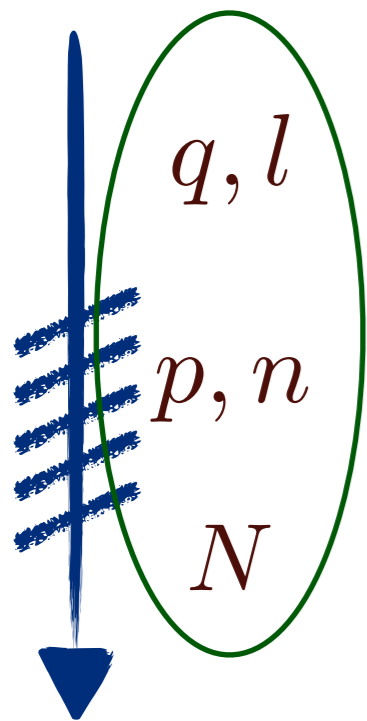
www.fnal.gov

T2K, NOvA, MiniBooNE, MicroBooNE

MINERvA, MINOS, NuTeV

SBN, DUNE, HyperK, ESSnuSB

- precise measurements of neutrino properties, EW, and BSM search
- physics program relies on neutrino cross sections in MeV-TeV range



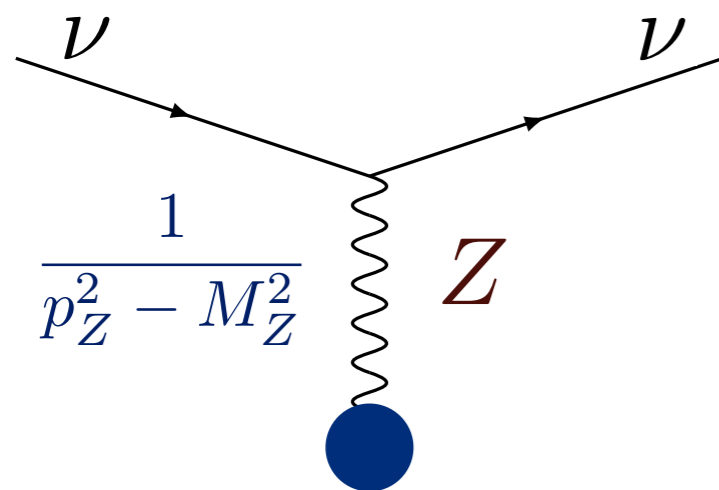
Cross sections on electrons, nucleons, and nuclei

Neutral- and charged-current processes

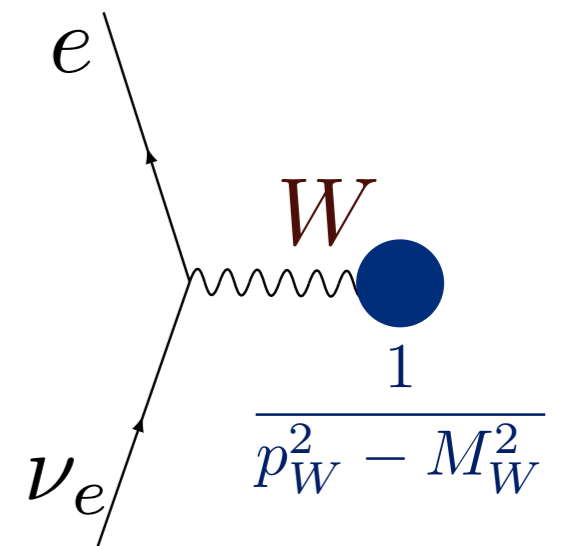
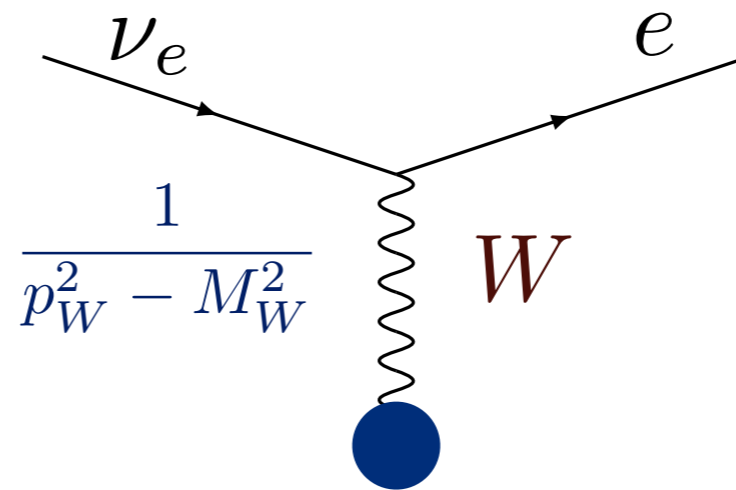
- cross sections determine neutrino-induced events

$$N_\nu \sim \int dE_\nu \Phi_\nu(E_\nu) \times \sigma(E_\nu) \times R(E_\nu, E_\nu^{\text{rec}})$$

neutral current



charged current



- contact interactions at GeV energy scale and below

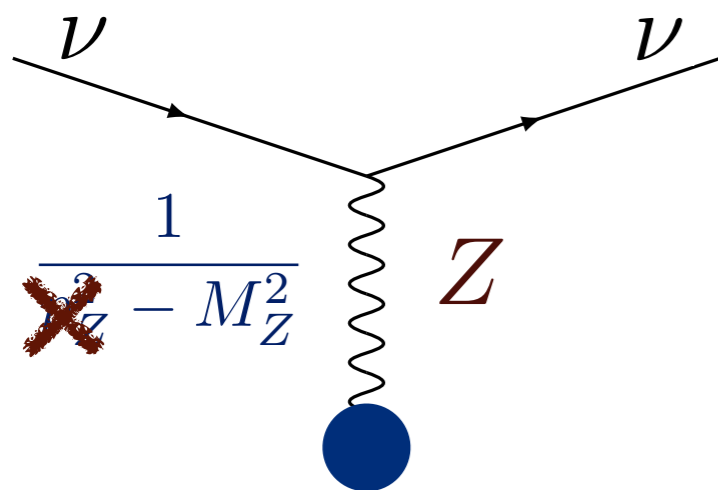
- charged current (only): **threshold** to produce lepton and recoil
- neutral current: **no thresholds**

Neutral- and charged-current processes

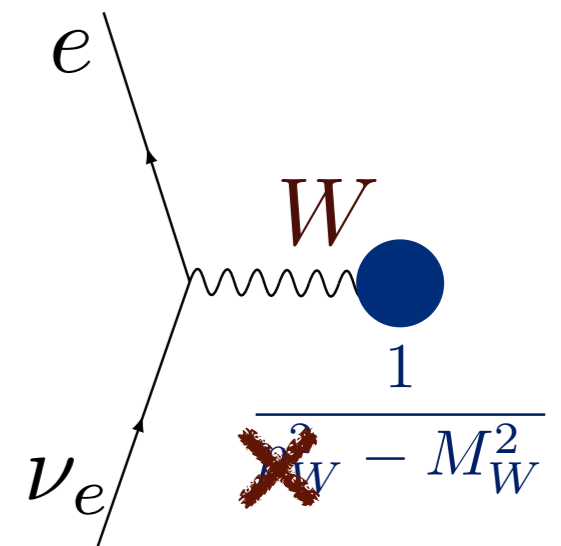
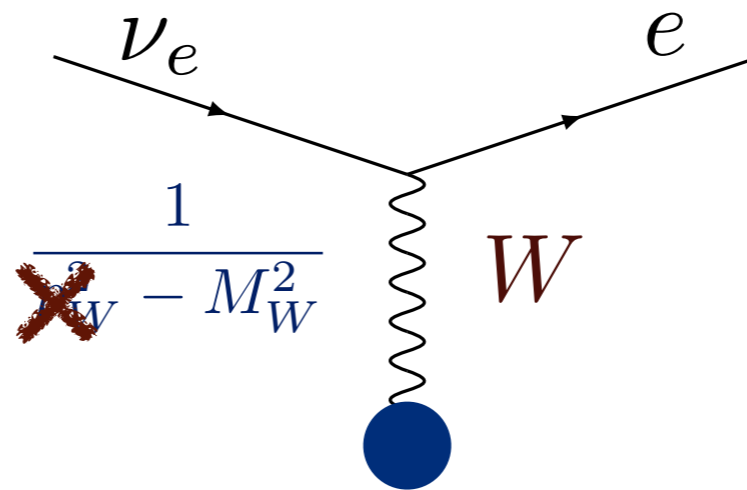
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$$N_\nu \sim \int dE_\nu \Phi_\nu(E_\nu) \times \sigma(E_\nu) \times R(E_\nu, E_\nu^{\text{rec}})$$

neutral current



charged current

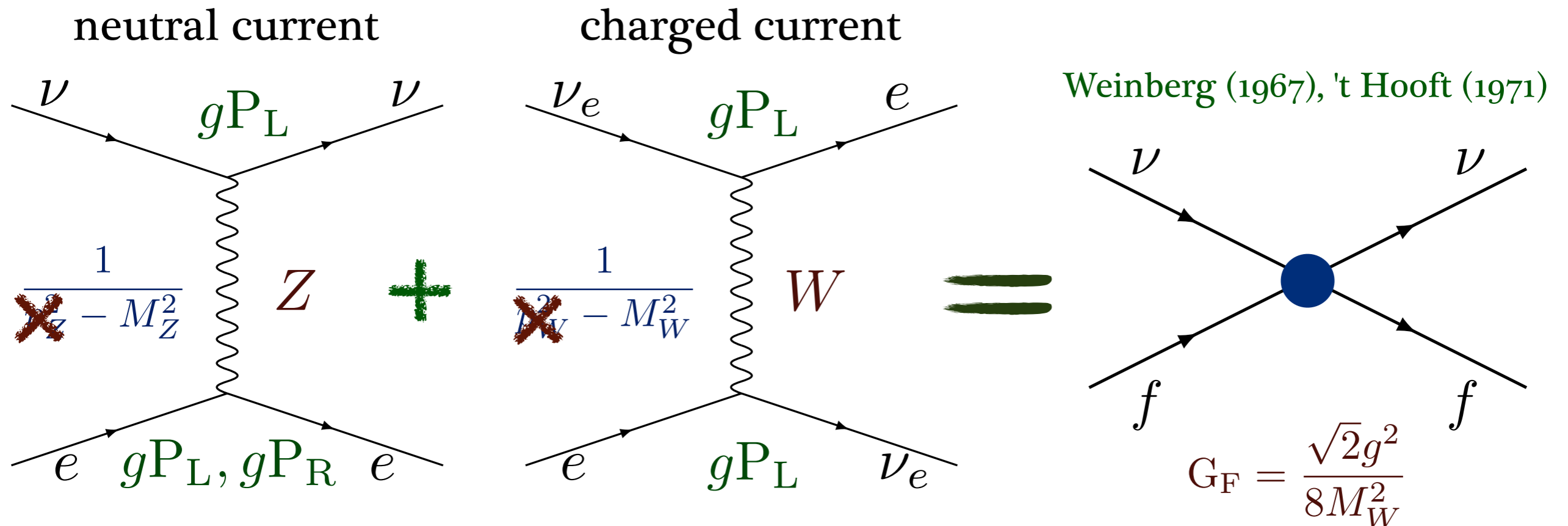


- contact interactions at GeV energy scale and below

- charged current (only): **threshold** to produce lepton and recoil
- neutral current: **no thresholds**

Neutrino-electron scattering

- Fermi theory at GeV energies and below, $\sigma \sim m$

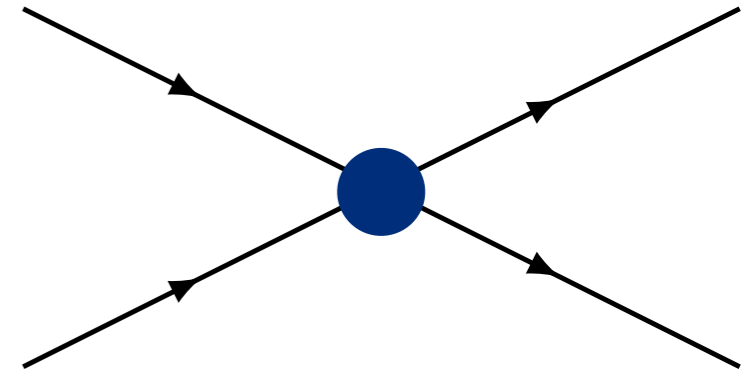


- s-channel resonant enhancement at vector-boson pole (PeV scale)

- historically: precise EW physics and BSM searches
- channel for in-situ flux constraints at accelerator experiments
- solar neutrinos@Super-K, SNO, Borexino
- recent observation of Glashow resonance by IceCube

Neutrino-nucleon scattering (CC)

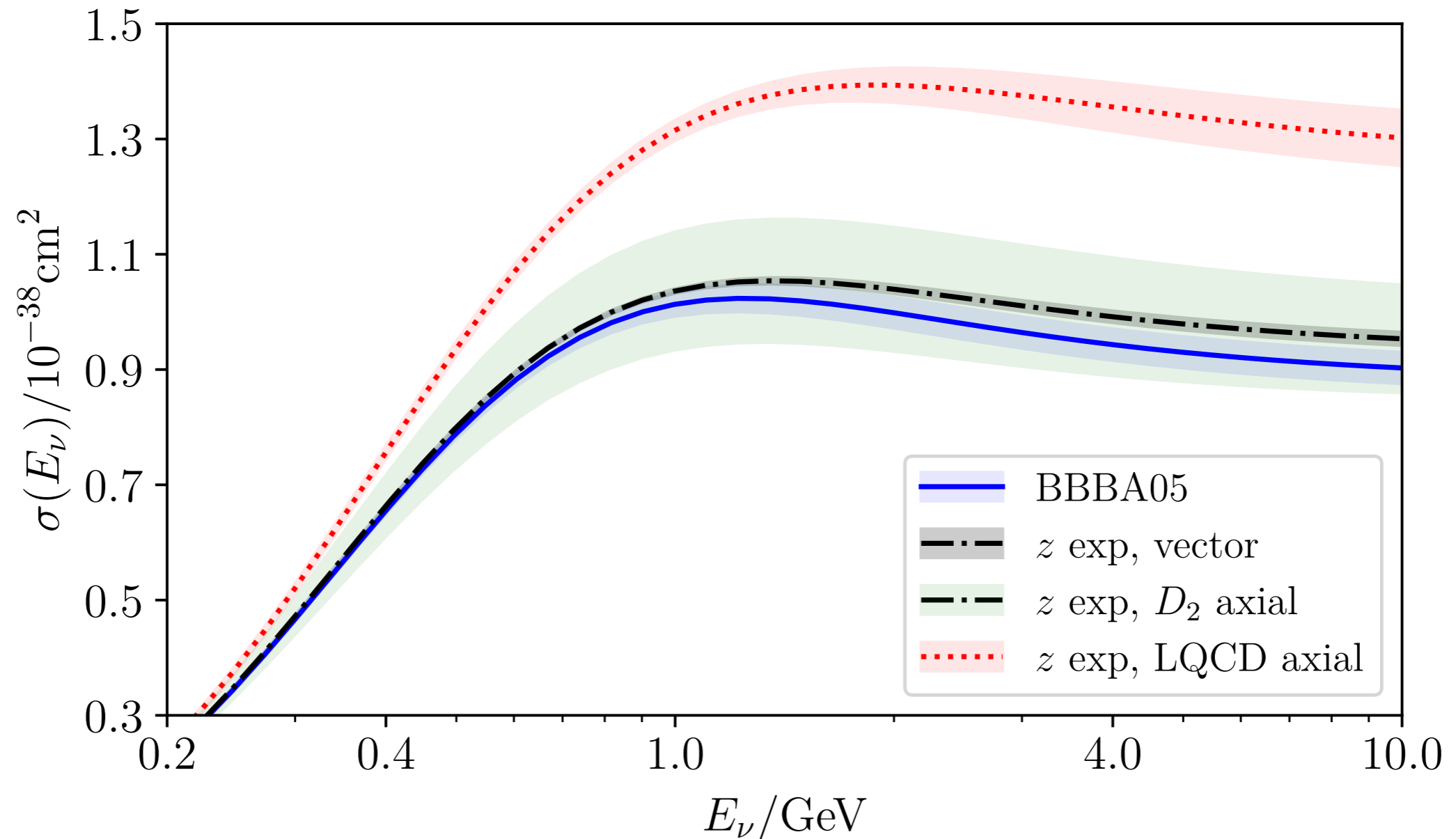
- 4-Fermi theory + ChPT @ and $<$ pion-mass scale
- thresholds: muon ~ 110 MeV, tau ~ 3.5 GeV
- only electron flavor for supernova, solar and reactor neutrinos
- deuterium bubble chamber data in 1980th
- provide nucleon axial form factor
- target for many lattice QCD groups



Fermilab bubble chamber, Richard Drew

- elastic scattering \rightarrow pion production \rightarrow deep inelastic scattering

Neutrino-nucleon scattering (CC)



A.S. Meyer, A. Walker-Loud, C. Wilkinson, Ann. Rev. of 72, 010622-120608 (2022)

A.S. Meyer, M. Betancourt, R. Gran, and R.J. Hill, PRD (2016)

Kaushik Borah, Gabriel Lee, Richard J. Hill, and O. T., PRD (2021)

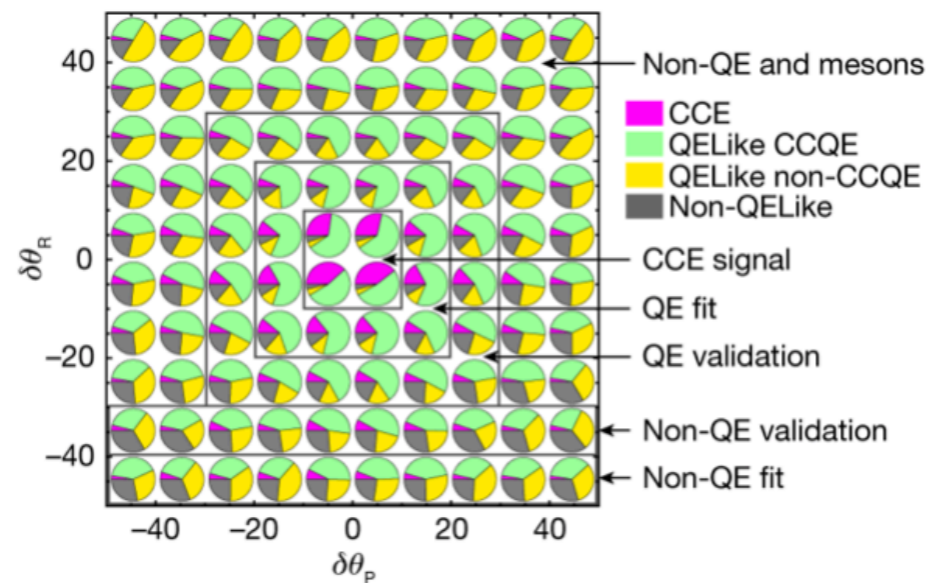
- knowledge of vector structure stops a progress in studies of axial
- acknowledged discrepancy: lattice QCD \leftrightarrow experimental data

MINERvA result with free protons

- idea of scattering on molecular hydrogen realized !!!

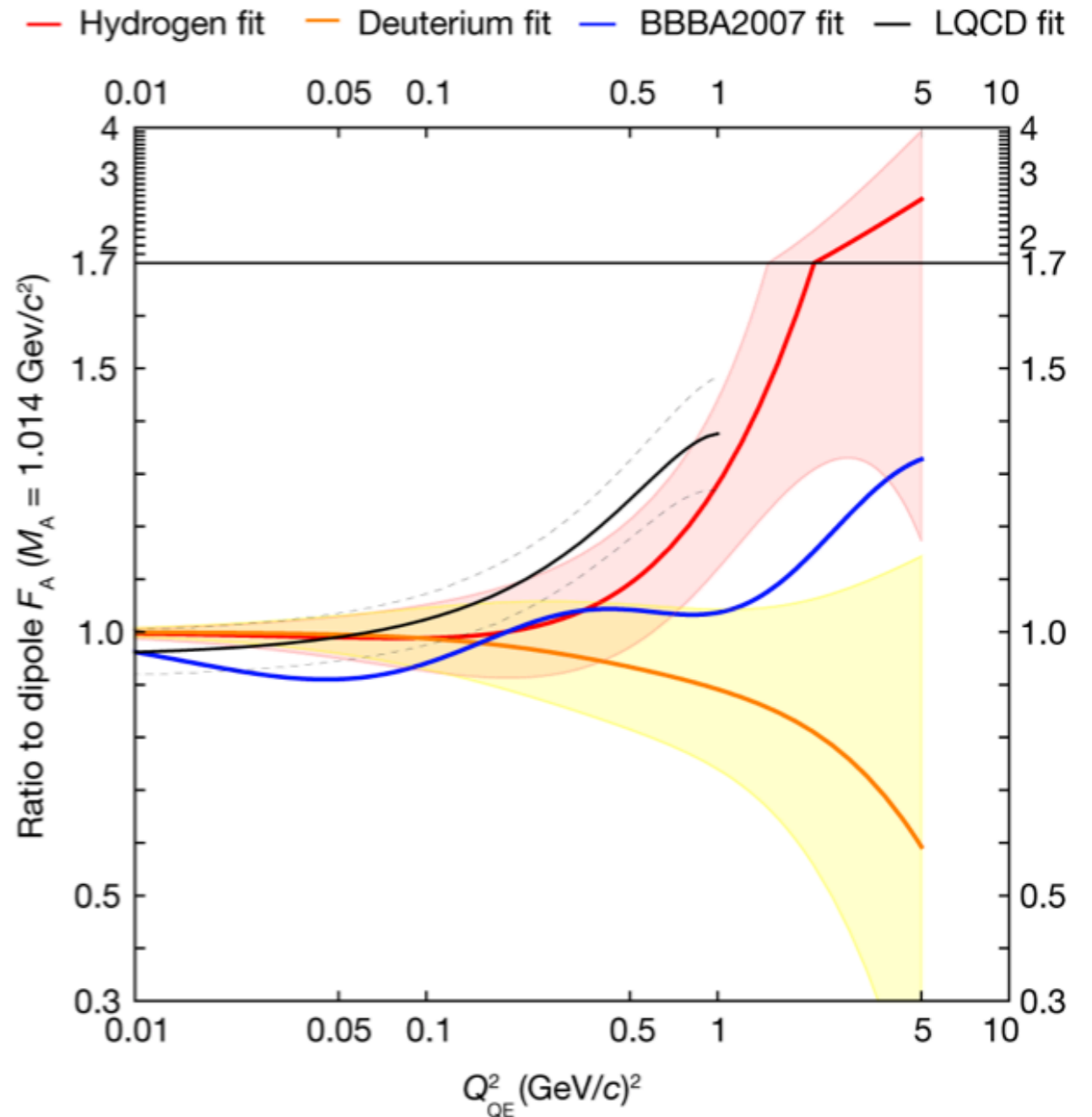


kinematic selection



5580 events over
12500 background

background nuclear events
constrained by scattering of ν

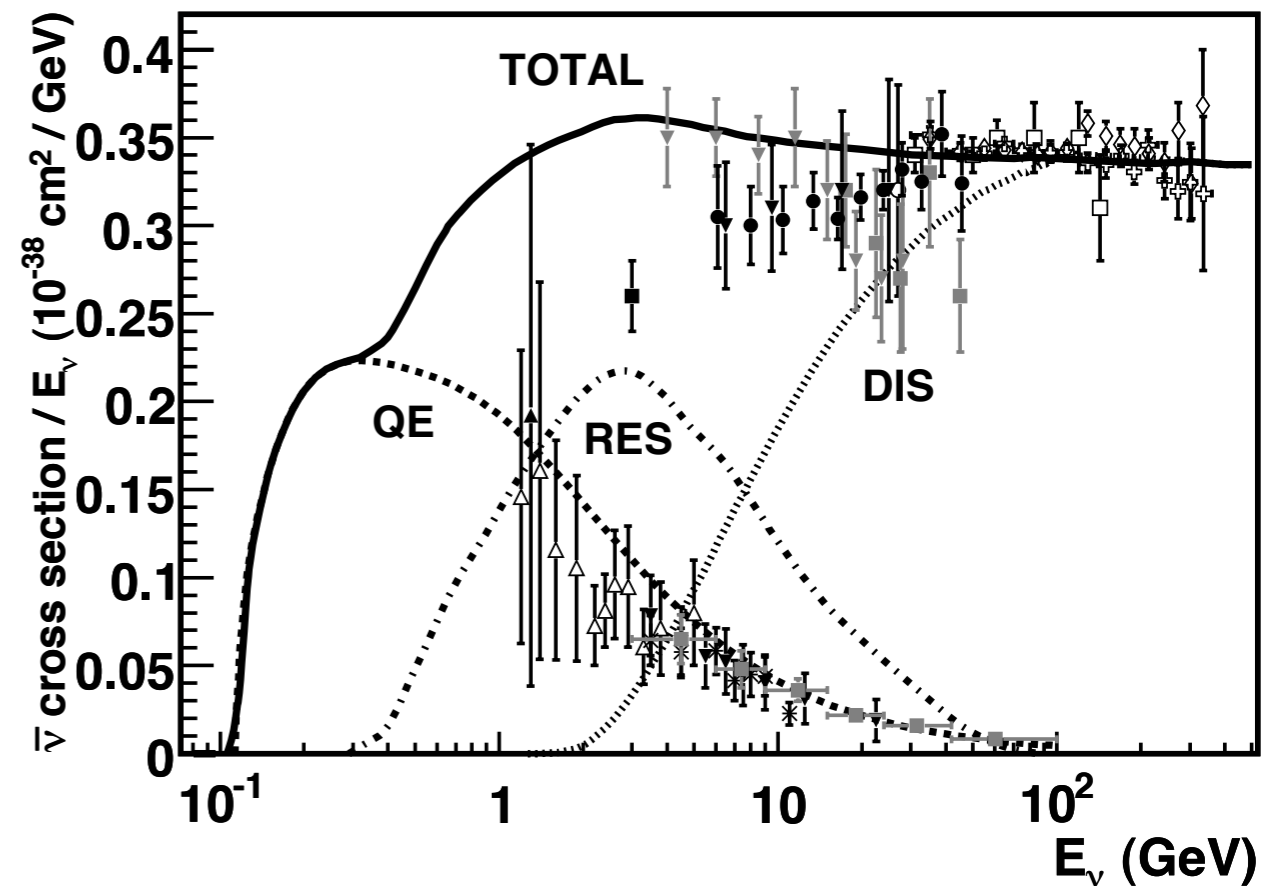
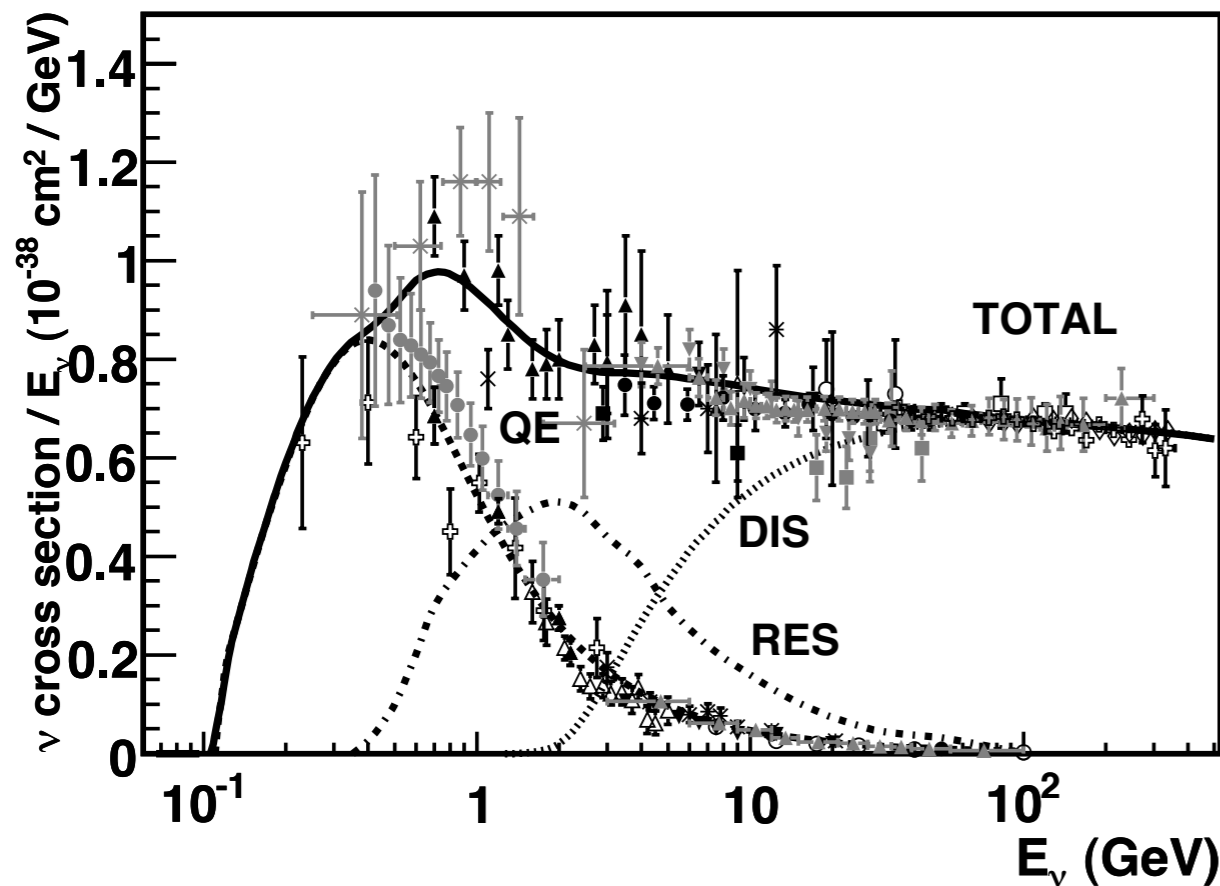


- 1st measurement of axial form factor on “free” protons $\bar{\nu}_\mu p \rightarrow \mu^+ n$

T. Cai et al., MINERvA Collaboration, Nature (2023), 614, 48-53

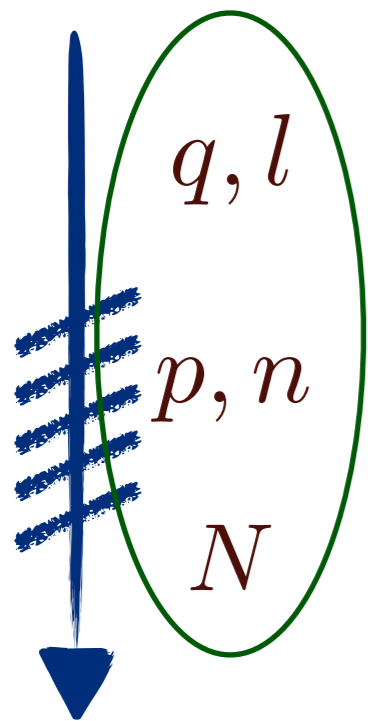
Neutrino-nucleus scattering

- NC scattering across all energies \rightarrow neutrino floor
- CC with electron flavor for supernova, solar, and reactor neutrinos
- same open channels as at nucleon level



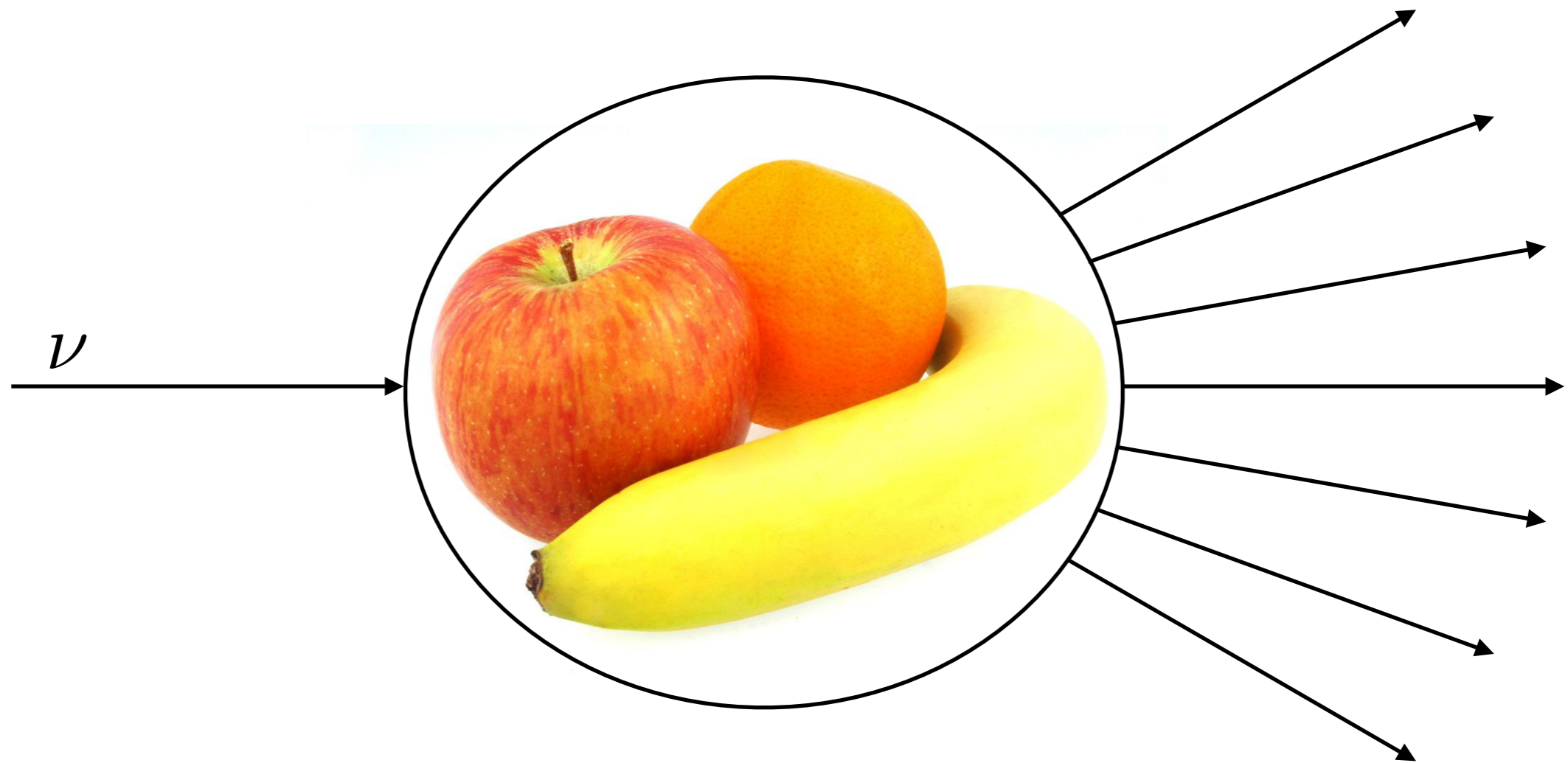
Formaggio and Zeller (2013)

- binding effects, Fermi motion, Pauli blocking
- meson exchange, 2p-2h, final-state interaction

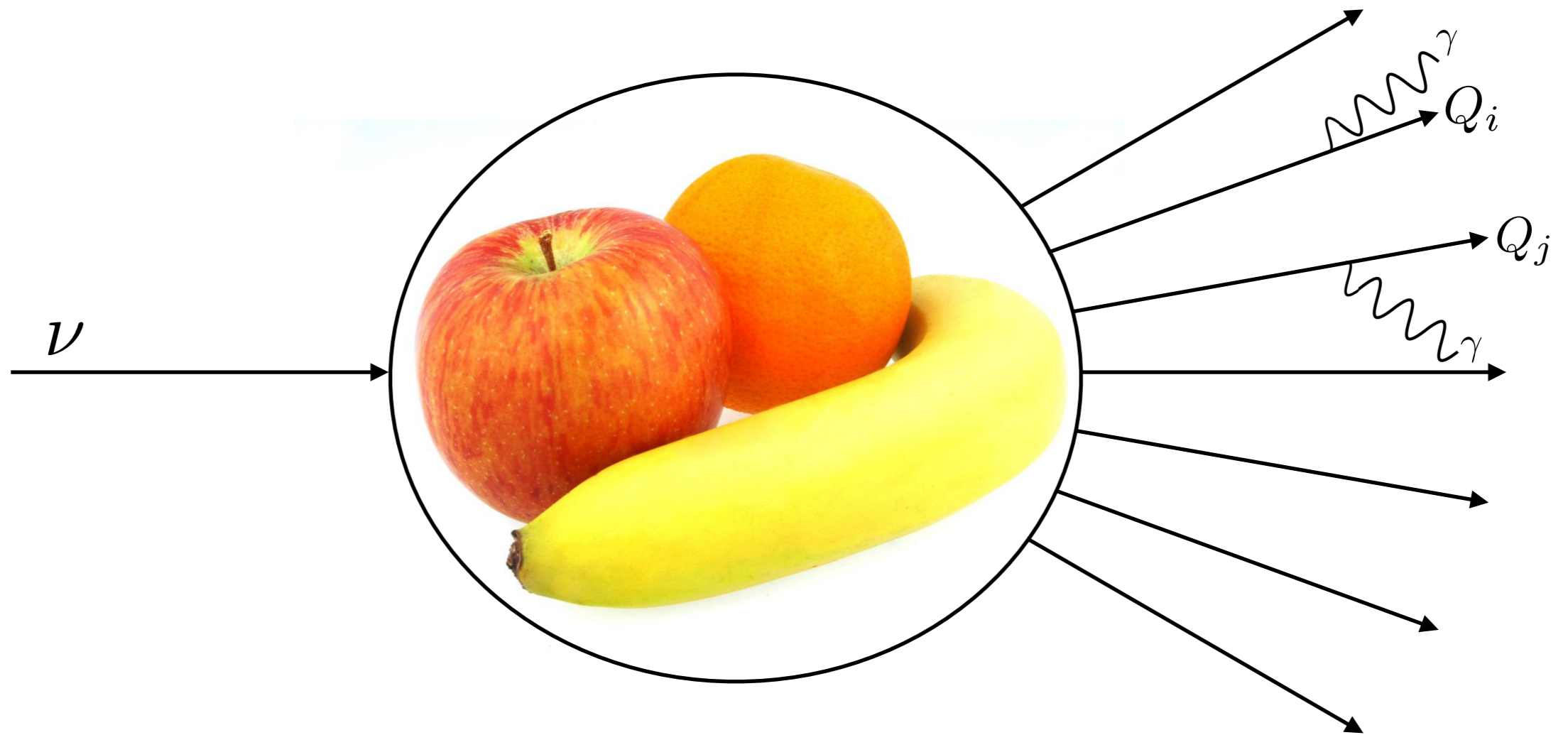


Radiative corrections
in neutrino physics
(at MeV-GeV energies)

Neutrino interactions

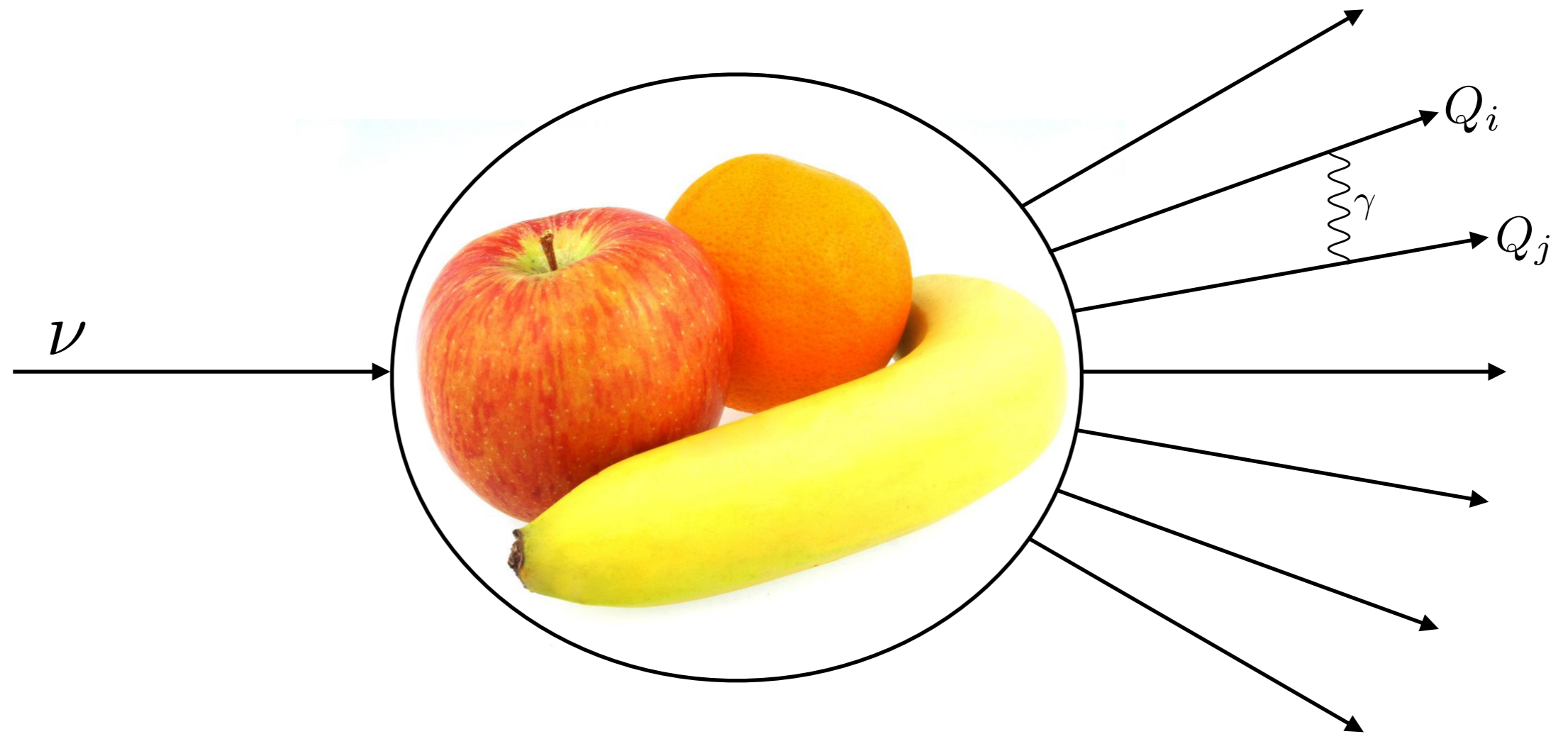


QED corrections



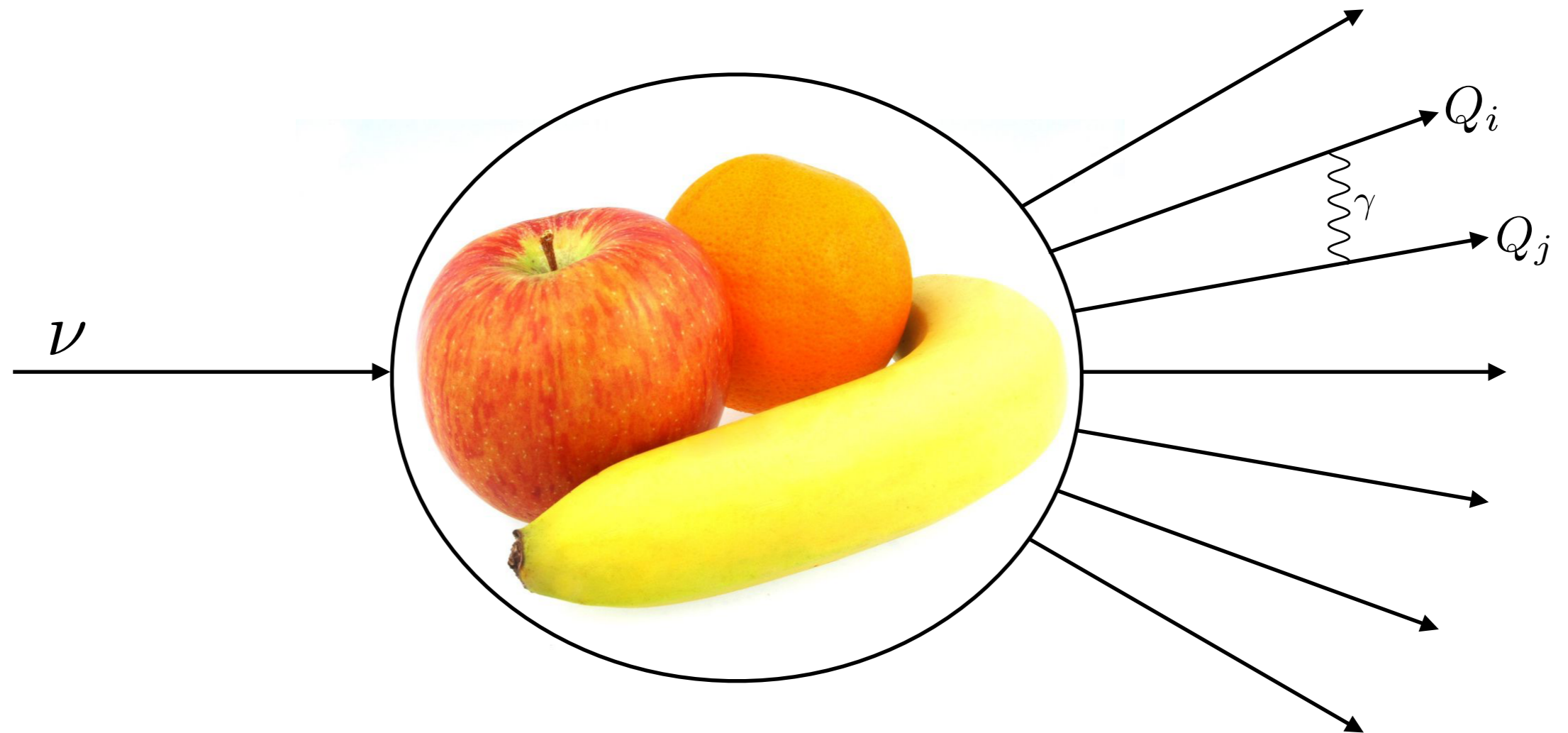
- all charged particles couple to real and virtual photons

QED corrections



- all charged particles couple to real and virtual photons

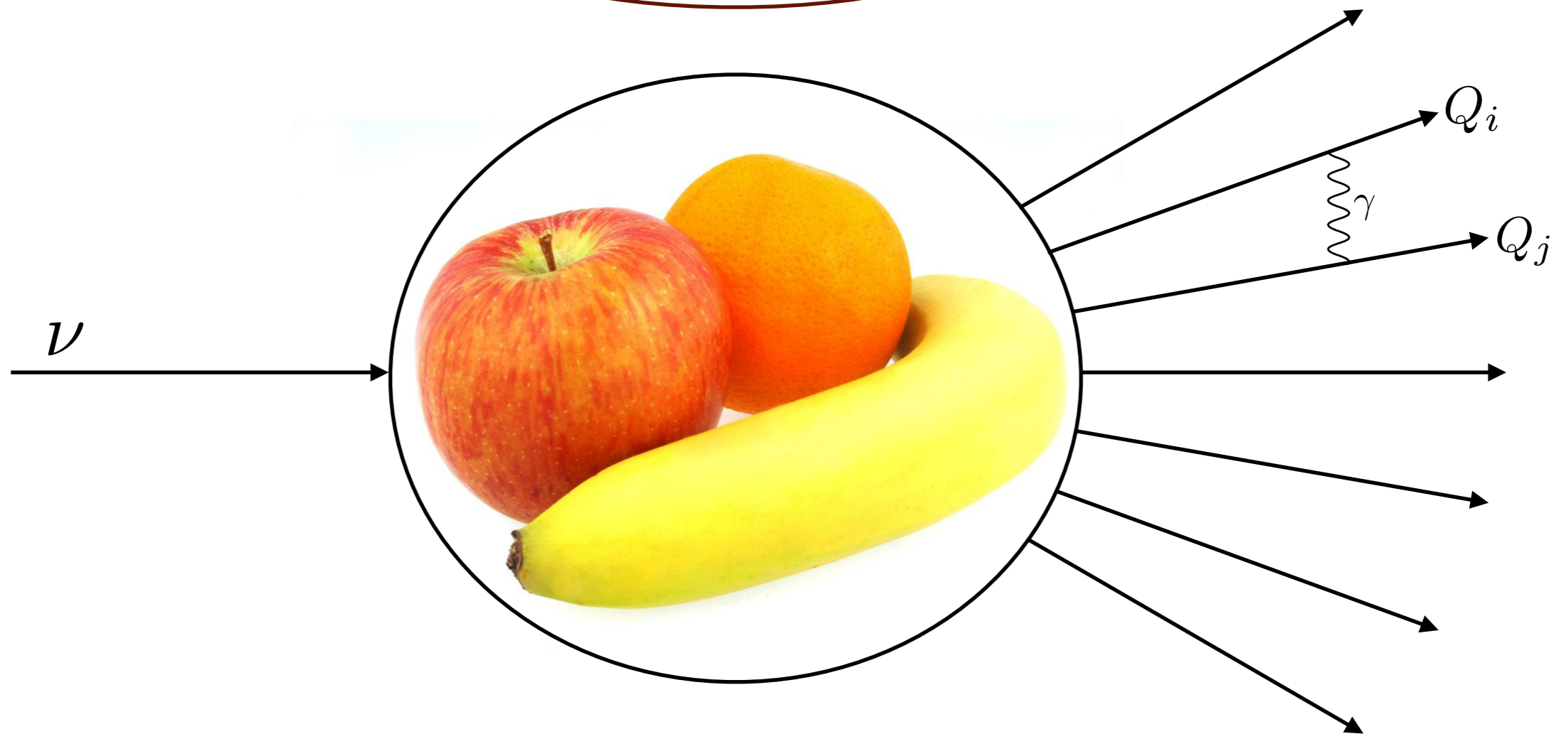
QED corrections



- $\frac{\alpha}{\pi} \sim 0.2\%$ suppression by electromagnetic coupling constant

QED corrections

$$m_e \ll m_\mu \ll E_\nu$$

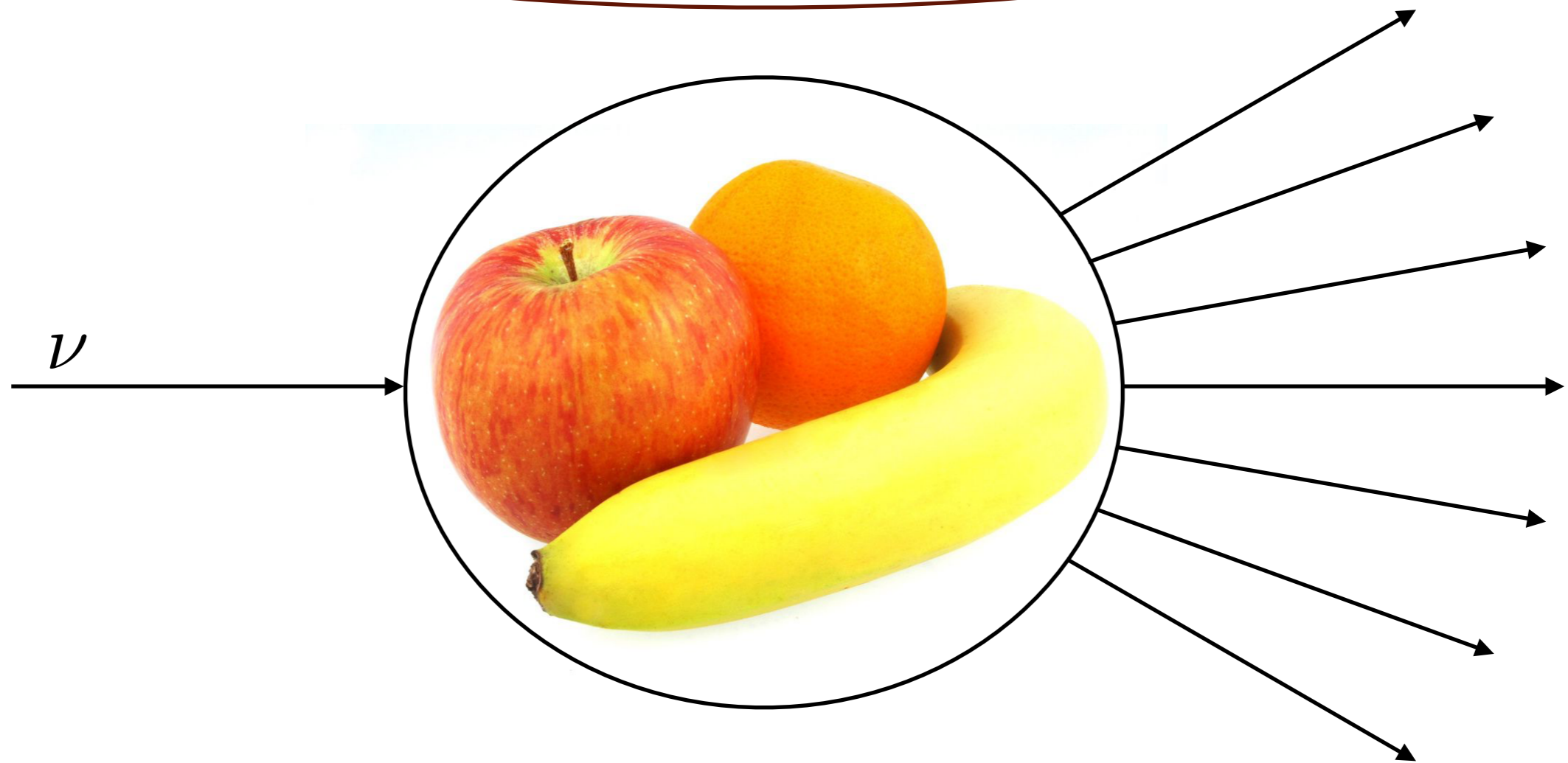


$$\frac{\alpha}{\pi} \sim 0.2 \% \text{ multiplied by } \ln \frac{E_\nu}{m_e} \sim 6 - 10 \text{ or } \ln^2 \frac{E_\nu}{m_e} \sim 36 - 100$$

- scale separation introduces large flavor-dependent QED logarithms

Electroweak corrections

$$m_e, m_\mu, M, E_\nu \ll M_W, M_Z, m_t, m_H$$



$$\frac{\alpha}{\pi} \sim 0.2 \% \text{ multiplied by } \frac{1}{\sin^2 \theta_W}, \ln \frac{M_Z}{M}, \ln \frac{M_t}{M}, \dots$$

- electroweak corrections can be included in low-energy interactions

couplings of **effective Lagrangian** are precisely determined

$$\mathcal{L}_{\text{eff}}^{\text{NC}} = -\bar{\nu}_l \gamma_\mu P_L \nu_l \cdot \bar{f} \gamma^\mu (c_L^{\nu_l f} P_L + c_R^{\nu_l f} P_R) f$$

$$\mathcal{L}_{\text{eff}}^{\text{CC}} = -2\sqrt{2}G_F \sum_{l \neq l'} \bar{\nu}_{l'} \gamma^\mu P_L \nu_l \bar{l} \gamma_\mu P_L l' - c^{qq'} \sum_{q \neq q'} \bar{l} \gamma^\mu P_L \nu_l \bar{q} \gamma_\mu P_L q'$$

Neutrino-lepton, neutrino-quark scattering

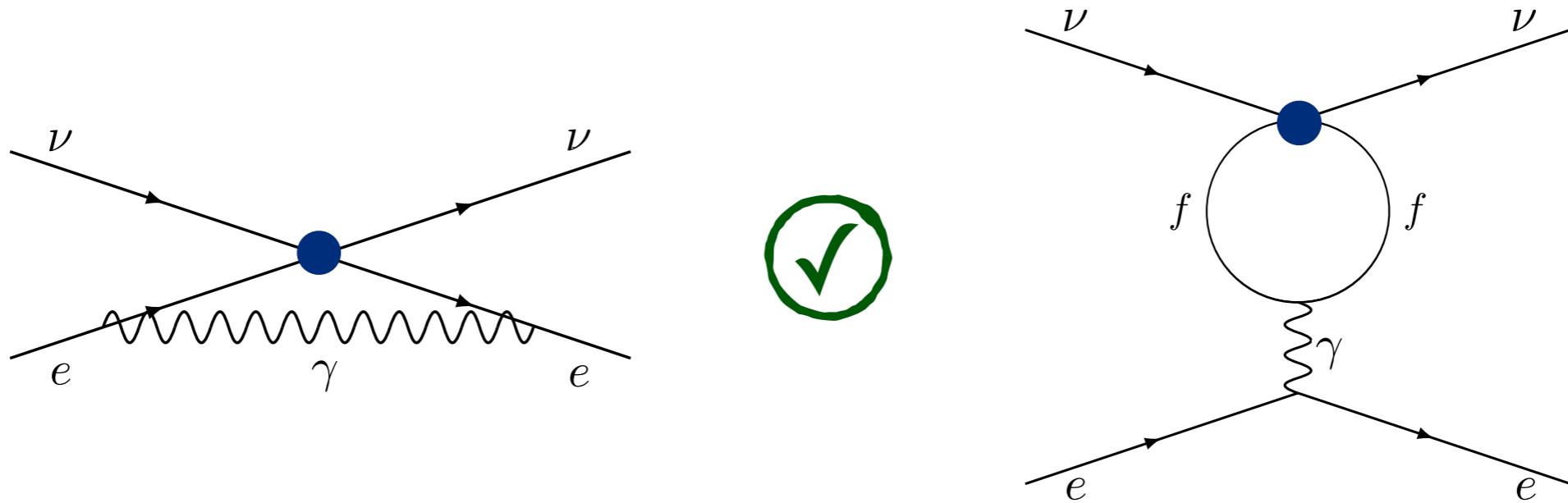
O.T. and Richard J Hill, Phys. Lett. B 805, 3, 135466 (2020)

known at permille level



leading in G_F terms with loop expansion in α , α_s within Standard Model

Leptonic probes: “Standard Candles” for flux constraints

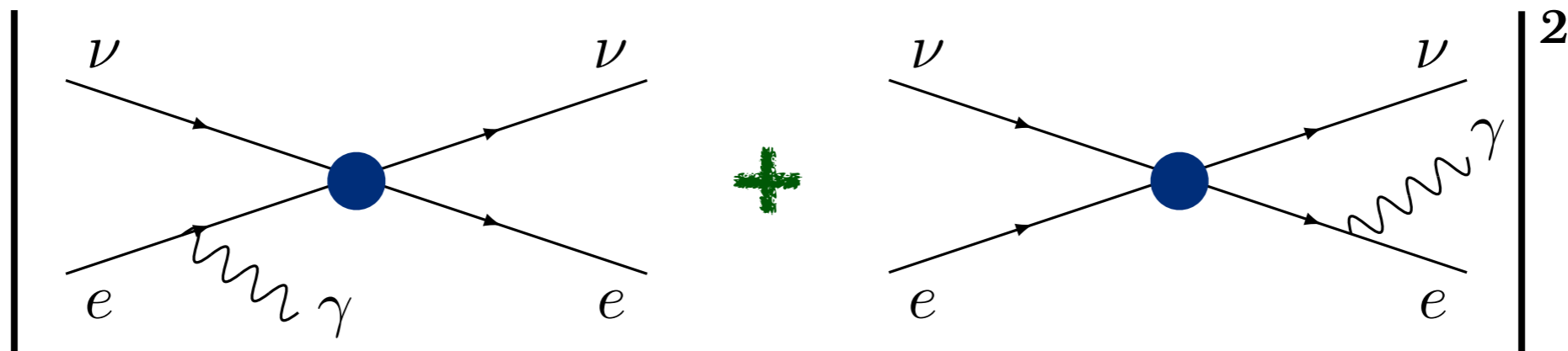


Neutrino-electron scattering

O.T. and Richard J Hill, Phys. Rev. D 101 3, 033006 (2020)

percent-level predictions for MINERvA

known analytically at permille level for NOvA and DUNE, solar ν

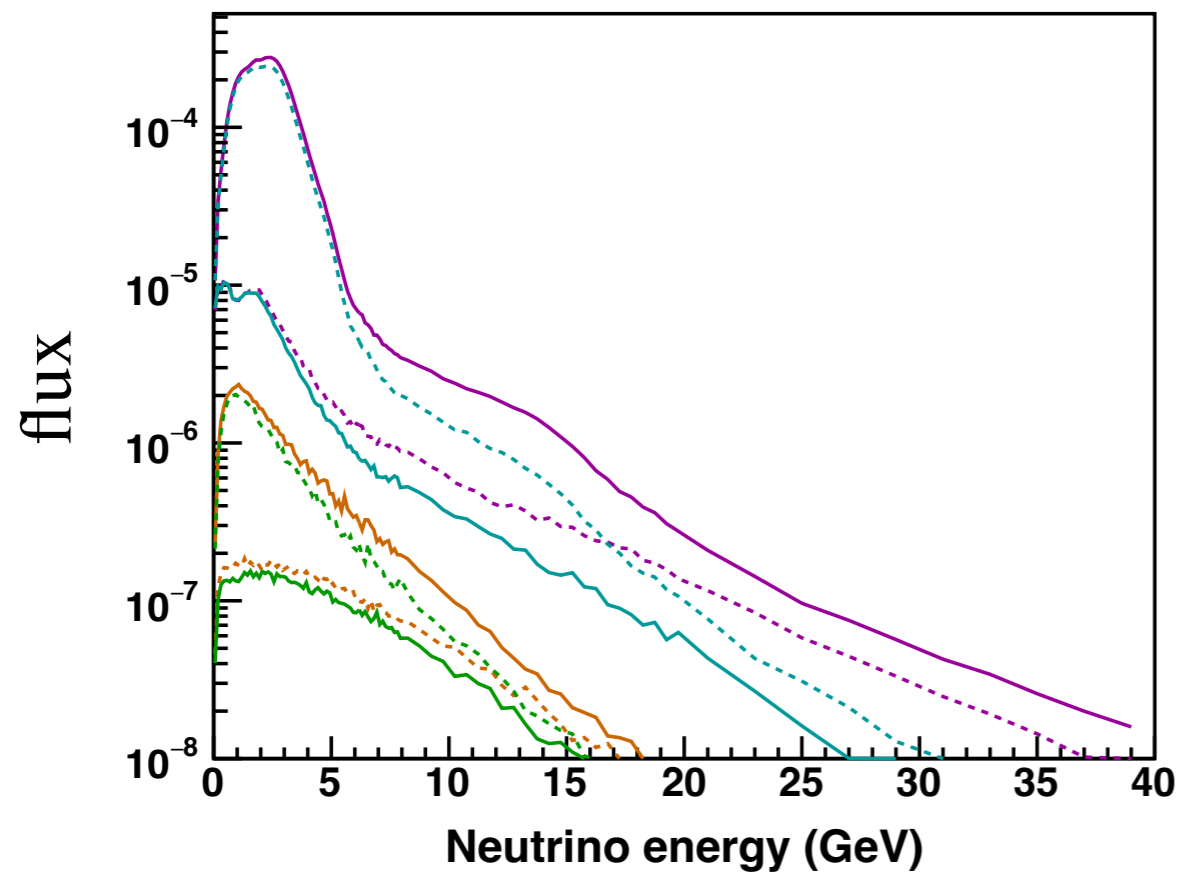


Main theoretical uncertainty

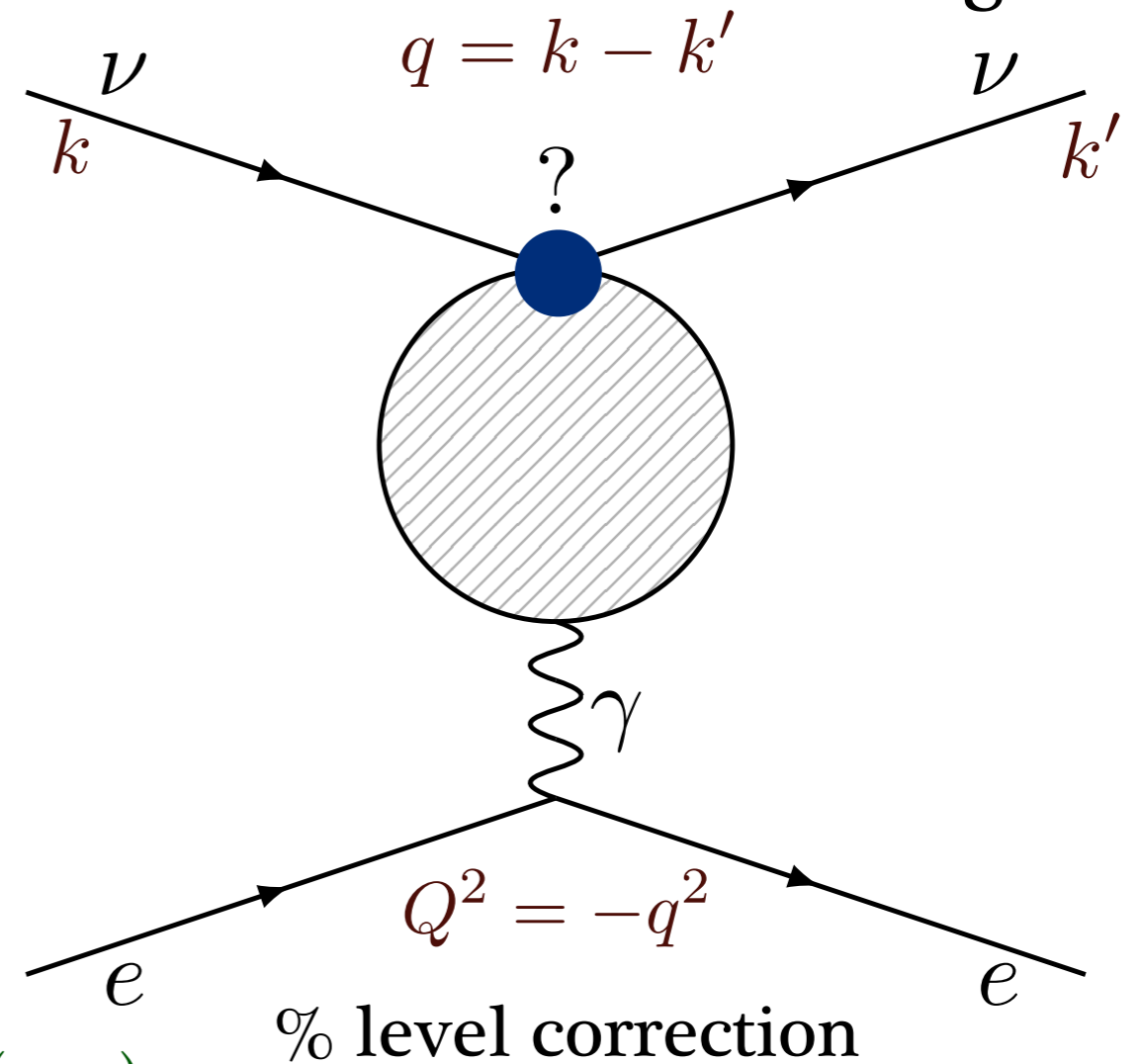
- kinematics is suppressed by electron mass:

$$s, Q^2 \lesssim 2mE_\nu \ll \Lambda_{\text{QCD}}^2$$

- description in terms of quarks is invalid for GeV neutrino energies



Ch. Marshall et al, Phys.Rev.D 101 3, 032002 (2020)

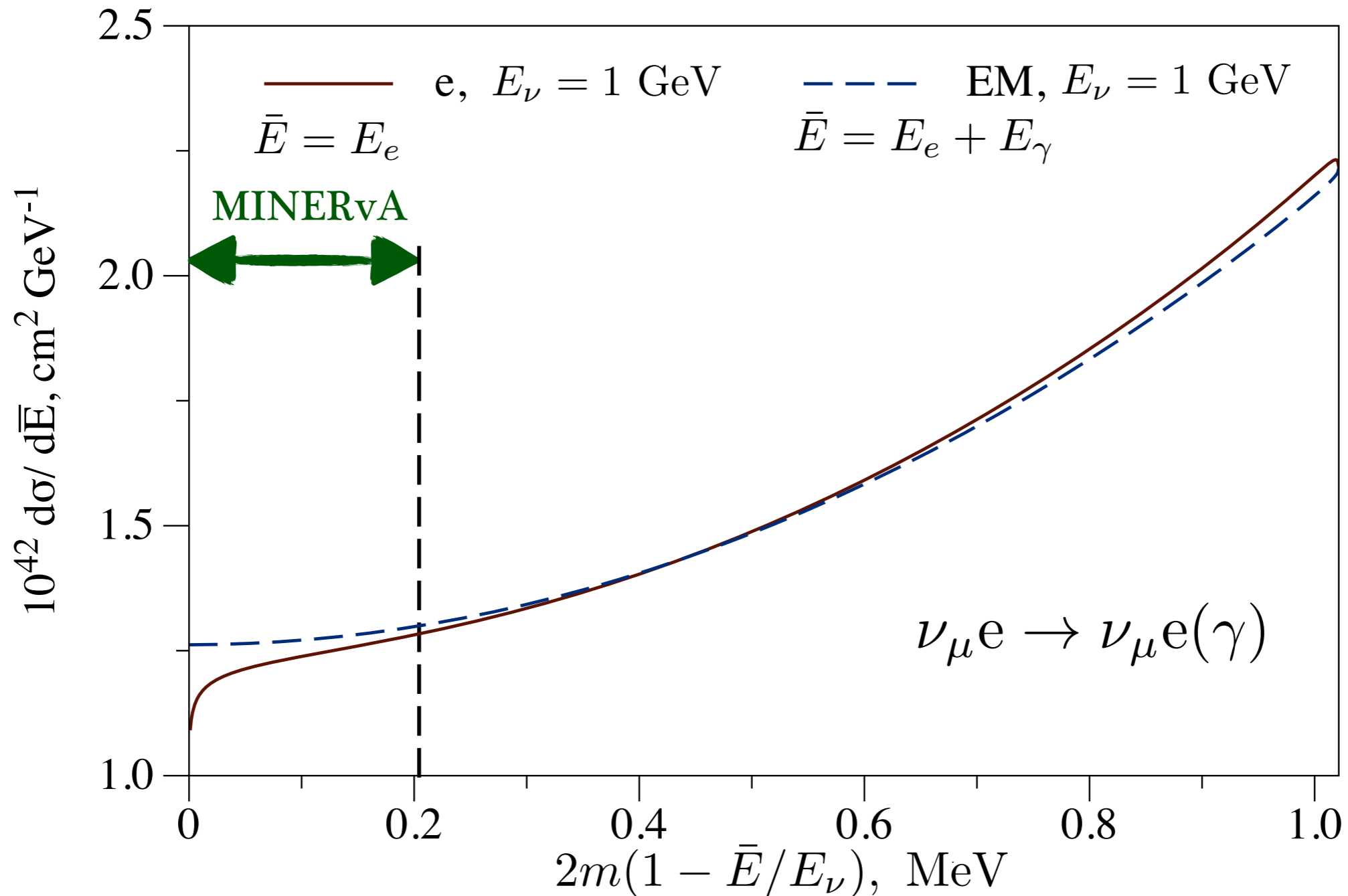


- hadronic correction is the main error in theory

Electron vs electromagnetic (EM) spectra

- resulting spectrum:

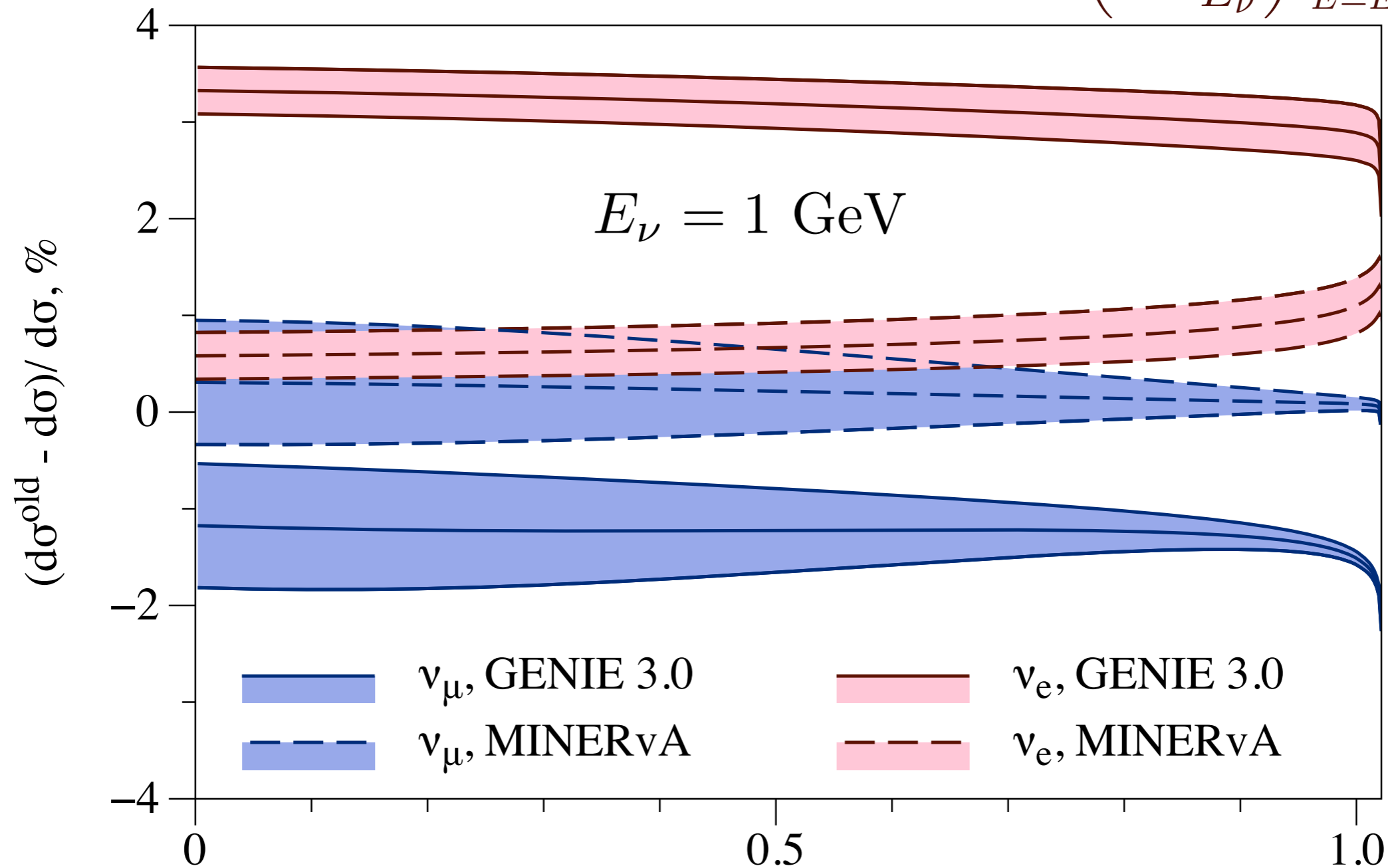
$$2m \left(1 - \frac{\bar{E}}{E_\nu} \right) \Big|_{\bar{E}=E_e} \approx E_e \theta_e^2$$



- cut dependence after radiative corrections

Comparison to GENIE

- electromagnetic energy spectrum: $2m \left(1 - \frac{\bar{E}}{E_\nu} \right) \Big|_{\bar{E}=E_e} \approx E_e \theta_e^2$



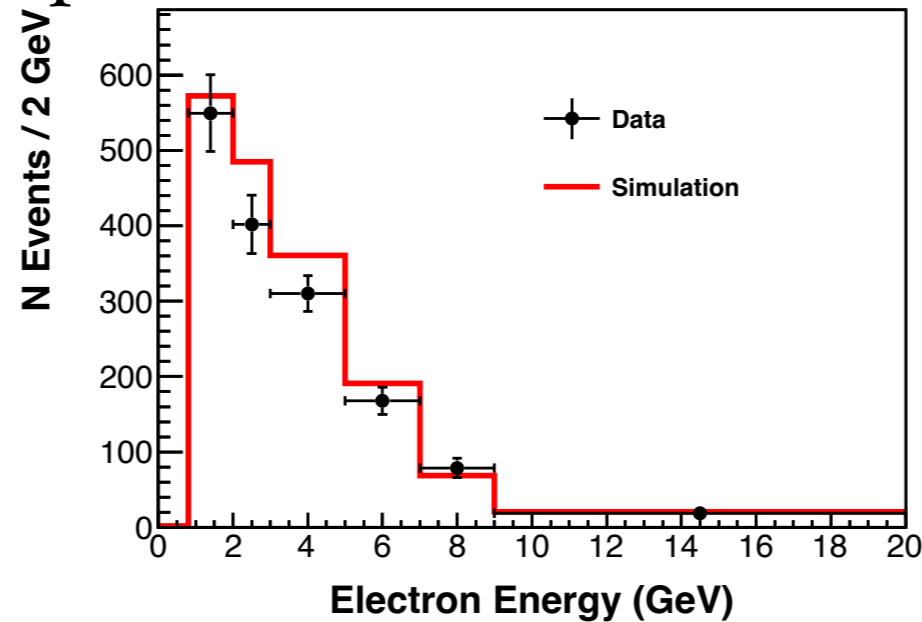
courtesy of Kevin S. McFarland

- correct description and definite improvement at GeV energies

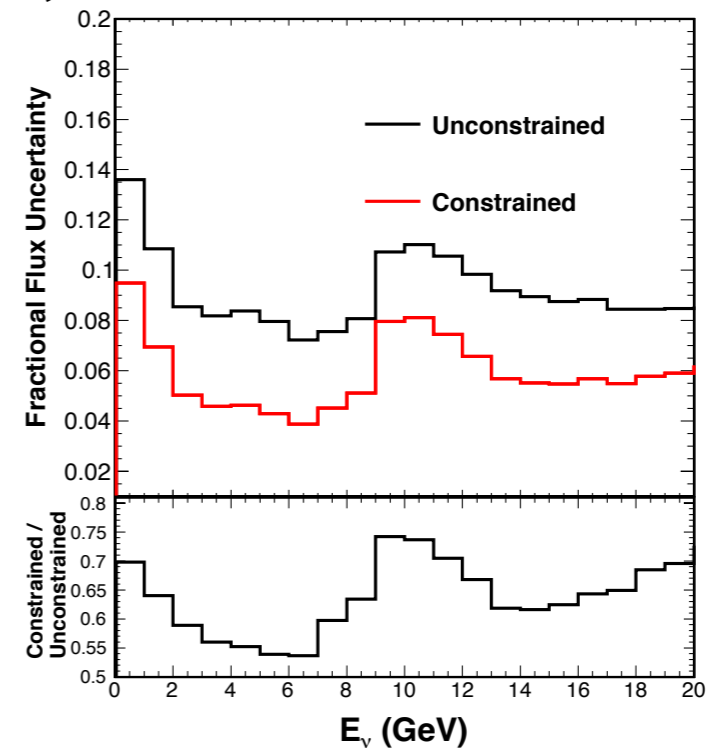
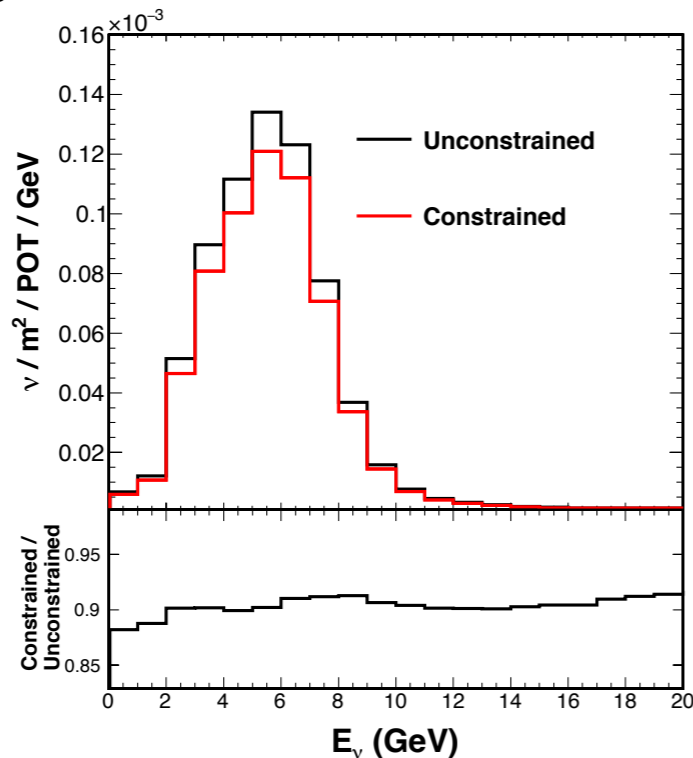
MINERvA constraint

- electron energy spectrum:

MINERvA, Phys.Rev.D 100 9, 092001 (2019)



- 10% correction on flux normalization, reduced error



- successful implementation by MINERvA collaboration

Neutrino-electron scattering at Fermilab

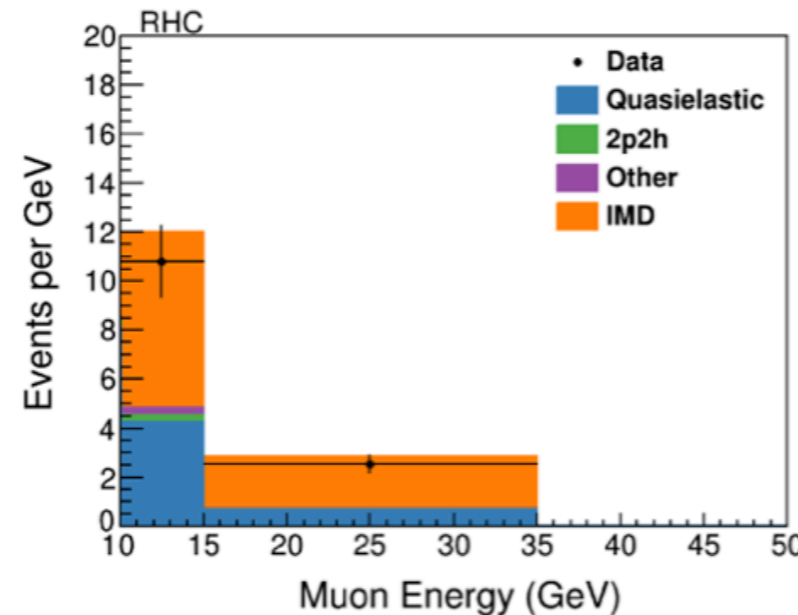
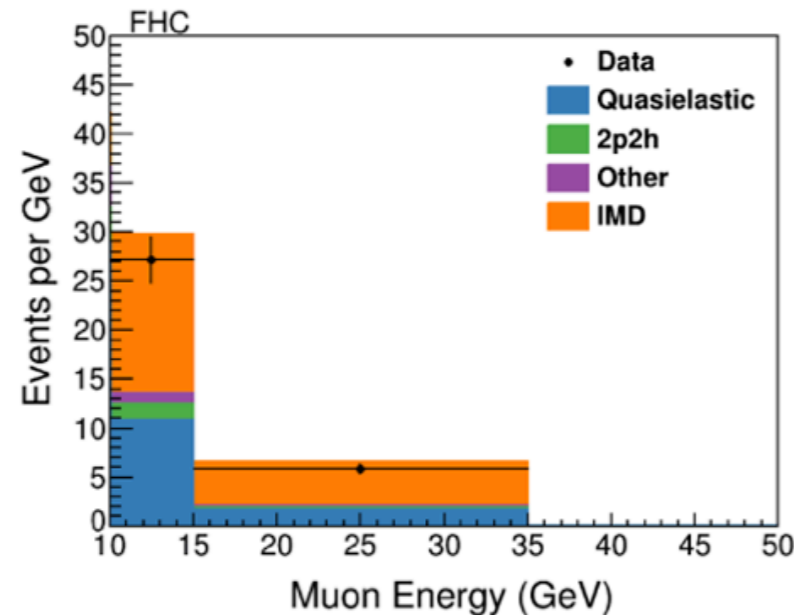
- **MINERvA** experiment: measure neutrino-nucleus cross sections
- flux constraints via scattering on atomic electrons: 7.5% to 4%
MINERvA, Phys. Rev. D 93, 112007 (2016), Phys.Rev.D 100 9, 092001 (2019)
- cross section scales as target mass m
 10^{-4} - 10^{-3} of cross section on nucleons and nuclei
- unique process **free from structure effects**
- huge statistics of DUNE near detector vs MINERvA: 8% to 2%
5000-7000 events in a year vs 1100-1200 events in total
Ch. Marshall et al, Phys.Rev.D 101 3, 032002 (2020)

- νe scattering: standard candle to constrain neutrino flux

MINERvA constraint by inverse muon decay

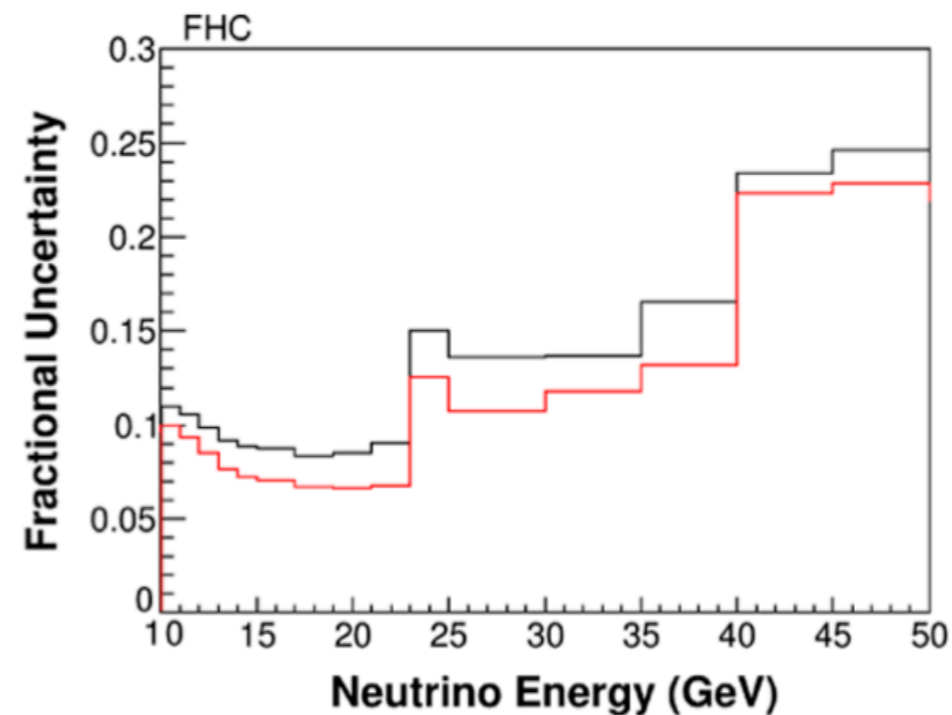
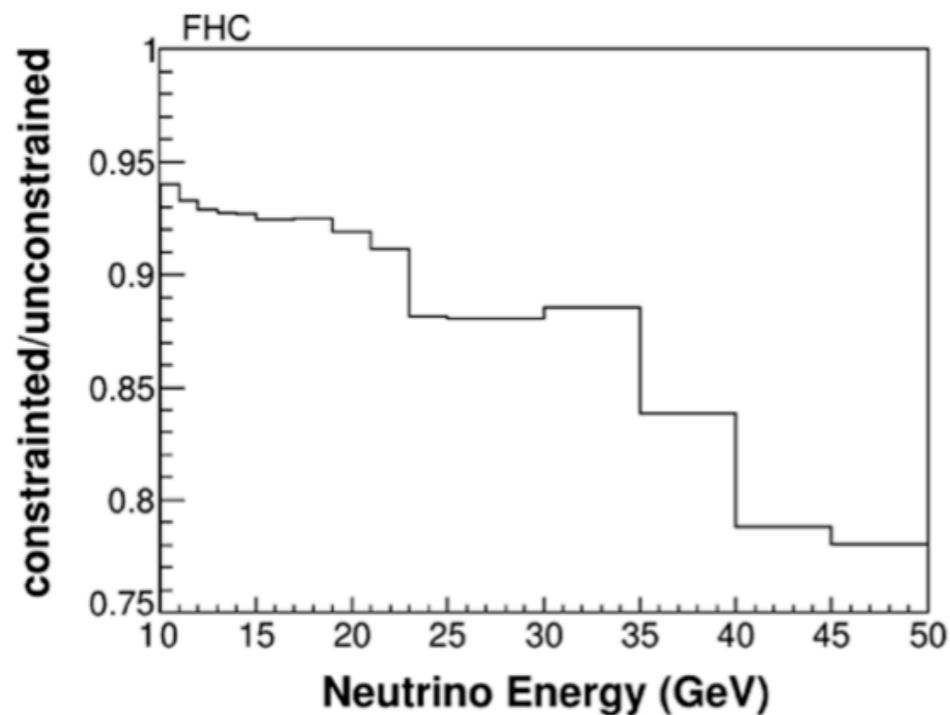
MINERvA, Phys.Rev.D 104, 092010 (2021)

- muon energy spectrum:



$$E_{\nu}^{\text{thr}} \gtrsim 10.9 \text{ GeV}$$

- 10-20% correction on flux normalization, reduced error



- successful implementation by MINERvA collaboration

Inverse muon decay theory

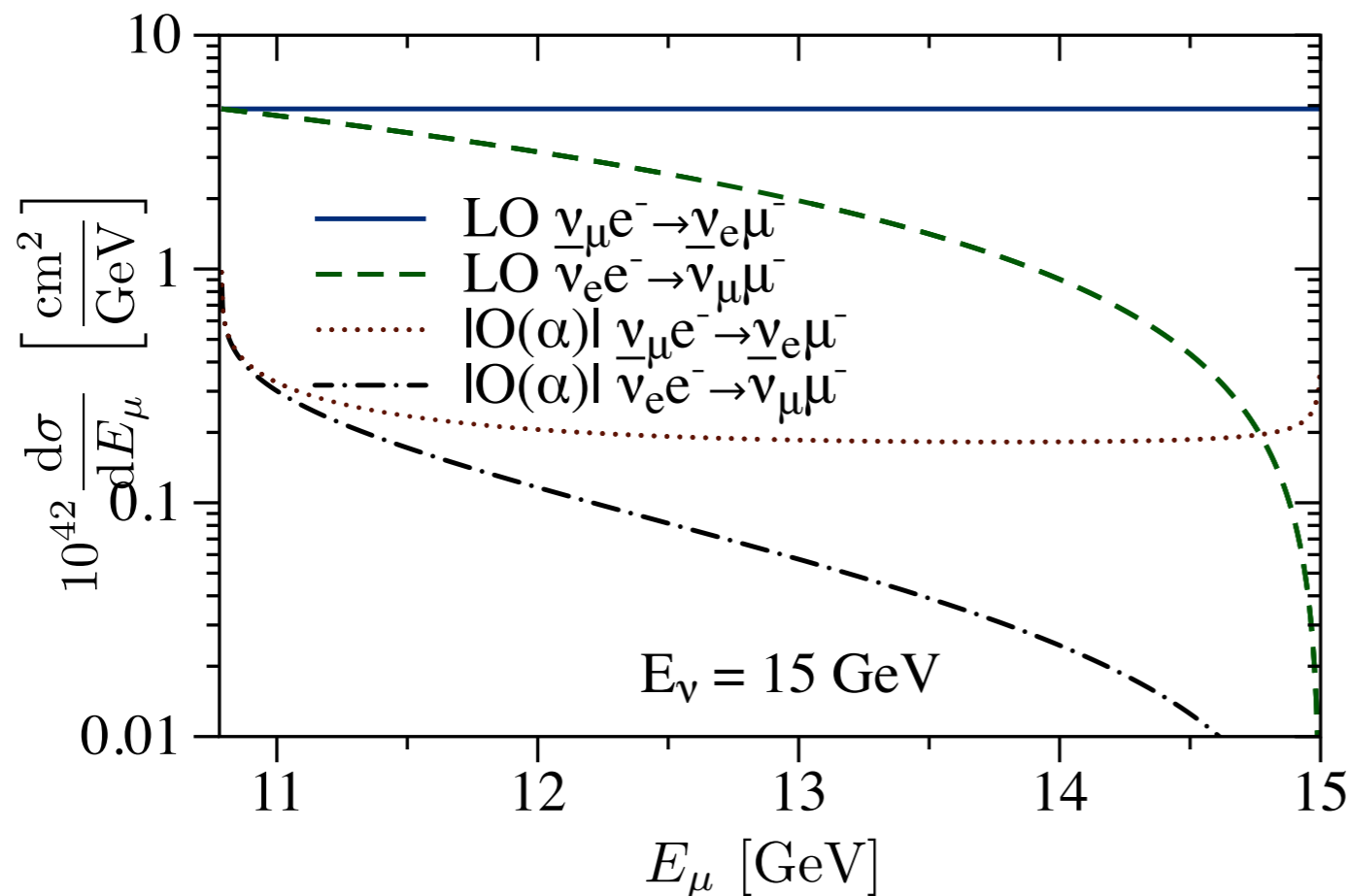
- precise Lagrangian with G_F from muon decay

$$\mathcal{L}_{\text{eff}} = -2\sqrt{2}G_F\bar{\nu}_e\gamma^\lambda P_L\nu_\mu\bar{\mu}\gamma_\lambda P_L e + \text{h.c.}$$

- 2.5 from 3 cross sections reproduced by alternative method

Bardin and Dokuchaeva (1987)

- **new** total cross sections, energy spectra, and 2D cross sections



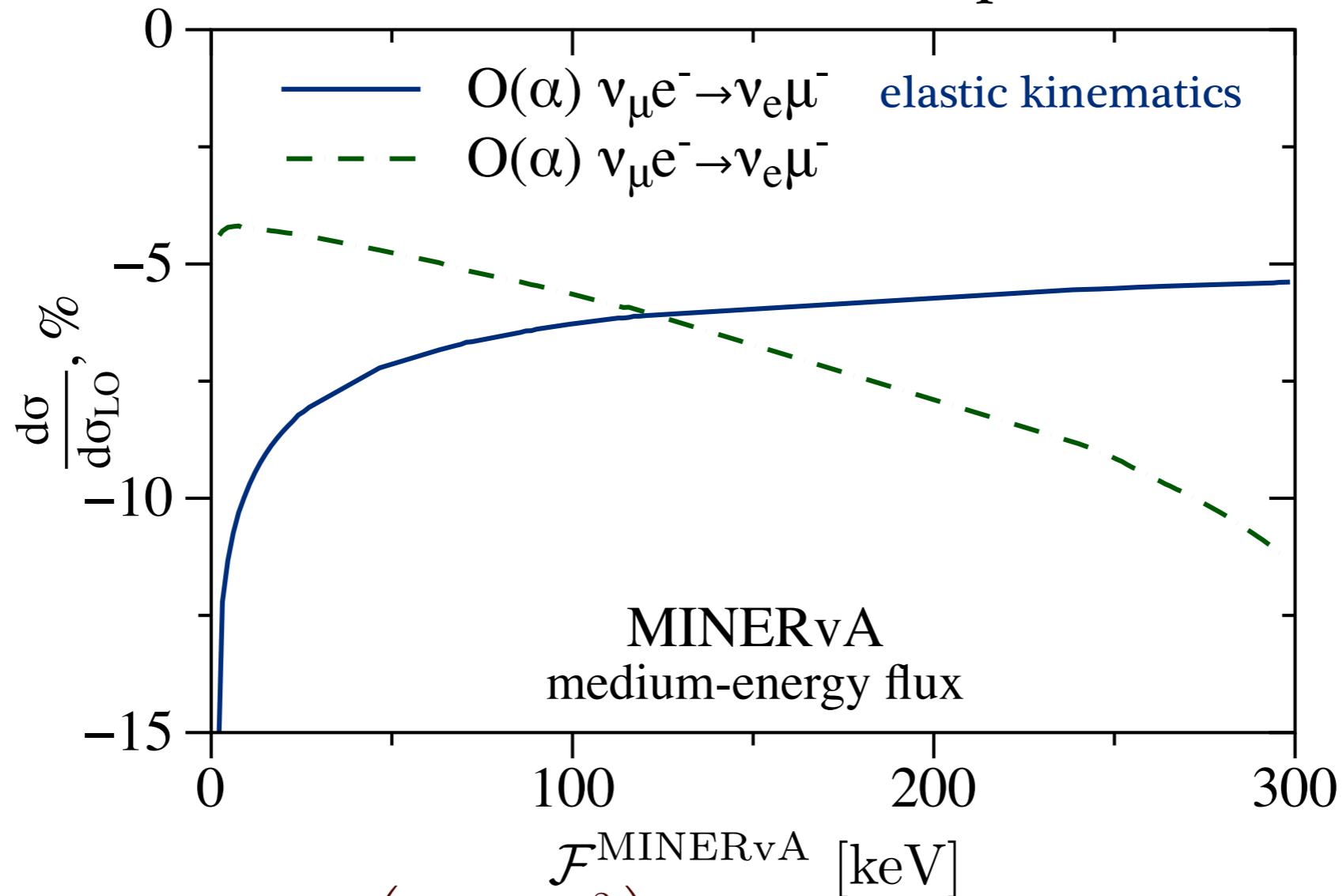
dominant neutrino component
has larger cross section

energy spectrum in
both channels

- muon energy spectrum verified $\nu_\mu e^- \rightarrow \nu_e \mu^-$, derived $\bar{\nu}_e e^- \rightarrow \bar{\nu}_\mu \mu^-$

Inverse muon decay theory

- radiative corrections to distribution of experimental discriminant



$$\mathcal{F} = E_\mu \theta_\mu^2 \approx \left(1 - \frac{E_\mu}{E_\nu}\right) \left(2m_e - \frac{m_\mu^2}{E_\mu}\right) \quad \mathcal{F}^{\text{MINERvA}} = \frac{E_\mu \theta_\mu^2}{1 - \frac{E_\mu}{35 \text{ GeV}}}$$

O.T., Kaushik Borah, Richard J. Hill, Kevin S. McFarland, Daniel Ruterbories
Phys. Rev. D 107 9, 093005 (2023)

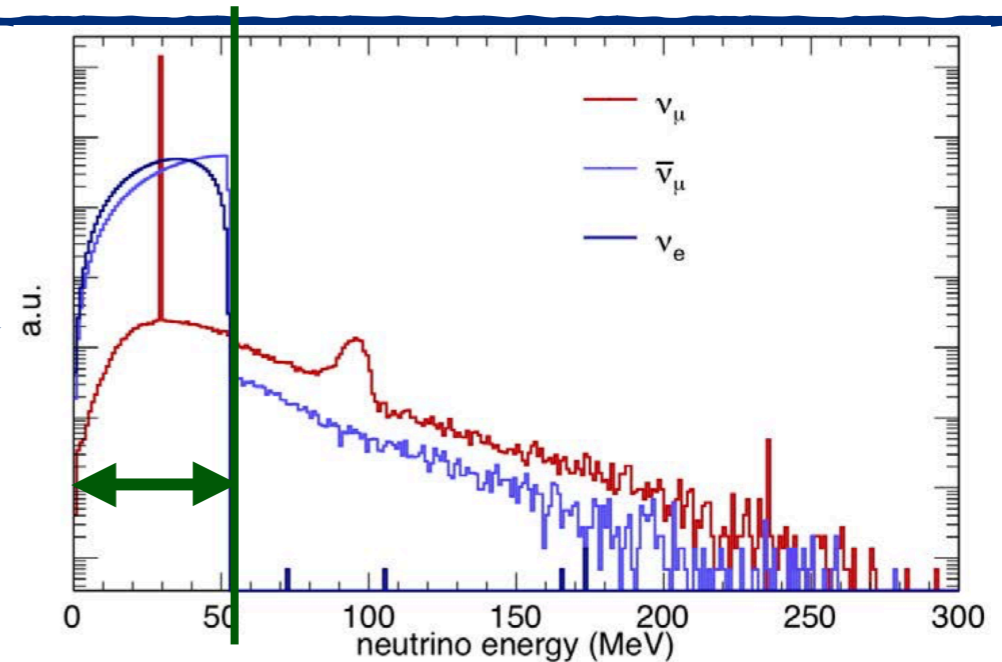
- double-differential distributions and corrections to \mathcal{F} distribution

flavor-dependence at tree-level

energy spectra from π DAR \rightarrow

$$\pi^+ \rightarrow \mu^+ \nu_\mu$$

$$\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu$$



Akimov et al., Science 357 6356, 1123-1126 (2017)

Neutrinos from muon, pion and kaon decays

O. T., Phys. Lett. B 829, 137108 (2022)

$$\pi^+ \rightarrow \mu^+ \nu_\mu \gamma$$

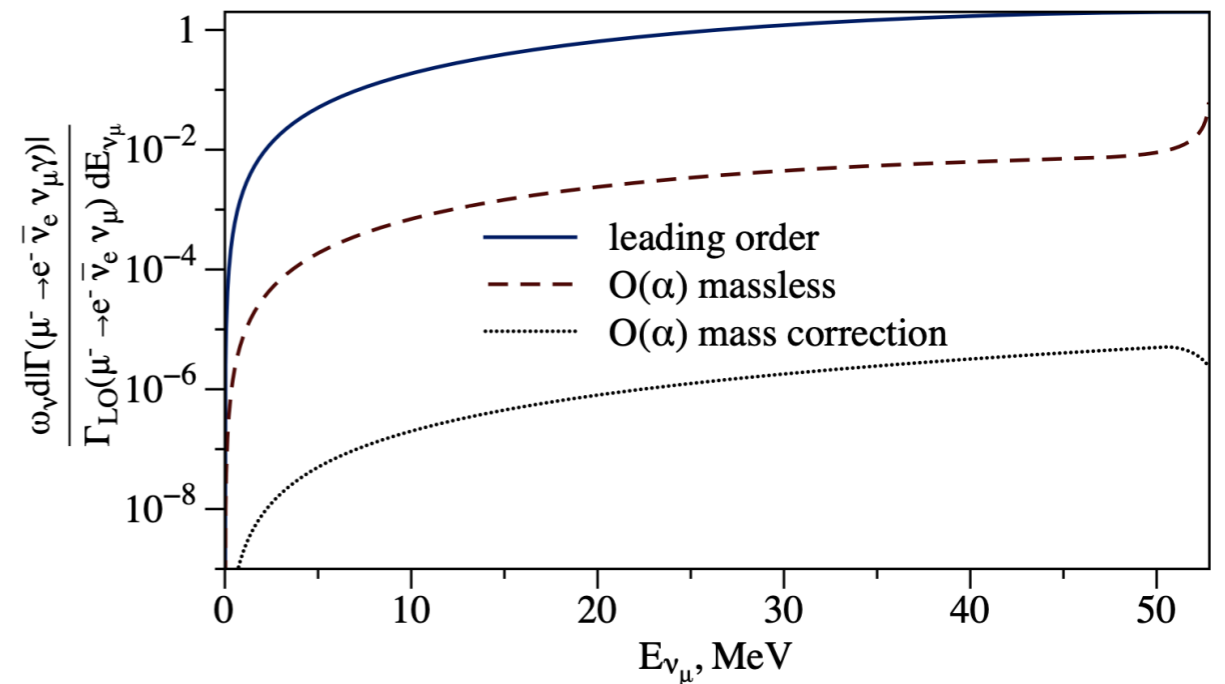
< 0.1 ‰

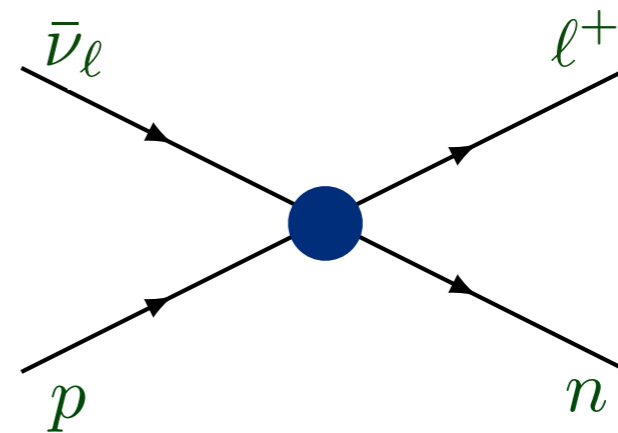
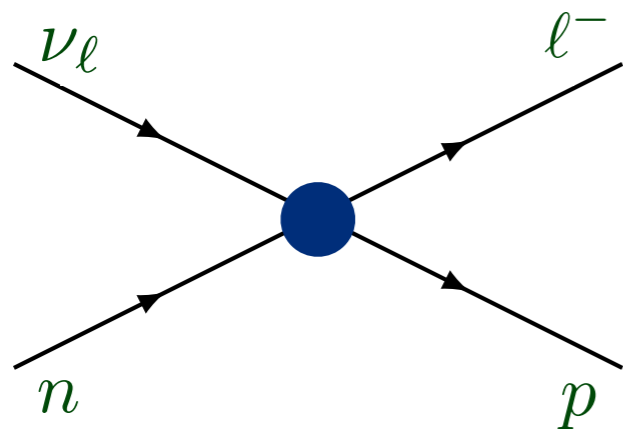
$$K^+ \rightarrow \mu^+ \nu_\mu \gamma$$

flavor-dependence is clarified to permille level analytically



$$\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu \gamma \quad 3-4 \text{ ‰}$$

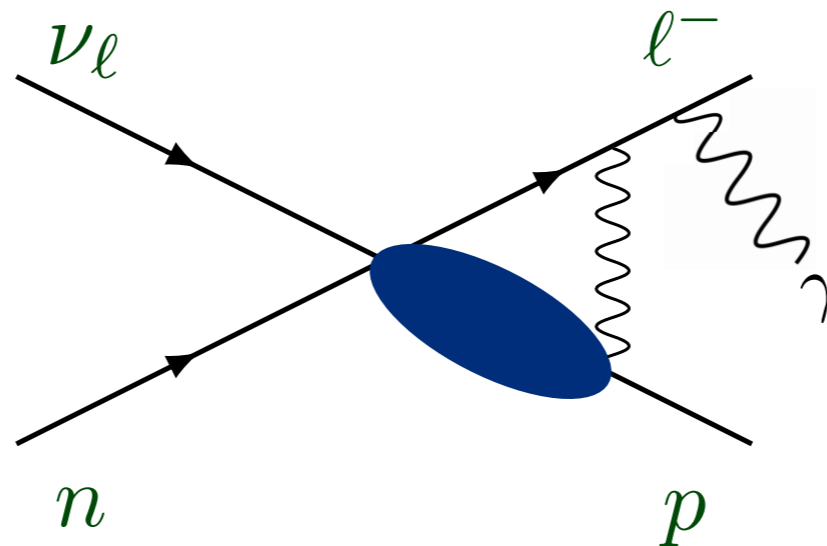




O. T., Qing Chen, Richard J. Hill and Kevin S. McFarland, Nature Commun. 13 (2022), 1, 5286

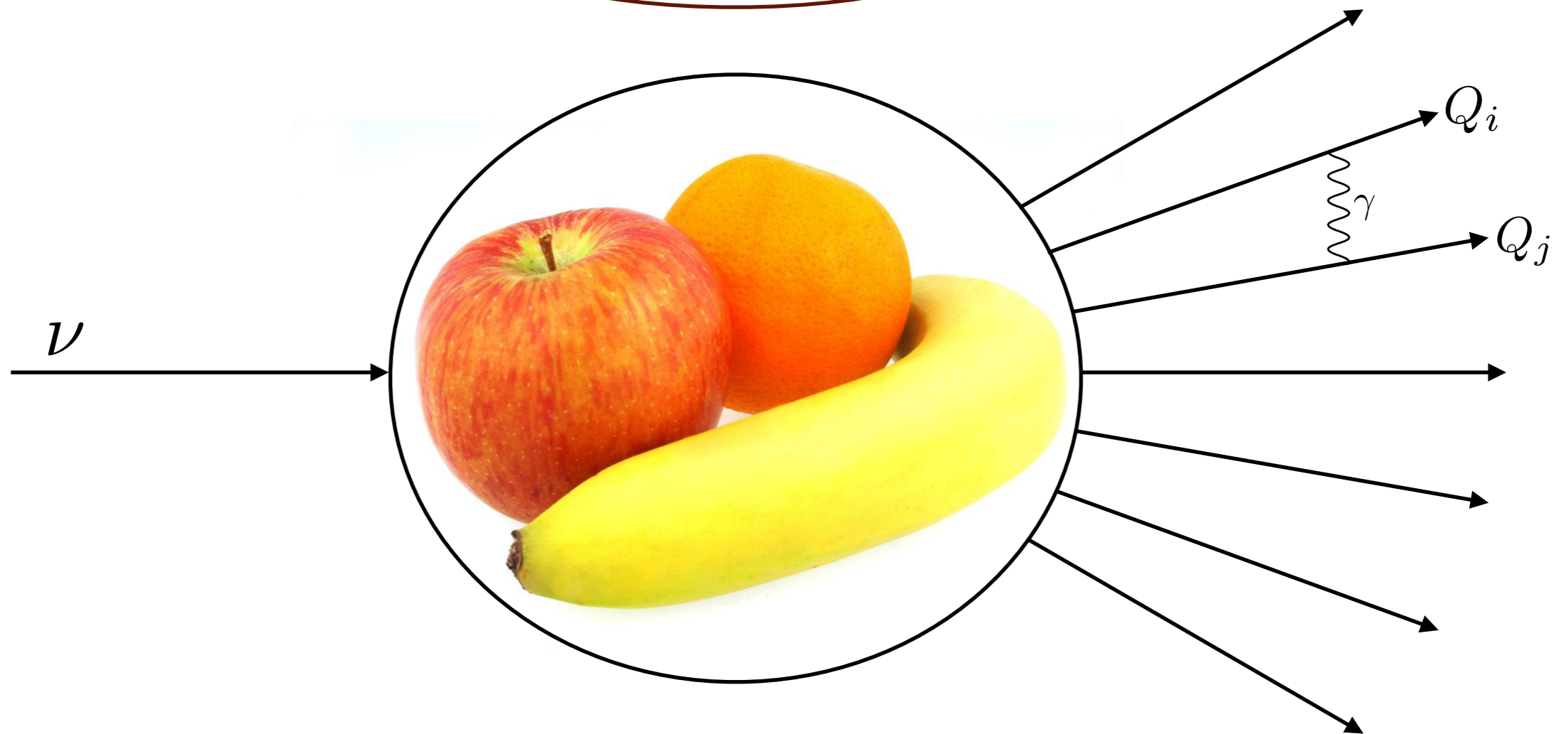
Radiative corrections in charged-current elastic scattering on free nucleons

O. T., Qing Chen, Richard J. Hill, Kevin S. McFarland and Clarence Wret
 editors suggestion in Phys. Rev. D (2022)



QED corrections

$$m_e \ll m_\mu \ll E_\nu$$



$$\frac{\alpha}{\pi} \sim 0.2 \% \text{ multiplied by } \ln \frac{E_\nu}{m_e} \sim 6 - 10 \text{ or } \ln^2 \frac{E_\nu}{m_e} \sim 36 - 100$$

- scale separation introduces large flavor-dependent QED logarithms

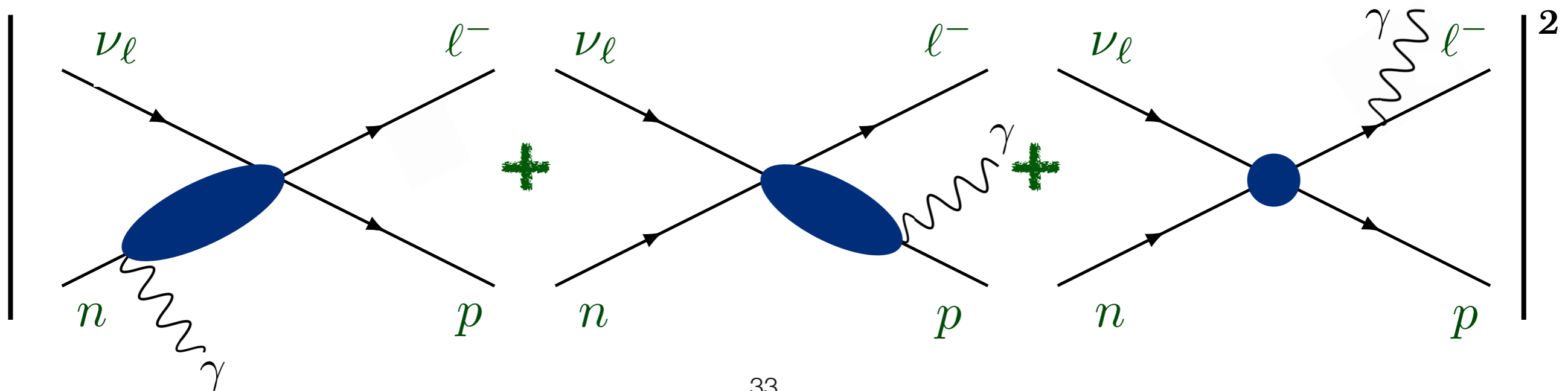
factorization for radiative corrections with model for hard function



Charged-current elastic scattering on nucleons

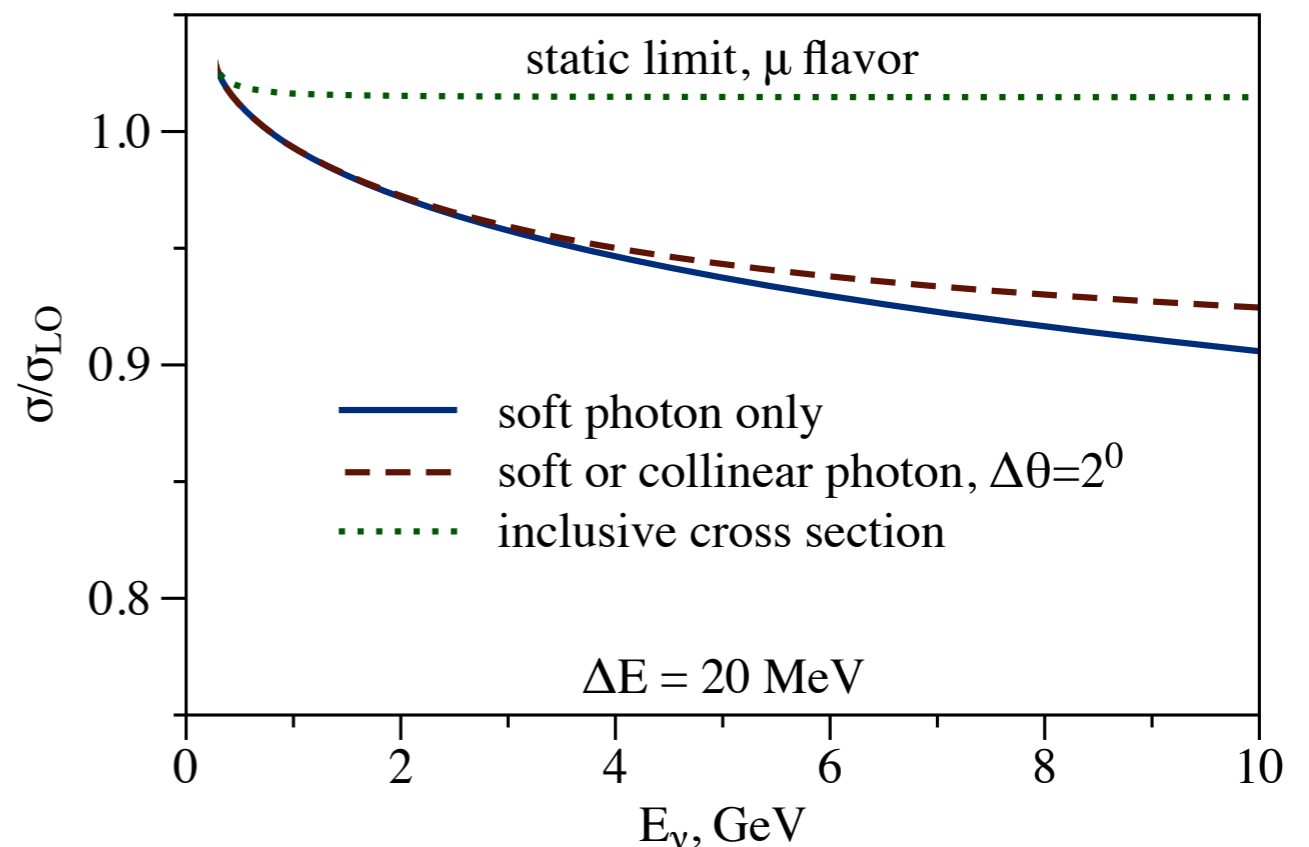
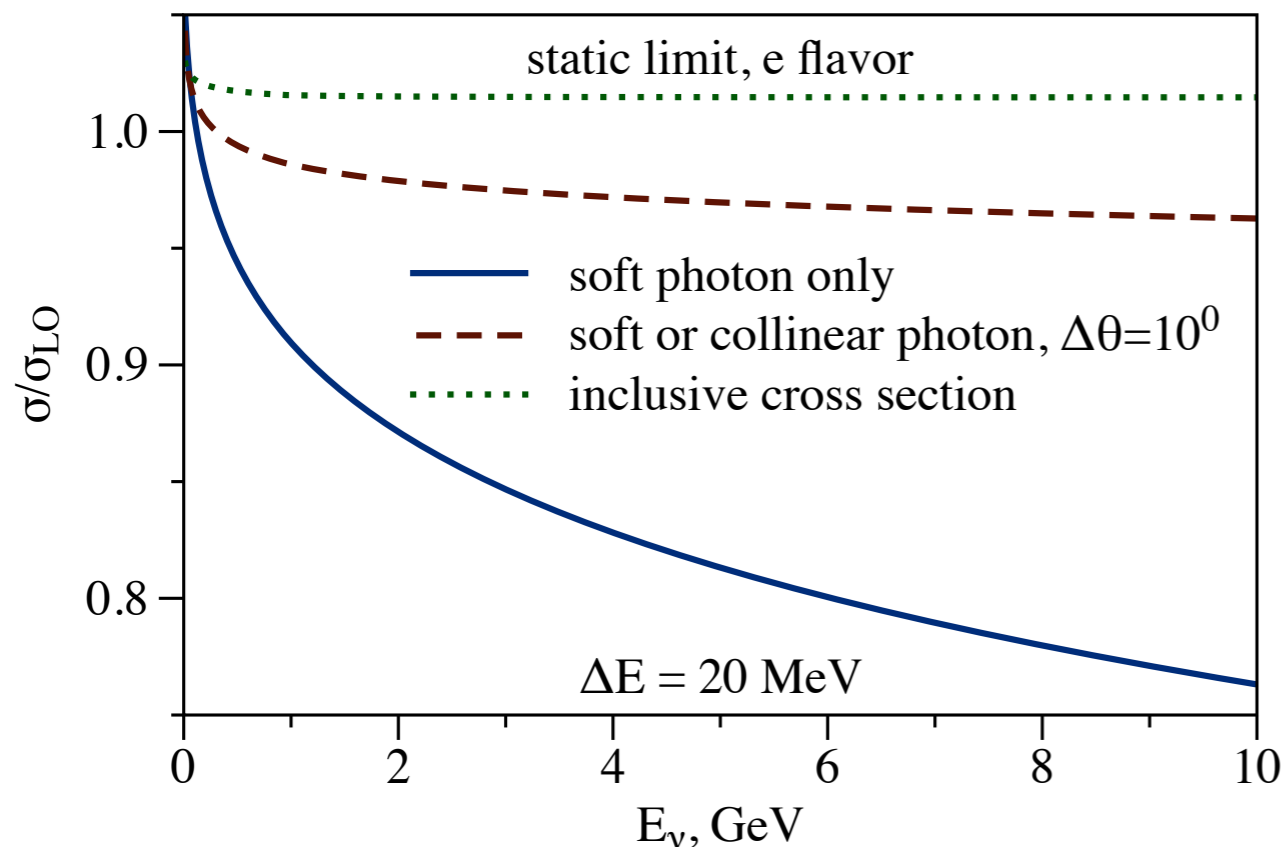
precise predictions for flavor ratios and radiative corrections

in exclusive and inclusive observables with GeV neutrino beams



Static nucleon limit

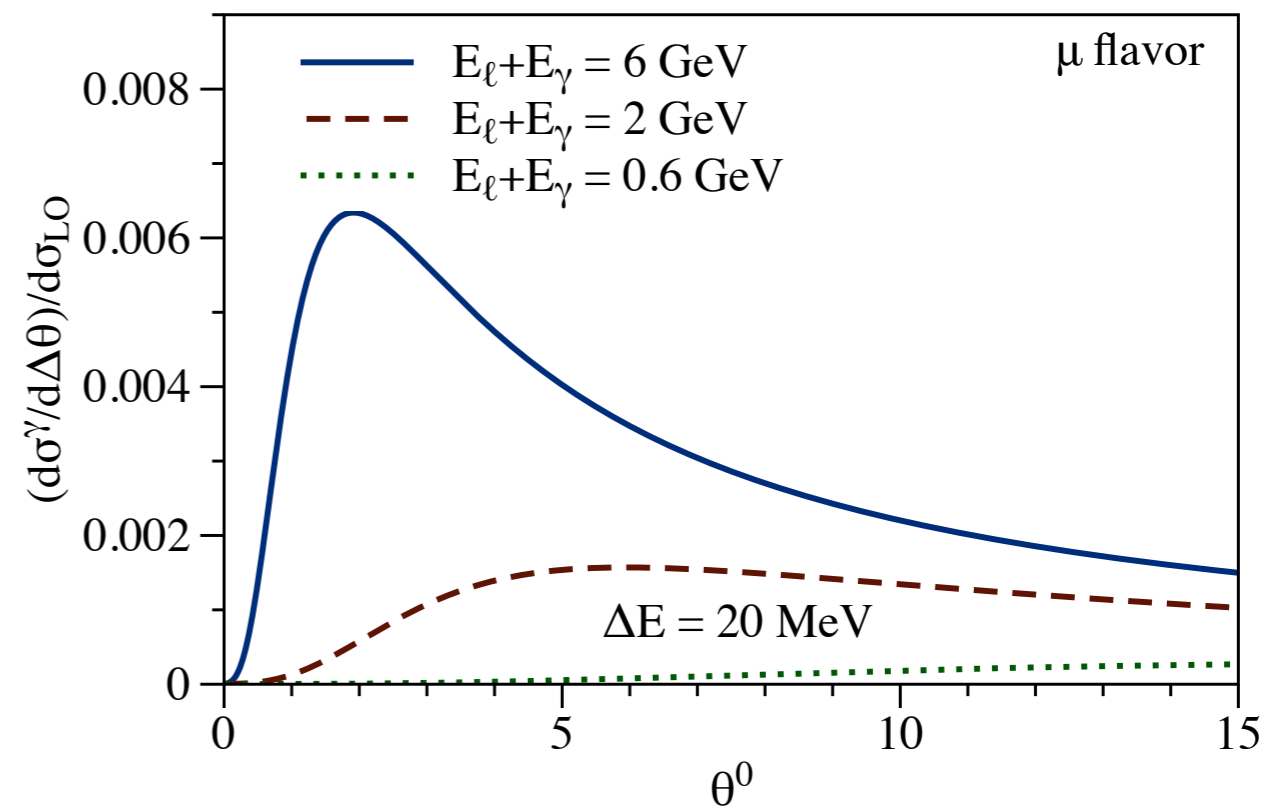
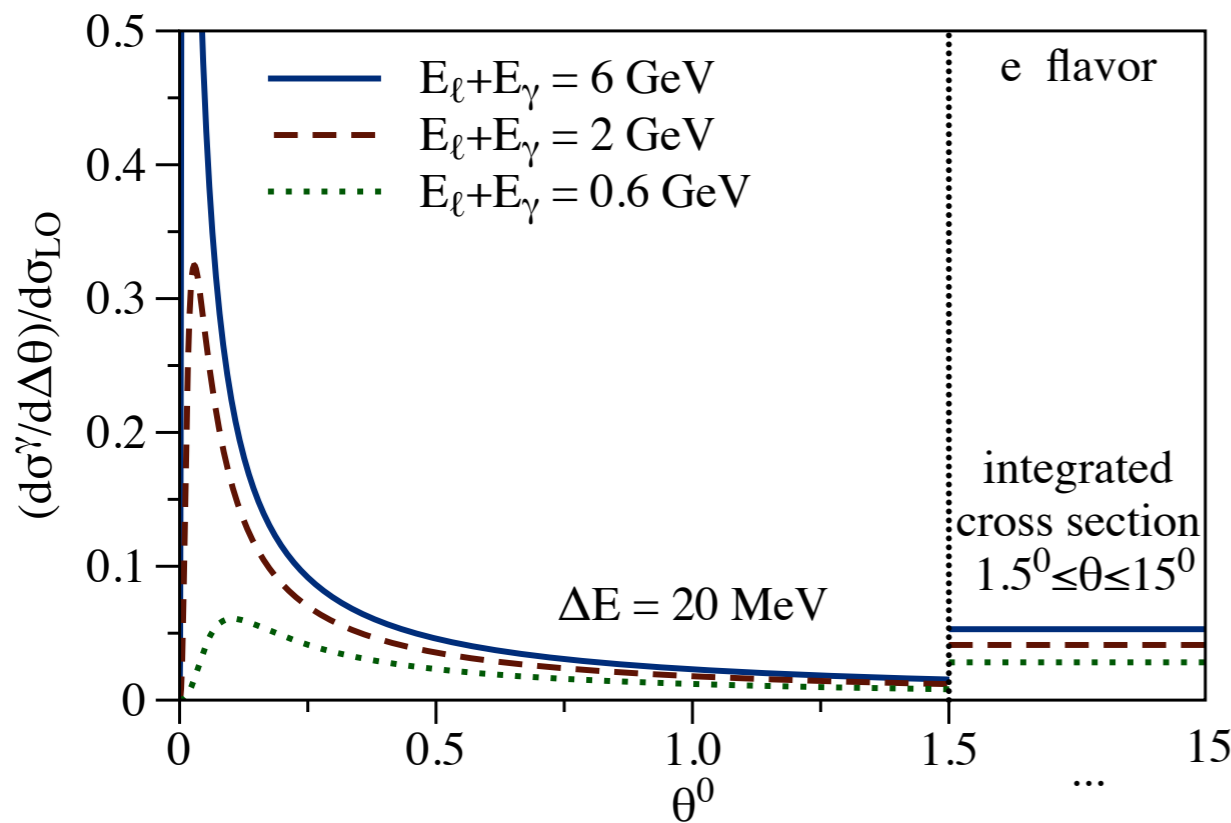
- formal limit of infinitely heavy nucleus $m_\ell \ll E_\ell \ll M$
- provides correct soft and collinear logarithms
- soft-photon energy < 20 MeV, jet size: 10° for electron and 2° for muon



- flavor-dependent effect, same for $\nu_\ell n \rightarrow \ell^- p$ vs $\bar{\nu}_\ell p \rightarrow \ell^+ n$
- collinear observable: cancellation of virtual vs real logs
- inclusive observables (+ γ): few % level, flavor independent

Electron vs muon jets

- factorization for radiation of collinear photons
- cone angle is defined to lepton direction
- photons of energy > 20 MeV, fixed energy in the cone



- flavor-dependent effect, same for $\nu_\ell n \rightarrow \ell^- p$ vs $\bar{\nu}_\ell p \rightarrow \ell^+ n$
- forward-peaked radiation for electron flavor
- negligible radiation for muons with shifted peak position

Factorization approach

- cross section is given by **factorization formula**

$$d\sigma \sim S \left(\frac{\Delta E}{\mu} \right) J \left(\frac{m_\ell}{\mu} \right) H \left(\frac{M}{\mu} \right)$$

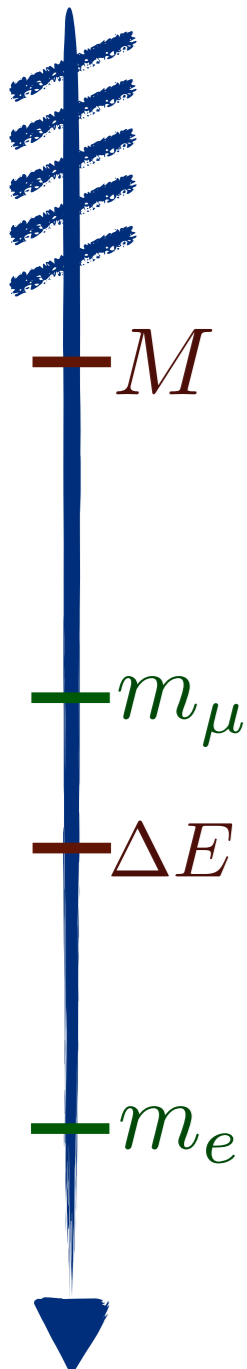
- determine **hard function** at hard scale by matching experiment or **hadronic model** to the theory with heavy nucleon

- **soft and collinear functions** are evaluated **perturbatively**

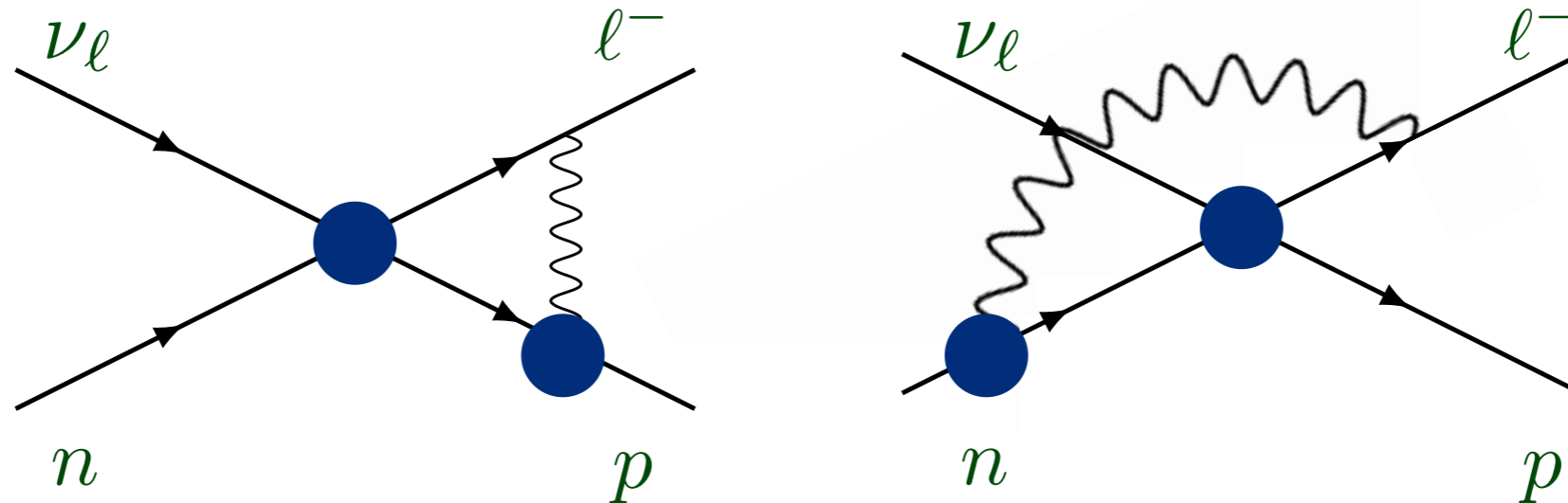
SCET power expansion parameter

$$\lambda \sim \frac{m_\mu^2}{E_\nu^2} \sim (\Delta\theta)^2 \sim \frac{\Delta E}{E_\nu}$$

$\ln \lambda$ enhancements



Hadronic model at GeV scale




- exchange of photon between the charged lepton and nucleons
- assume **onshell form** for each interaction with dipole form factors
discussed for neutrino-nucleon scattering: Graczyk, Phys. Lett. B 732, 315-319 (2013)
- add **self energy** for charged particles
- reproduce soft and collinear regions of SCET

- best determination of hard function

Factorization approach

- cross section is given by **factorization formula**

$$d\sigma \sim S \left(\frac{\Delta E}{\mu} \right) J \left(\frac{m_\ell}{\mu} \right) H \left(\frac{M}{\mu} \right)$$

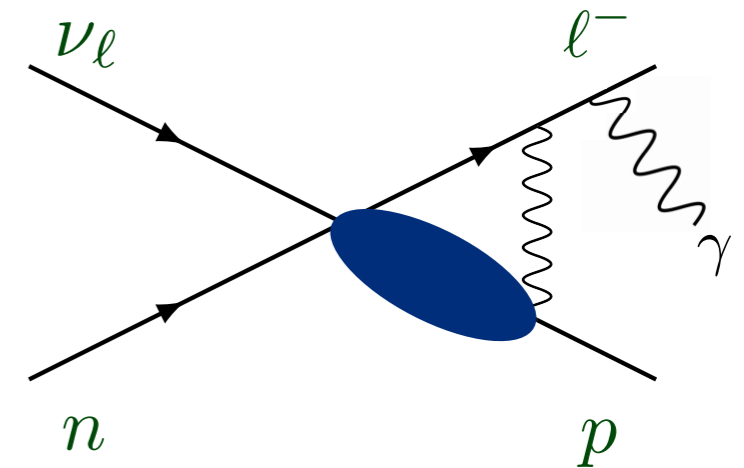
- 
- determine **hard function** at hard scale by matching experiment or **hadronic model** to the theory with heavy nucleon
 - **RGE evolution** of the hard function to scales $\Delta E, m_\ell$
 - **soft and collinear functions** are evaluated **perturbatively**
 - calculate cross section at low energies accounting for **all large logs**
ep scattering with soft radiation only: Richard J. Hill, Phys. Rev. D 95 1, 013001 (2016)

- **soft and collinear functions** determined **analytically**
- **hard function** describes physics at GeV energies

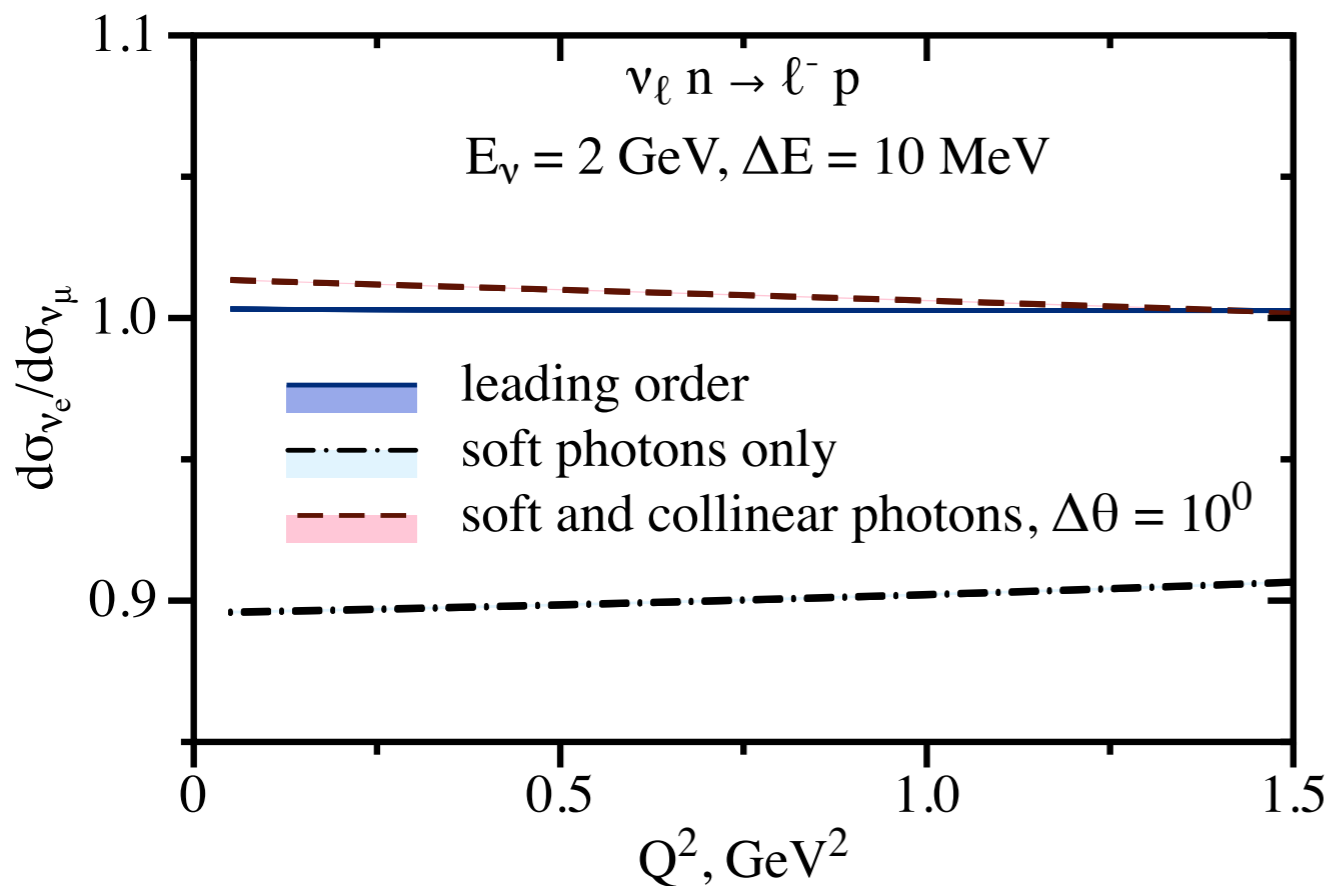
Charged-current scattering on nucleons

- theory and 1st-ever complete calculation
- 10-20% hadronic uncertainties
- cancel for e/μ ratio

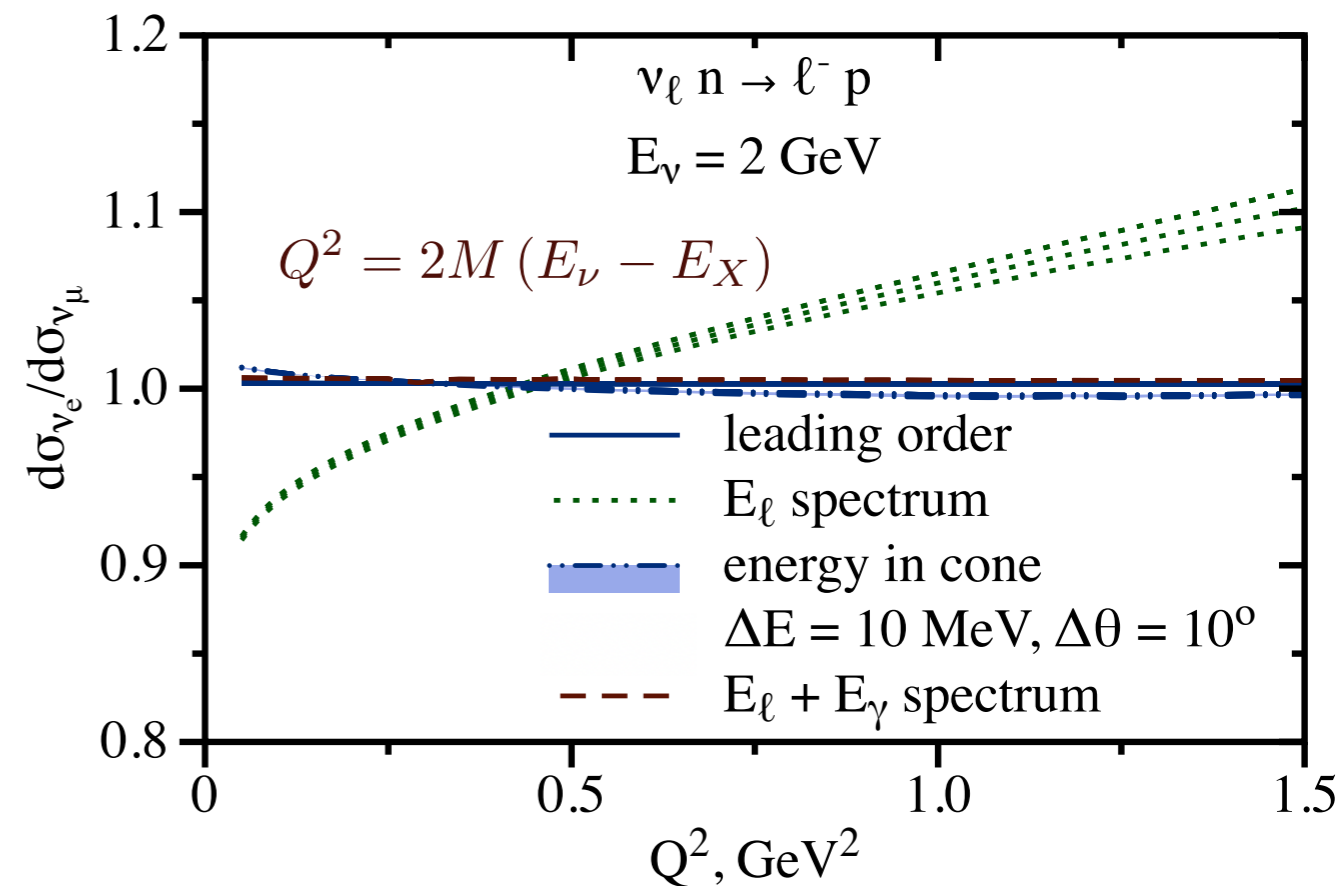
O. T. Qing Chen, Richard J. Hill, Kevin S. McFarland, and Clarence Wret (2021, 2022)



exclusive



inclusive

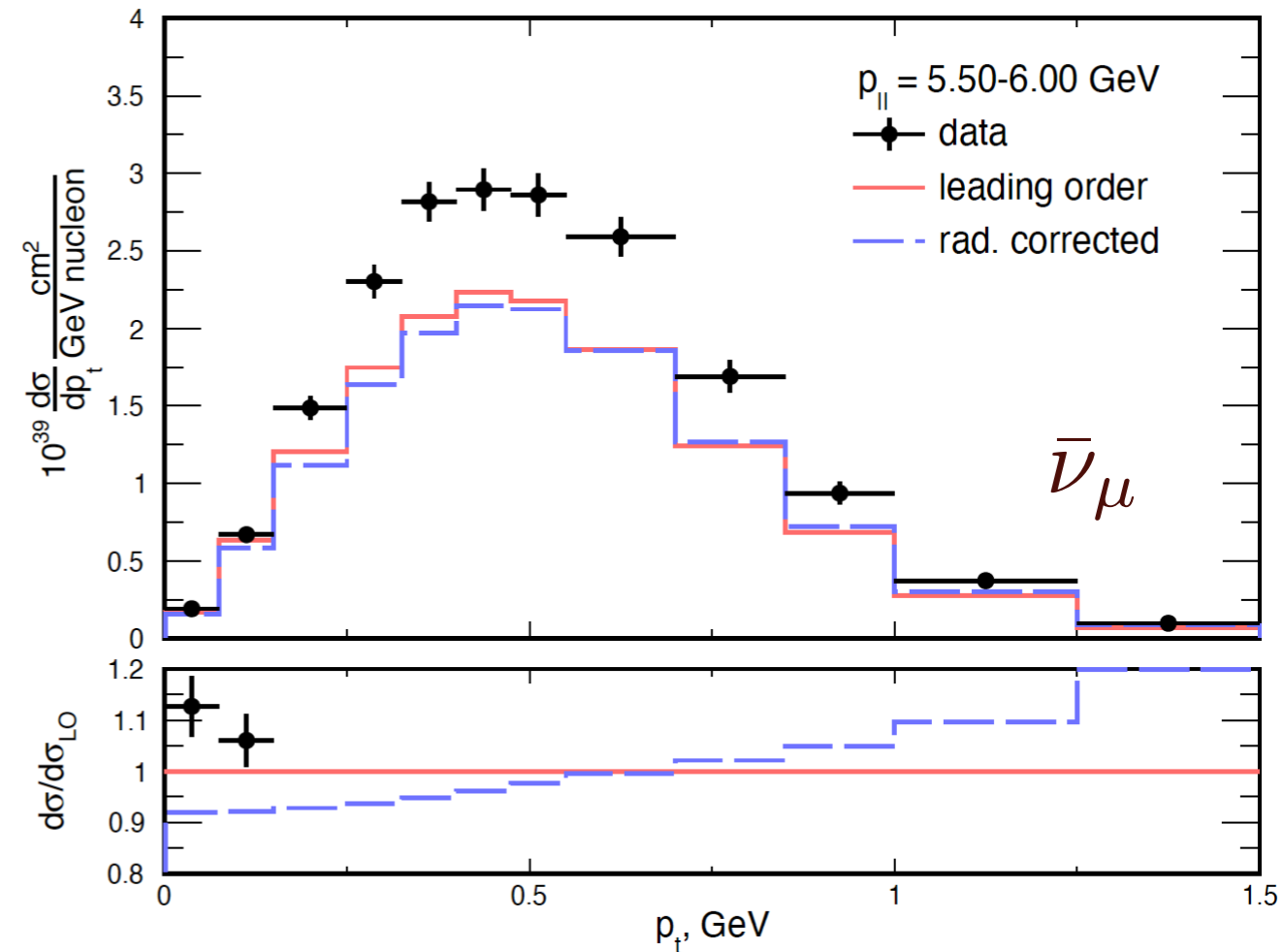
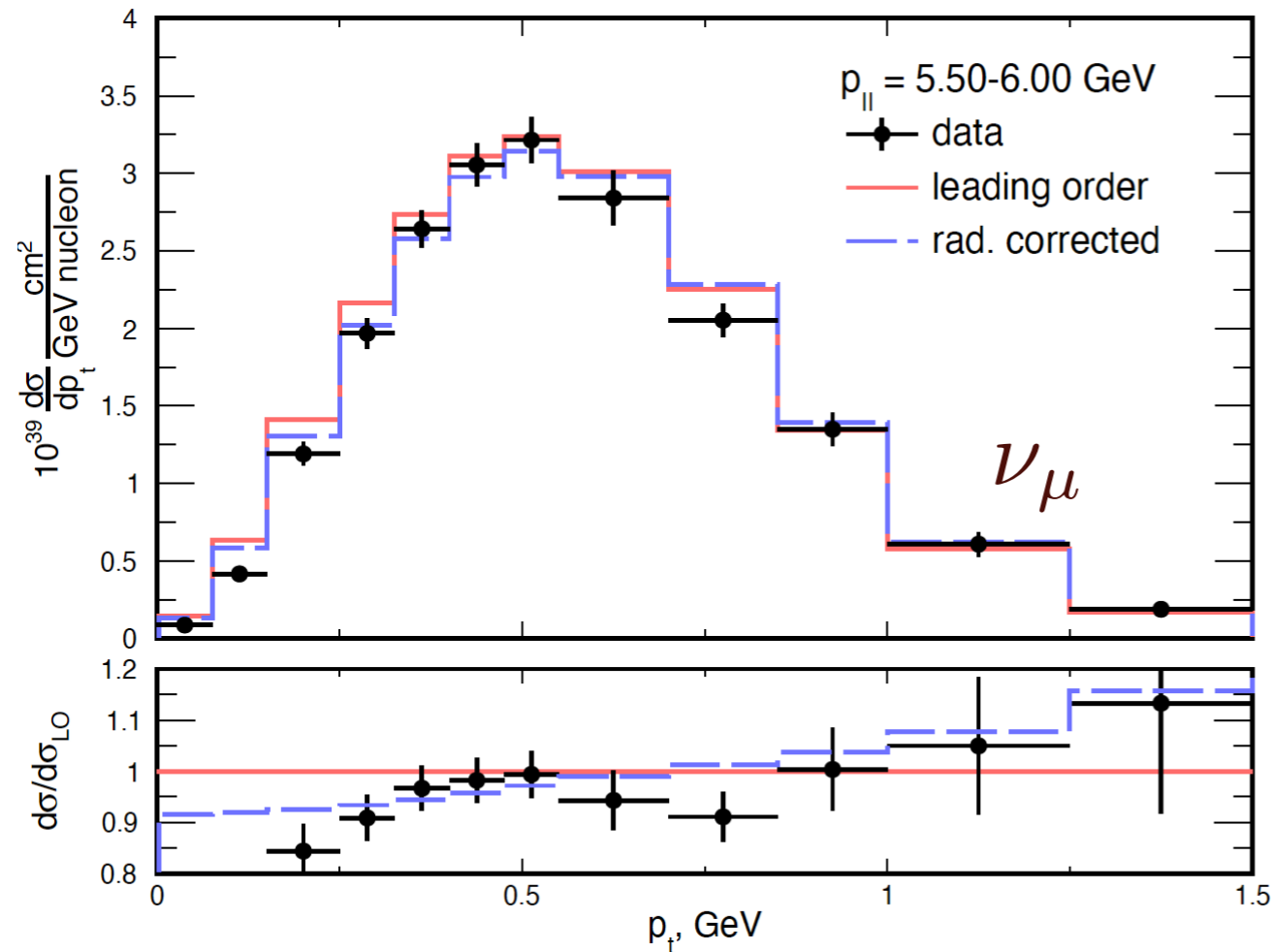


- critical dependence on details of experimental analysis
- predict σ_{ν_e} from σ_{ν_μ} measurements with neutrino beam



Comparison to data

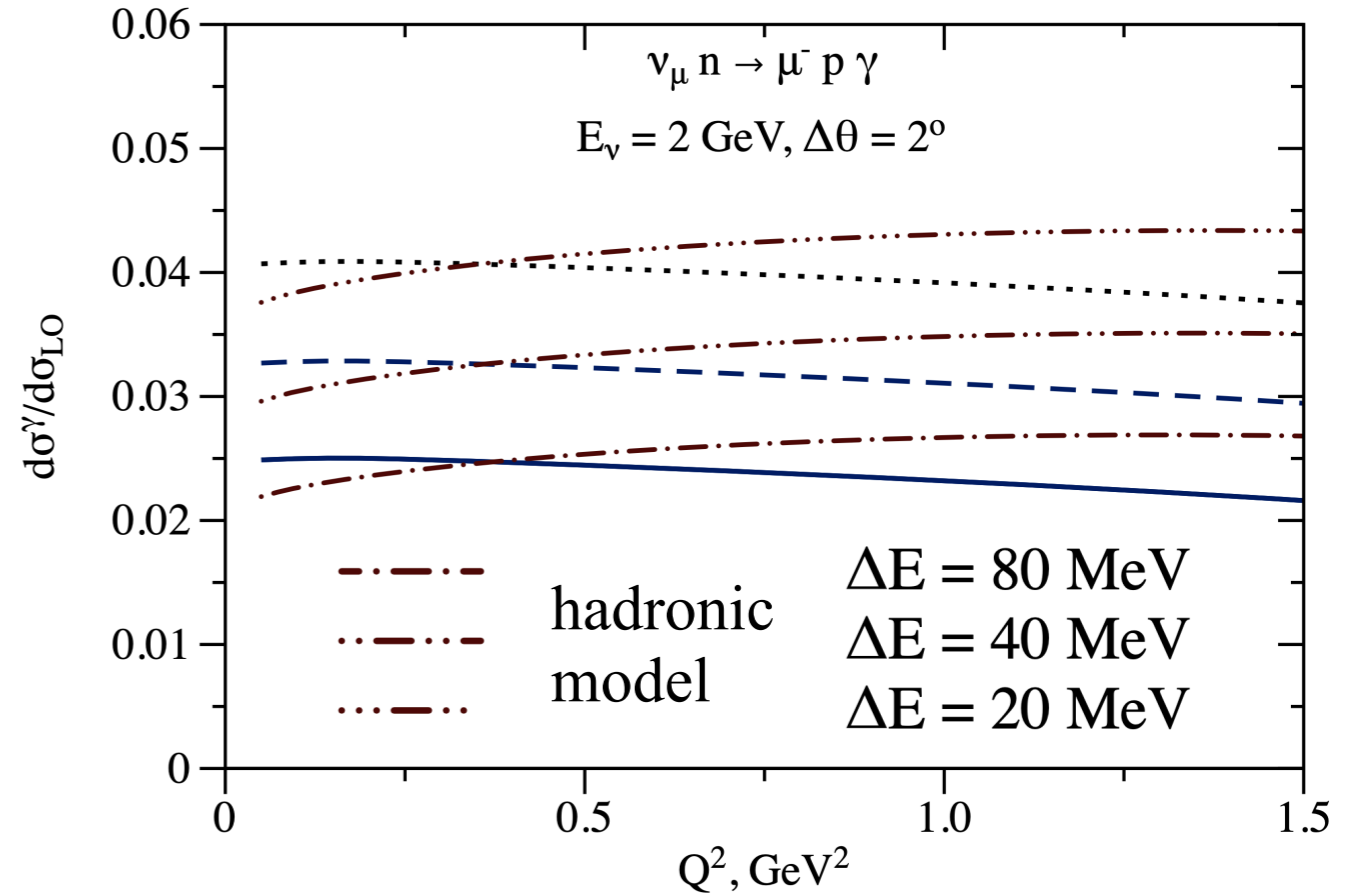
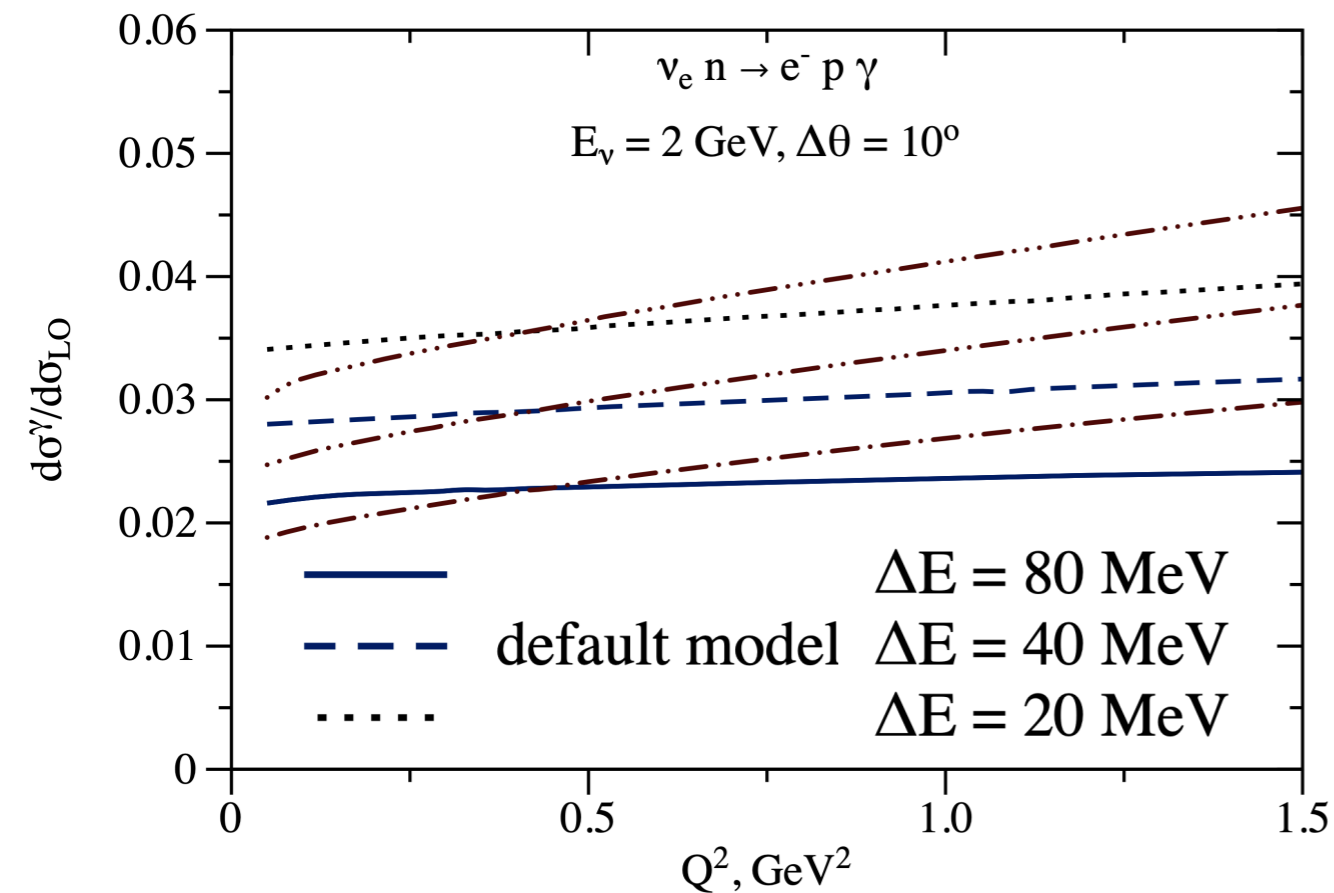
- medium-energy flux data from MINERvA@FERMILAB



- electron flavor: measurements are uncertain
- muon flavor: comparable to experimental precision

Radiation of hard photons

- model-dependent description for radiation of hard photons



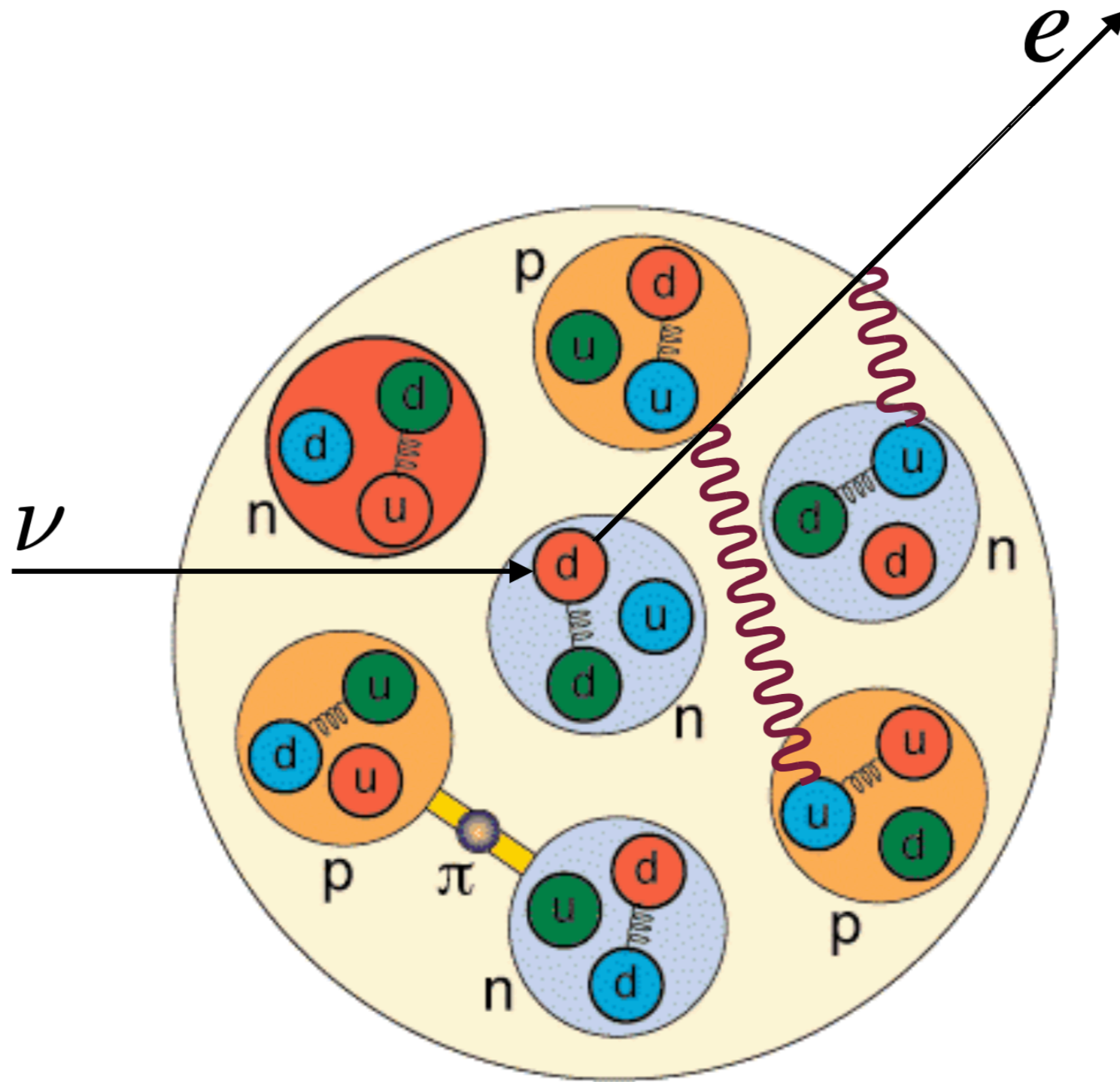
“Blunden calculation”

- photon energies are above 20, 40, and 80 MeV: default vs “SIFF”

“hadronic model”

- % -level radiation of non-collinear hard photons
- 10^{-4} flavor misidentification rate for NO ν A&T2K kinematics

QED medium effects



- charged lepton exchanges photons with nuclear medium

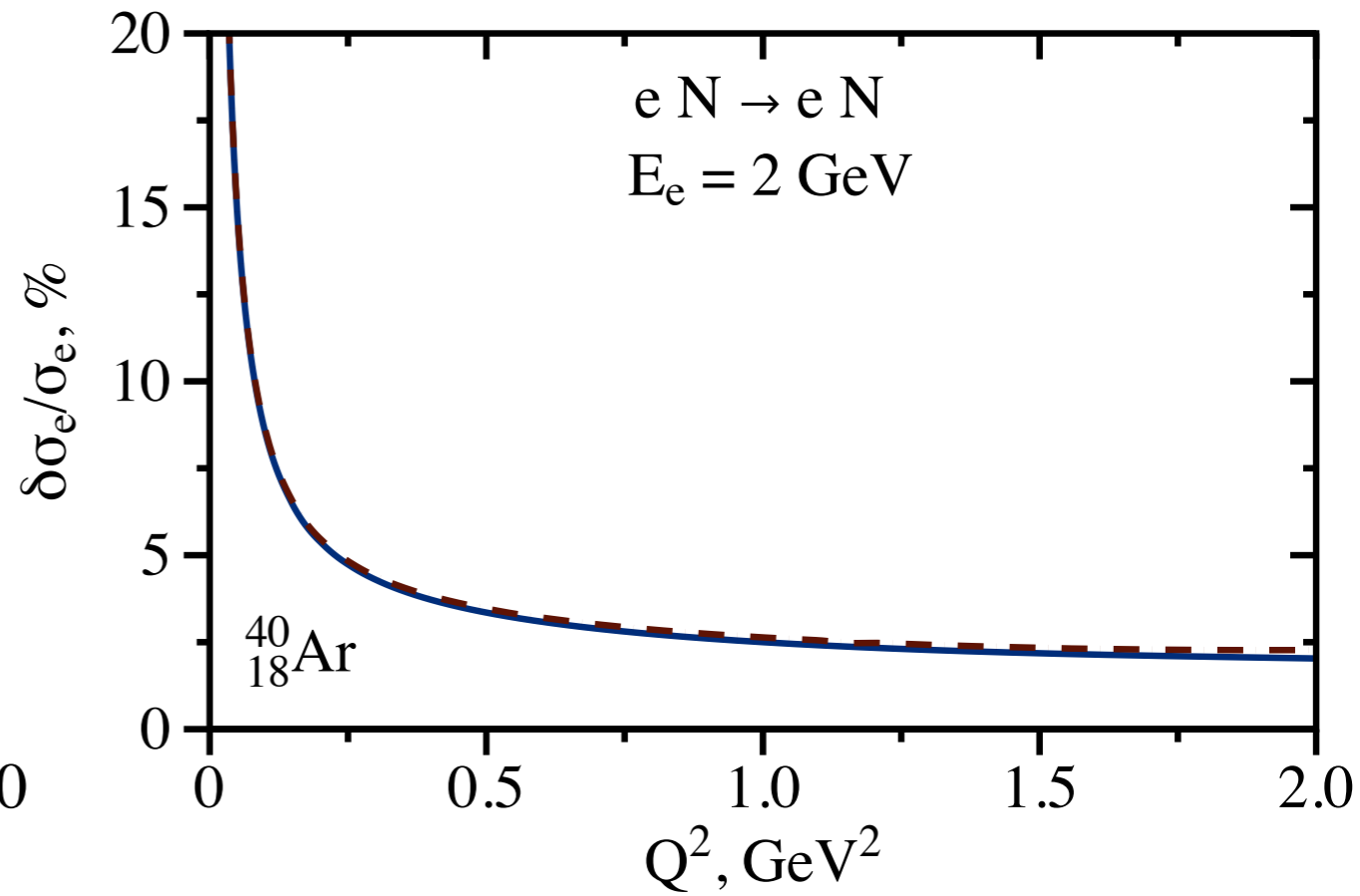
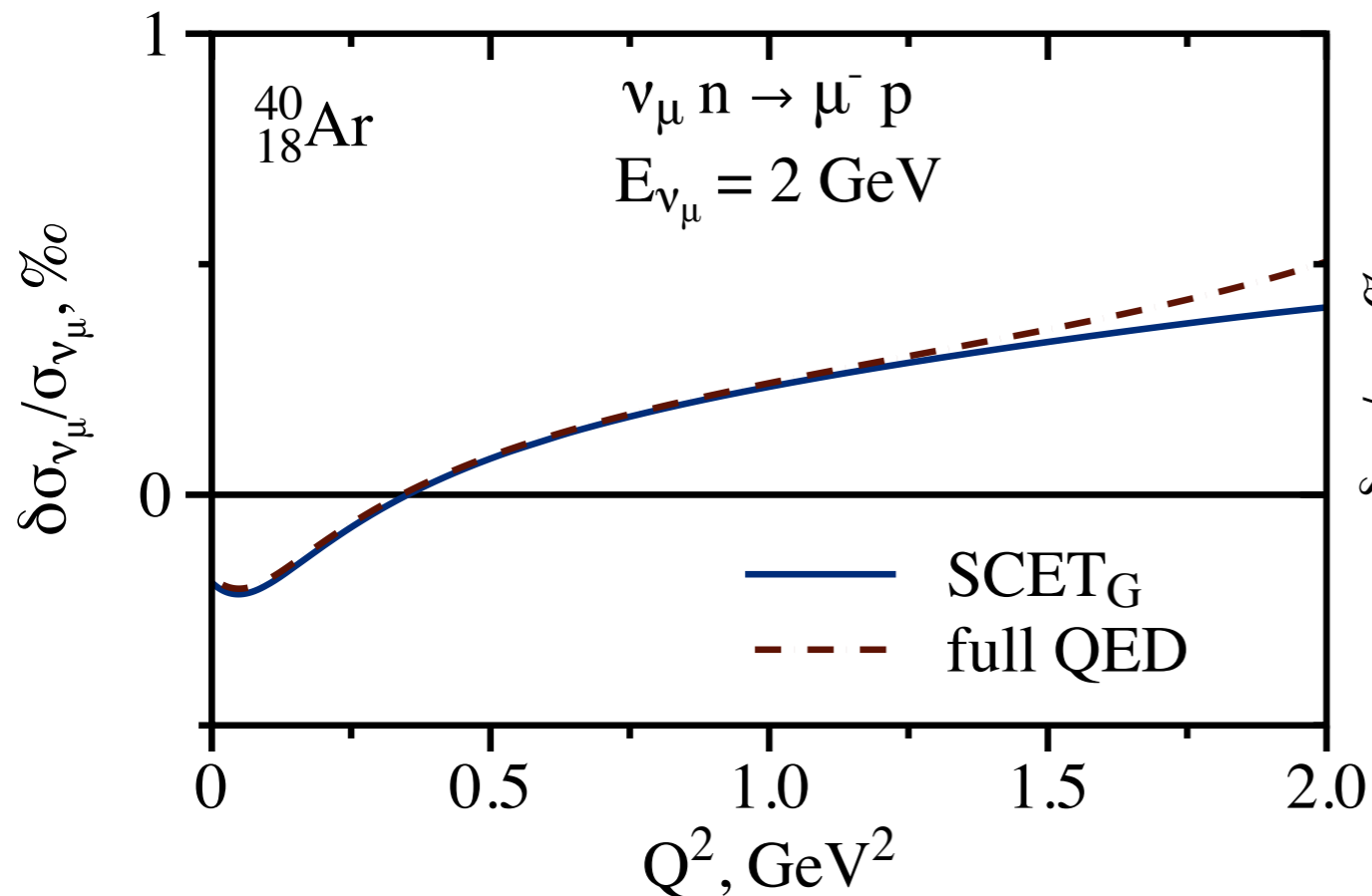
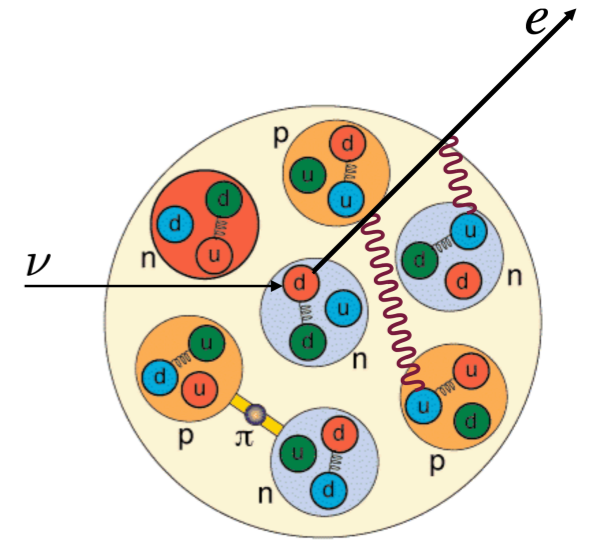
QED nuclear medium effects

- theory and 1st-ever estimate by two methods:

SCET_G: Soft-collinear effective theory (Glauber)

QED: quantum electrodynamics

O. T. and Ivan Vitev, Phys. Lett. B 805, 135466 (2022)



- permille-level for $\nu_e A \rightarrow eA'$, percent-level for $eA \rightarrow eA$
- critical new effect for electron scattering experiments

Conclusions

- neutrino cross sections is the main tool to access neutrinos
- various production and interaction mechanisms at all energy scales
- radiative corrections (1-20%) for consistent uncertainty estimates
- radiative corrections for precise flux determinations
- QED nuclear effects in neutrino and electron scattering
- total and differential $\nu e, \nu_\ell n \rightarrow \ell^- p$ and $\bar{\nu}_\ell p \rightarrow \ell^+ n$
flavor ratios evaluated from theory with rigorous error analysis

Thanks for your attention !!!