

Nonlinear Optical Properties of 2D Quantum Materials

ExpandQISE Track 2: Quantum Materials Institute: 2D Materials, heterostructures and metasurfaces for quantum light

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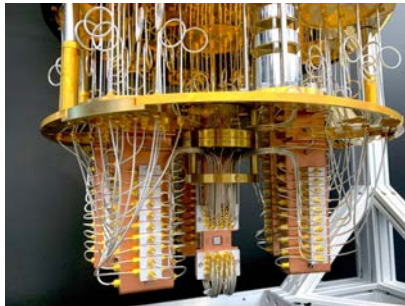
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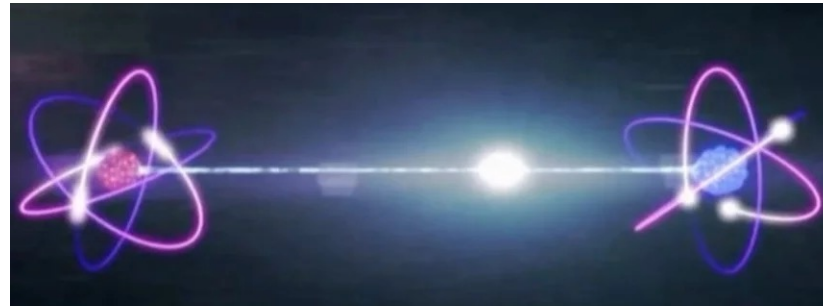
Quantum Information Science

Quantum Information Science (QIS) encompasses efforts to develop quantum computers, quantum sensors, and secure communications networks, all of which obtain some advantage over their classical counterparts due to the intrinsic properties of quantum mechanics. A leading effort towards secure communications involves the exchange of cryptographic keys using a quantum network, so called quantum key distribution (QKD) systems. Leading efforts to realize QKD systems involve photonics and nanophotonics which are the focus of this talk.

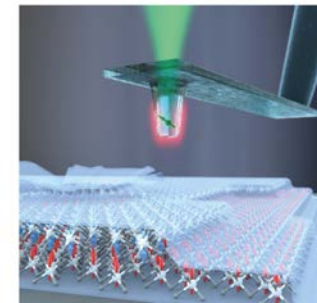
Quantum
Computing¹



Quantum
Communications²



Quantum
Sensing³



¹<https://www.popsci.com/technology/in-photos-journey-to-the-center-of-a-quantum-computer/>

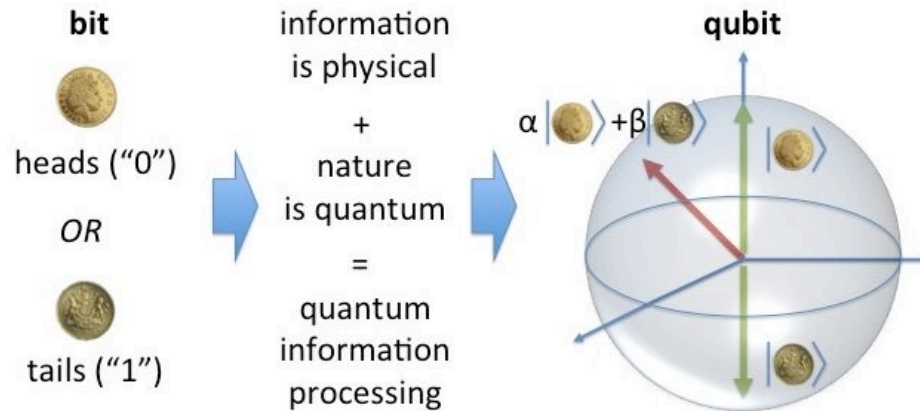
²<https://thequantuminsider.com/2023/02/20/quantum-entanglement-communication/>

³<https://quantum-sensing.physik.unibas.ch/en/p/461/6/>

Superposition and Entanglement

QIS is based on two important features of quantum mechanics, superposition and entanglement:

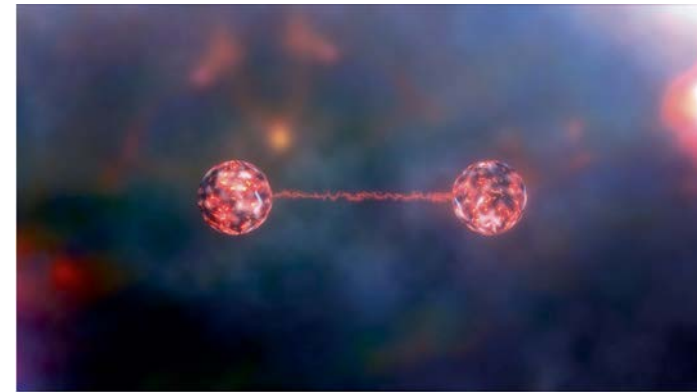
Superposition¹



Information is encoded in a superposition of states, for a two-level system this is termed a qubit.

¹<https://cnqo.phys.strath.ac.uk/research/quantum-information/>

Entanglement²



Pioneering quantum information science

4 October 2022, the Royal Swedish Academy of Sciences announced that the [2022 Nobel Prize in Physics](#) would be awarded to three scientists — Alain Aspect, John F. Clauser and Anton Zeilinger — “for experiments with entangled photons, establishing the violation of Bell inequalities and pioneering quantum information science.”

²*Nature Computational Science* 2022 Vol. 2 Issue 11 Pages 687-688
DOI: 10.1038/s43588-022-00368-0

EPR Paradox and Bells Theorem

EINSTEIN ATTACKS QUANTUM THEORY

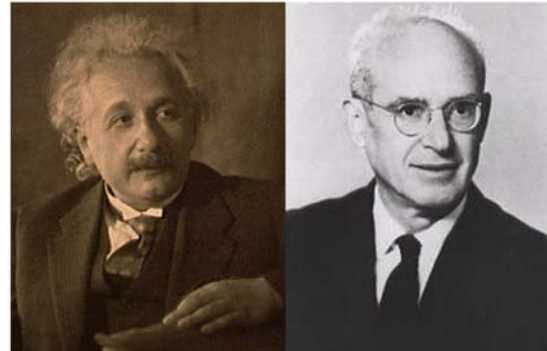
Scientist and Two Colleagues
Find It Is Not 'Complete'
Even Though 'Correct.'

SEE FULLER ONE POSSIBLE

Believe a Whole Description of
'the Physical Reality' Can Be
Provided Eventually.

New York Times, May 4, 1935

EPR Paradox¹



Einstein and Rosen drafted in coordination with Podolsky their famous paper labeling effects originating from complementarity and entanglement the Einstein-Podolsky-Rosen paradox. – Wikipedia

"EPR appeared to have contrived a means to establish the exact values of *either* the momentum *or* the position of B due to measurements made on particle A, without the slightest possibility of particle B being physically disturbed."

¹https://en.wikipedia.org/wiki/Einstein-Podolsky-Rosen_paradox

Bells Theorem²



Locality

"... that the result of a measurement on one system be unaffected by operations on a distant system..." (Bell)

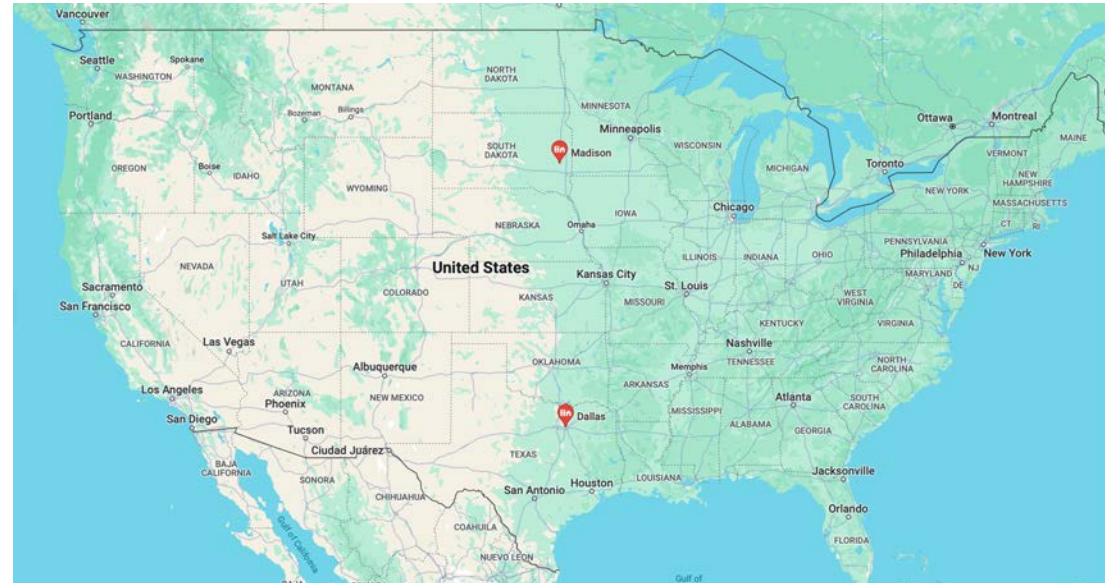
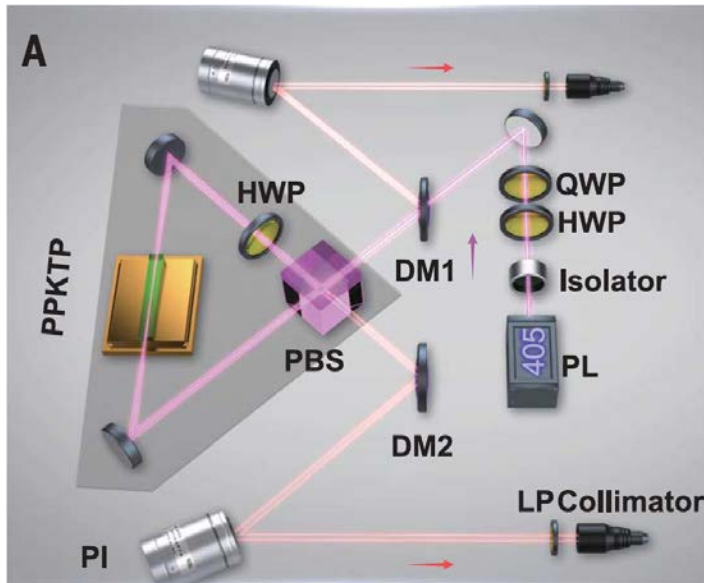
John Stewart Bell is the originator of Bell's theorem, important in quantum physics regarding hidden variable theories. – Wikipedia

- In 1964 John Stewart Bell replied on the Einstein-Podolsky-Rosen Paradox, deriving an inequality making it possible to distinguish between all local realistic theories and quantum theory.
- in the early 80's Aspect, Grangier and Roger showed their experimental data violated the inequality, refuting all local realistic theories and proving that quantum theory was right!

²<http://www.qutools.com>

Entangled Photons by SPDC on a Global Scale

Satellite-based entanglement over 1200 kilometers²



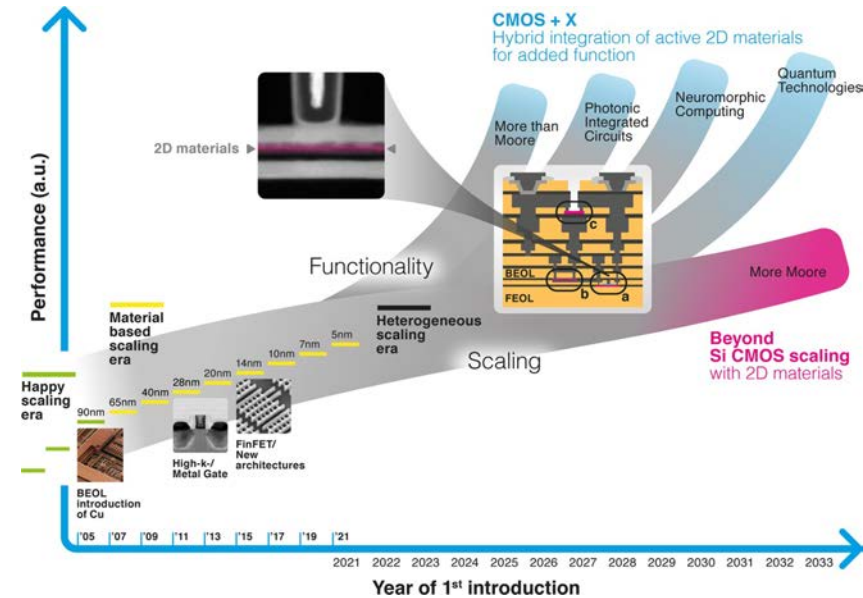
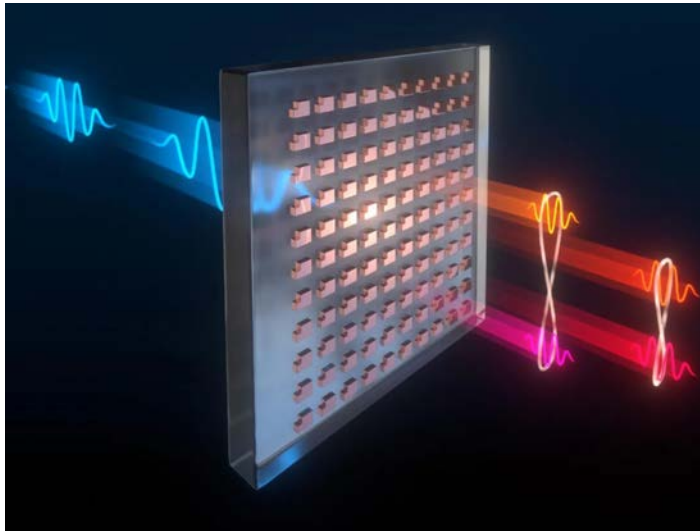
Entanglement over global length scales demonstrated via entangled photons generated by spontaneous parametric downconversion (SPDC) transmitted via satellite.

²J. Yin, Y. Cao, Y.-H. Li, S.-K. Liao, L. Zhang, J.-G. Ren, et al. *Science* 2017 Vol. 356 Pages 1140-1144
DOI:10.1126/science.aan3211

2D Materials for Integrated Quantum Technologies

Motivation: Parametric downconverters, single photon emitters and detectors are key components of quantum information systems. Structure-property relations of the materials they comprise determine performance and guide their development and application.

Focus: Develop spatially- and spectrally-resolved multiphoton imaging methods to characterize quantum materials on passive and enhancing substrates, including metasurfaces.



Parametric down conversion generates entangled photon pairs¹ for quantum communications. 2D materials can integrate into CMOS fab, promising properties².

¹<https://spectrum.ieee.org/metasurface-entangled-photons>

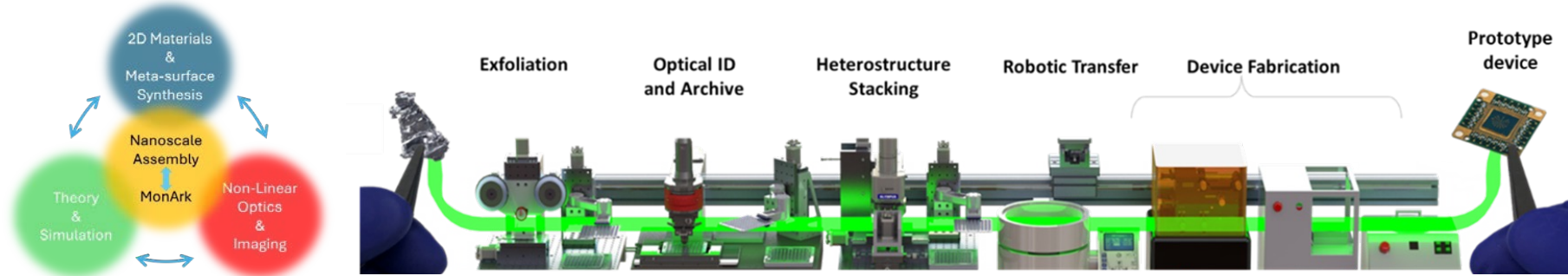
²Lemme, M.C., Akinwande, D., Huyghebaert, C. *et al.* 2D materials for future heterogeneous electronics. *Nat Commun* **13**, 1392 (2022). <https://doi.org/10.1038/s41467-022-29001-4>

⇒ Parametric downconversion

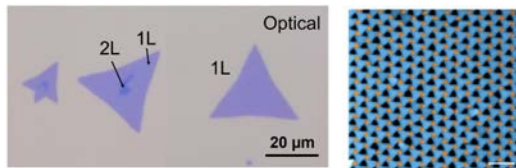
⇒ $\chi_{ijk}^{(2)}$ in 2D heterostructures

⇒ Integrable with chip scale fab

Nonlinear Optics, 2D Materials and Metaphotonics

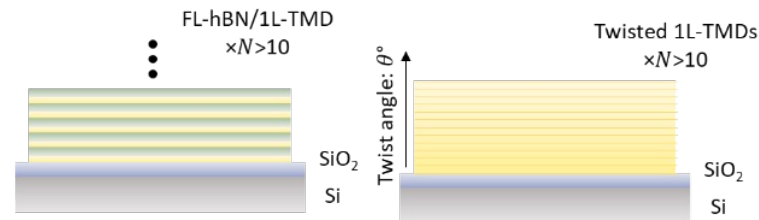


Methods Available at South Dakota Mines: Nonlinear imaging, **synthesis of 2D materials** and self-assembled nanostructures/metasurfaces, FDTD simulations and **density functional theory**.

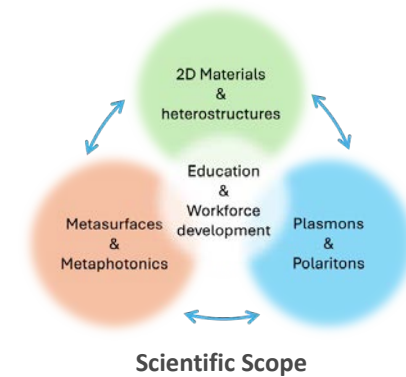


South Dakota Mines team: Expand scope to include **materials synthesis and theory** to explore limits of $\chi_{ijk}^{(2)}$ in 2D materials and 2D materials integrated with metasurfaces.

MonArk Enabling Infrastructure: The 2D-QMaPs of the MonArk NSF Quantum Foundry are a primary resource for the preparation of 2D samples from bulk crystals, **assembly of 2D heterostructures of multiple 2D layers**, and the fabrication of prototype quantum devices.



MonArk team: Collaborate on the development of multilayer 2D materials heterostructures and varying interlayer coupling leading to optimal $\chi_{ijk}^{(2)}$.



⇒ materials, growth, theory and optics ⇒ MonArk 2D-QMaP, heterostructures ⇒ metaphotonics, polaritons, plasmons

Spectrally-Resolved Multi-photon Imaging and Spectroscopy

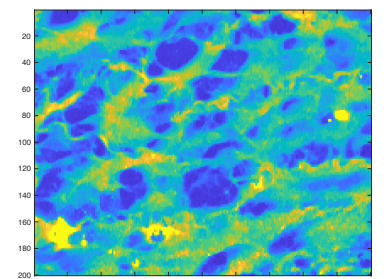
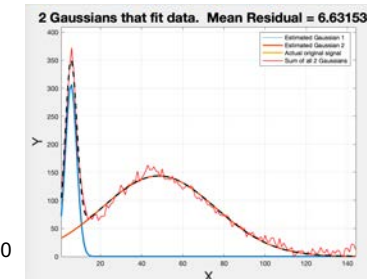
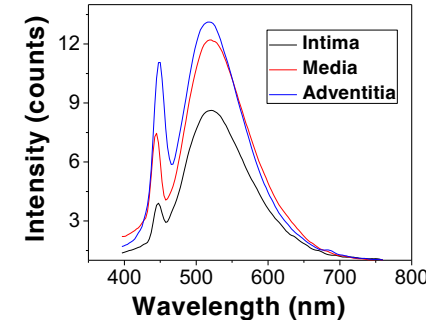
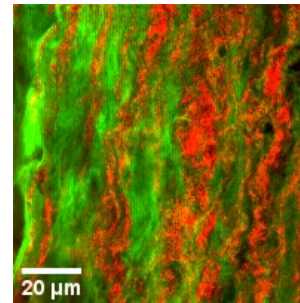
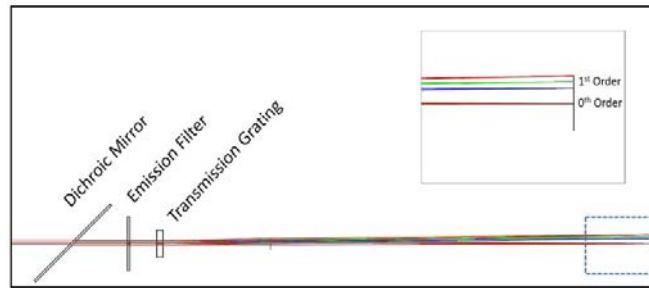
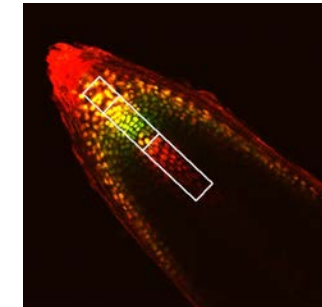
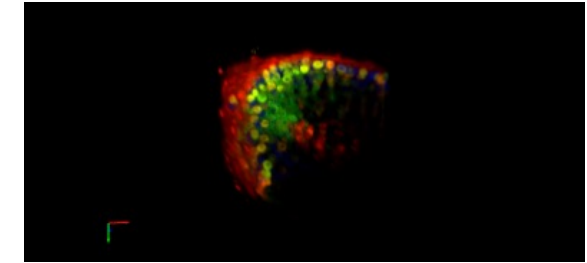
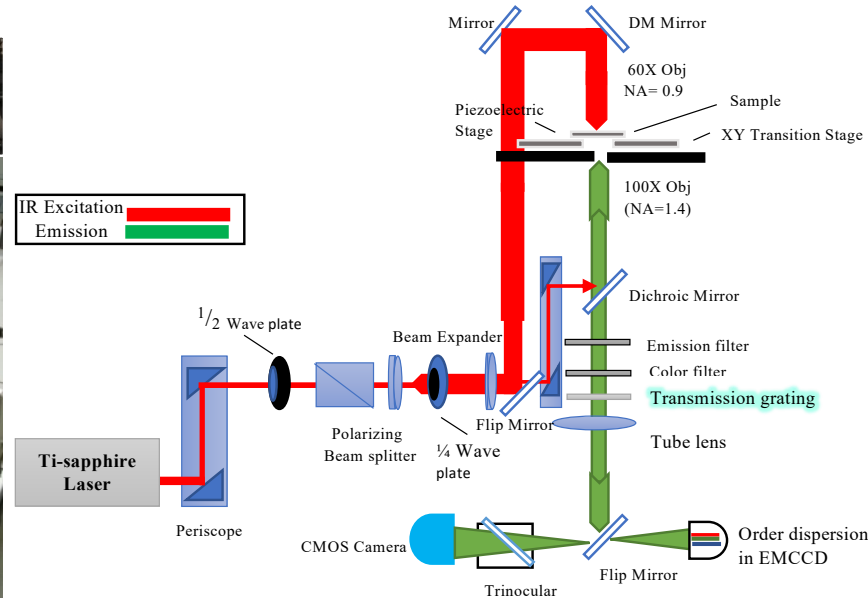
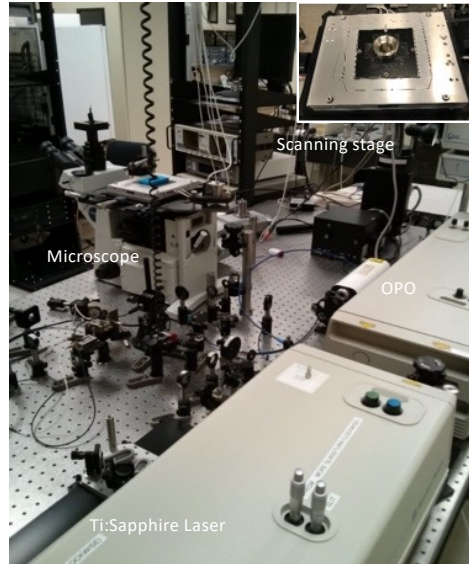


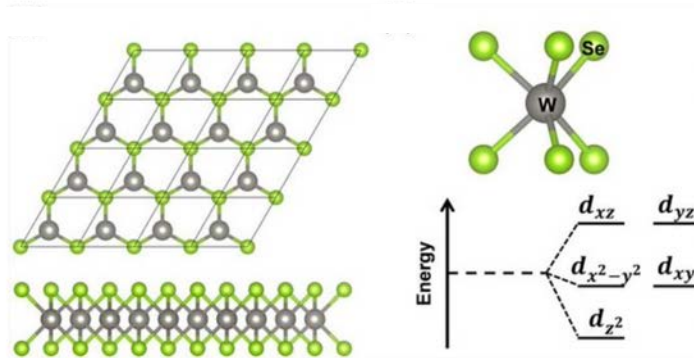
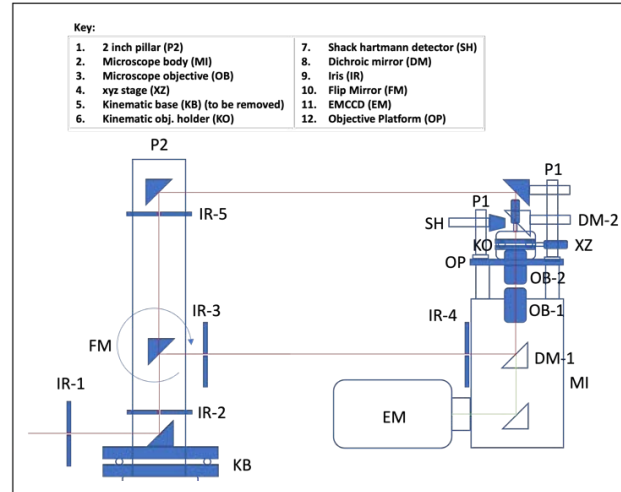
Figure: (left): Spectrally-resolved multiphoton microscope at SDSMT, with femtosecond lasers and scanning stage. (right): Schematic diagram and example multiphoton fluorescence (green) and SHG (red) image and spectra (SHG at 450nm) of collagen in arterial wall. Upper right: animation of 3D multiphoton excited fluorescence from transgenic plant (animation and maximum intensity projection). Lower right: deconvolved arterial wall image.

⇒ Imaging point spread function (x,y)

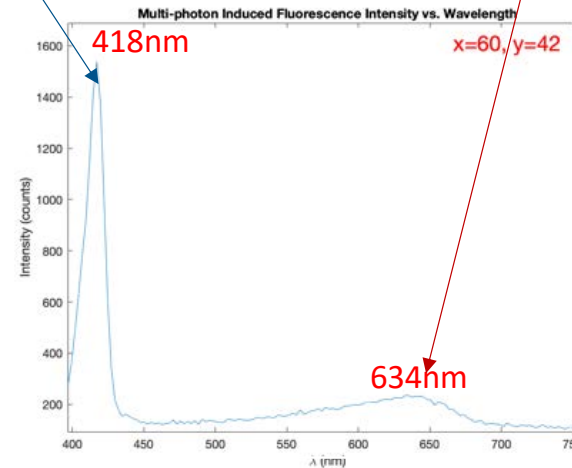
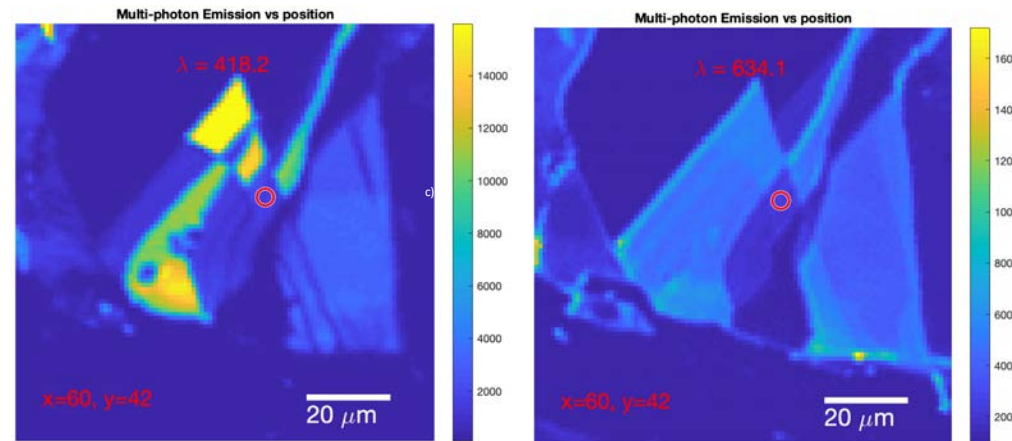
⇒ Spectra resolved, measure scattering

⇒ Normalize out intensity variations

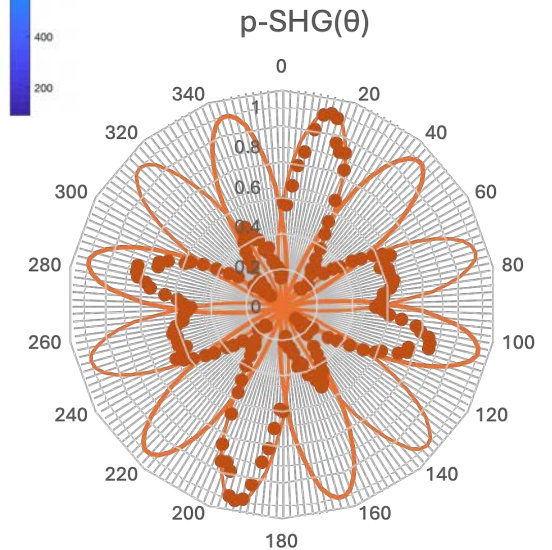
Multiphoton spectrally-resolved Imaging of WSe₂ (Borys)



⇒ SHG indicates monolayer fluctuations

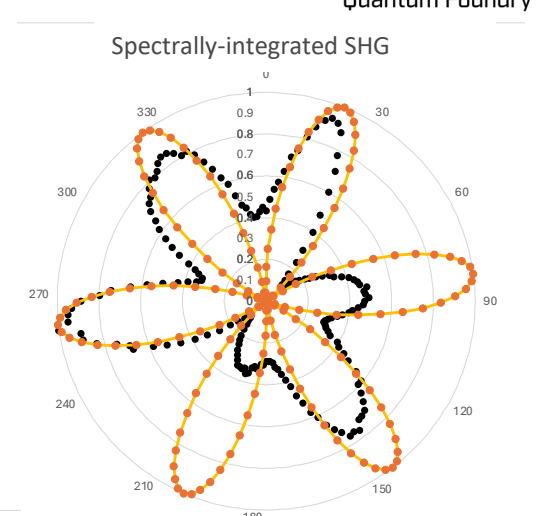
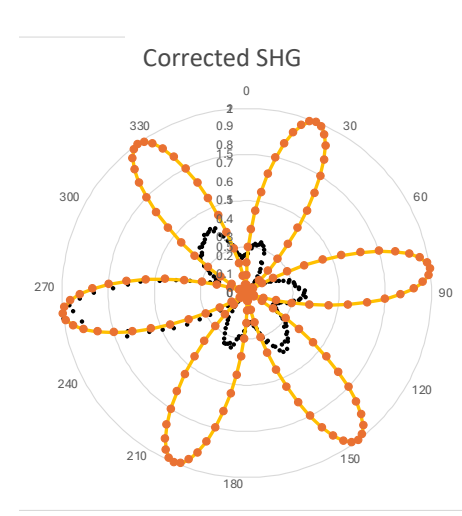
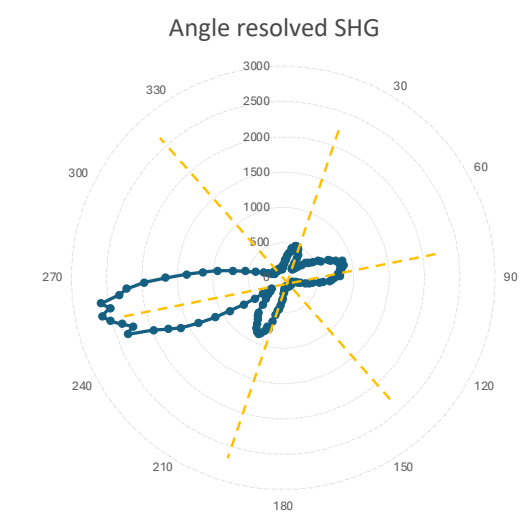
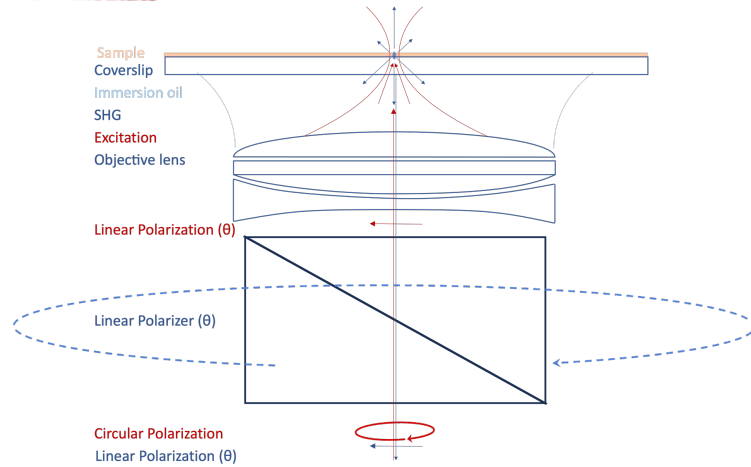


⇒ Correlated MPL details layers

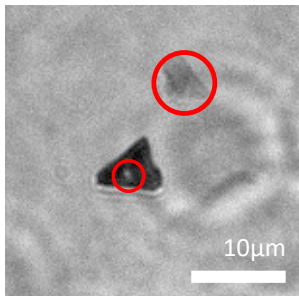


⇒ Spectra, Polarization at each point.

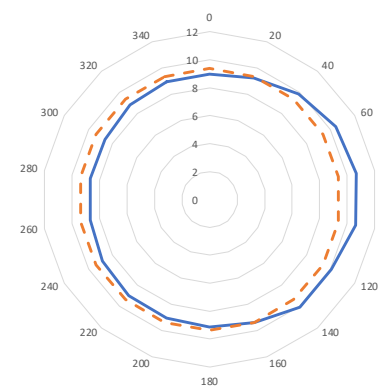
Angle-resolved linearly-polarized SHG from WSe₂ few-layer stacks



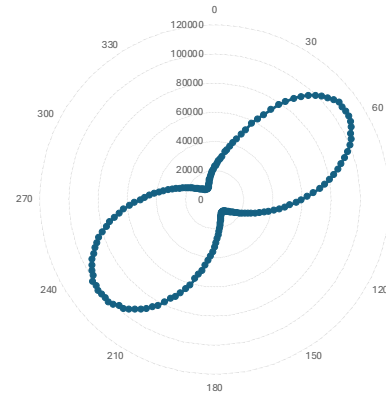
White light @ 100X



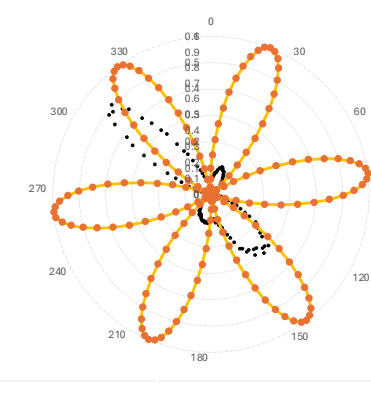
Dependence of Power after $\lambda/4$ plate compared to average



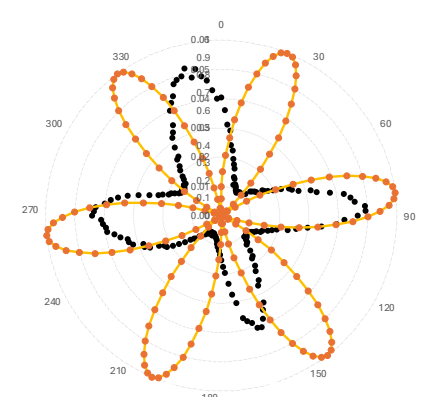
Dye Sphere SUM(C306:326)



Corrected SHG



Spectrally-integrated SHG

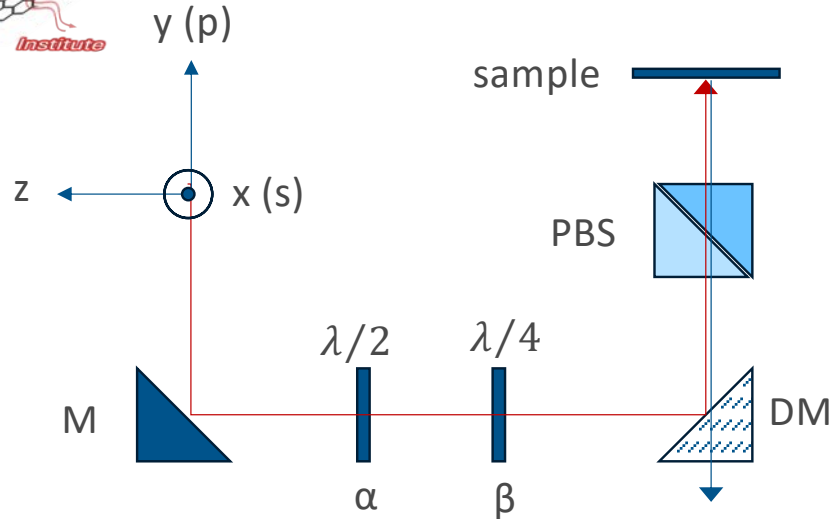


⇒ circularly polarized light input

⇒ primarily multi-layer samples

⇒ 6-fold and 4-fold symmetries appear

Correcting ellipticity in dichroic mirror to obtain circular polarization



Jones matrices for system elements:

$$\underline{\mathbf{M}}_{\delta} = \begin{pmatrix} R_s e^{i\delta/2} & 0 \\ 0 & R_p e^{-i\delta/2} \end{pmatrix} \quad \underline{\mathbf{R}} = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix}$$

$$\mathbf{v}_{in} = \begin{pmatrix} 0 \\ 1 \end{pmatrix} \quad \underline{\mathbf{M}}_{\lambda/2} = \begin{pmatrix} i & 0 \\ 0 & -i \end{pmatrix} \quad \underline{\mathbf{M}}_{\lambda/4} = \begin{pmatrix} e^{i\pi/4} & 0 \\ 0 & e^{-i\pi/4} \end{pmatrix}$$

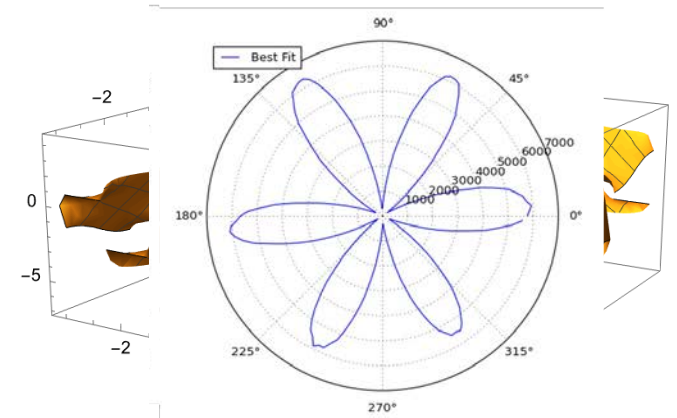
$$\underline{\mathbf{M}}_{\theta} = \underline{\mathbf{R}}^{-1}(\theta) \underline{\mathbf{M}}_{\lambda/n} \underline{\mathbf{R}}(\theta) \quad \mathbf{v}_{out} = \underline{\mathbf{M}}_{sys} \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$\underline{\mathbf{M}}_{sys} = \begin{pmatrix} R_s e^{i\delta/2} & 0 \\ 0 & R_p e^{-i\delta/2} \end{pmatrix} \begin{pmatrix} \cos \beta & \sin \beta \\ -\sin \beta & \cos \beta \end{pmatrix} \begin{pmatrix} e^{i\pi/4} & 0 \\ 0 & e^{-i\pi/4} \end{pmatrix} \begin{pmatrix} \cos \beta & -\sin \beta \\ \sin \beta & \cos \beta \end{pmatrix} \begin{pmatrix} \cos \alpha & \sin \alpha \\ -\sin \alpha & \cos \alpha \end{pmatrix} \begin{pmatrix} i & 0 \\ 0 & -i \end{pmatrix} \begin{pmatrix} \cos \alpha & -\sin \alpha \\ \sin \alpha & \cos \alpha \end{pmatrix}$$

$$\mathbf{v}_{out} = e^{i\delta/2} \begin{pmatrix} e^{i\delta/2} \{ (1+i) \cos 2\alpha - (1-i) \cos 2(\alpha - \beta) \} R_s \\ e^{-i\delta/2} \{ (1+i) \sin 2\alpha + (1-i) \sin 2(\alpha - \beta) \} R_p \end{pmatrix}$$

$$\mathbf{v}_{out} = e^{i\delta/2} \begin{pmatrix} e^{i\delta/2} \{ \cos 2\alpha - \cos 2(\alpha - \beta) + i(\cos 2\alpha + \cos 2(\alpha - \beta)) \} R_s \\ e^{-i\delta/2} \{ \sin 2\alpha + \sin 2(\alpha - \beta) + i(\sin 2\alpha - \sin 2(\alpha - \beta)) \} R_p \end{pmatrix}$$

$$\delta \sim \pi/4 \quad \mathbf{v}_{out} = \begin{pmatrix} \left(\frac{1}{2} + \frac{i}{2} \right) (-1)^{3/8} R_s (\cos 2\alpha + i \cos 2(\alpha - \beta)) \\ \left(\frac{1}{2} + \frac{i}{2} \right) (-1)^{1/8} R_p (\sin 2\alpha - i \sin 2(\alpha - \beta)) \end{pmatrix}$$

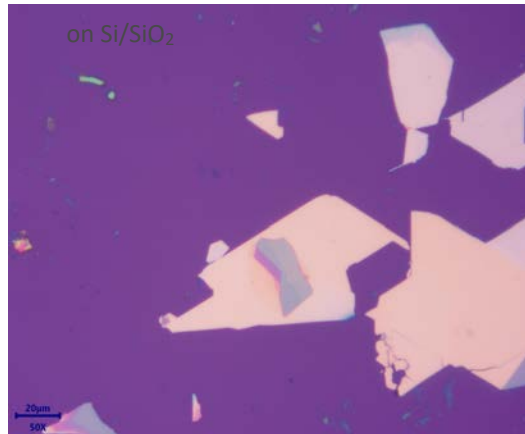


Giant Modulation of Second-Harmonic Generation in CuInP_2S_6 by Interfacing with MoS_2 Atomic Layers

Dawei Li^{*}, Xinyi Hou, Fanyi Kong, Kun Wang, and Xia Hong^{*}

Cite This: *ACS Nano* 2024, 18, 32890–32898

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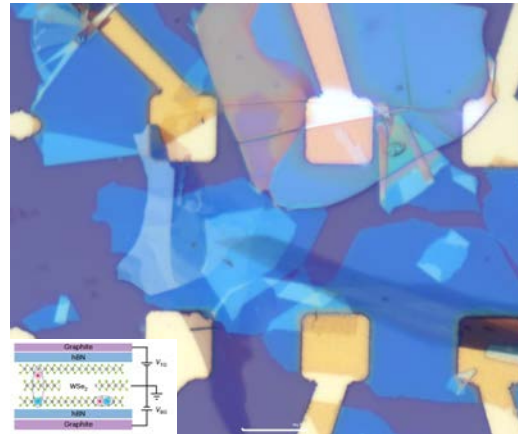
⇒ CIPS/MoS2 heterostructures

Giant optical nonlinearity of Fermi polarons in atomically thin semiconductors

Received: 21 September 2023

Accepted: 25 March 2024

Liuxin Gu^{1,2}, Lifu Zhang^{1,2}, Ruihao Ni¹, Ming Xie², Dominik S. Wild³,
Suji Park⁴, Houk Jang⁴, Takashi Taniguchi⁵, Kenji Watanabe⁶,
Mohammad Hafezi⁷ & You Zhou^{1,2}✉



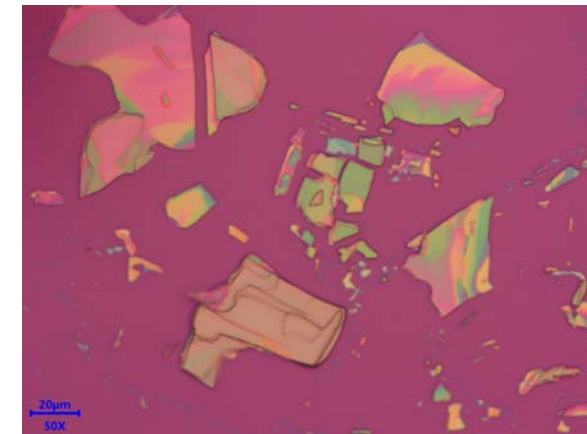
⇒ MonArk WSe_2 /h-BN heterostructures

Regulating Second-Harmonic Generation by Van der Waals Interactions in 2D Lead Halide Perovskite Nanosheets

Wen-Juan Wei, Xingxing Jiang, Li-Yuan Dong, Wei-Wei Liu, Xiao-Bo Han, Yan Qin, Kai Li, Wei Li, Zheshuai Lin, Xian-He Bu, and Pei-Xiang Lu

J. Am. Chem. Soc., Just Accepted Manuscript • DOI: 10.1021/jacs.9b01874 • Publication Date (Web): 26 May 2019

Downloaded from <http://pubs.acs.org> on May 26, 2019



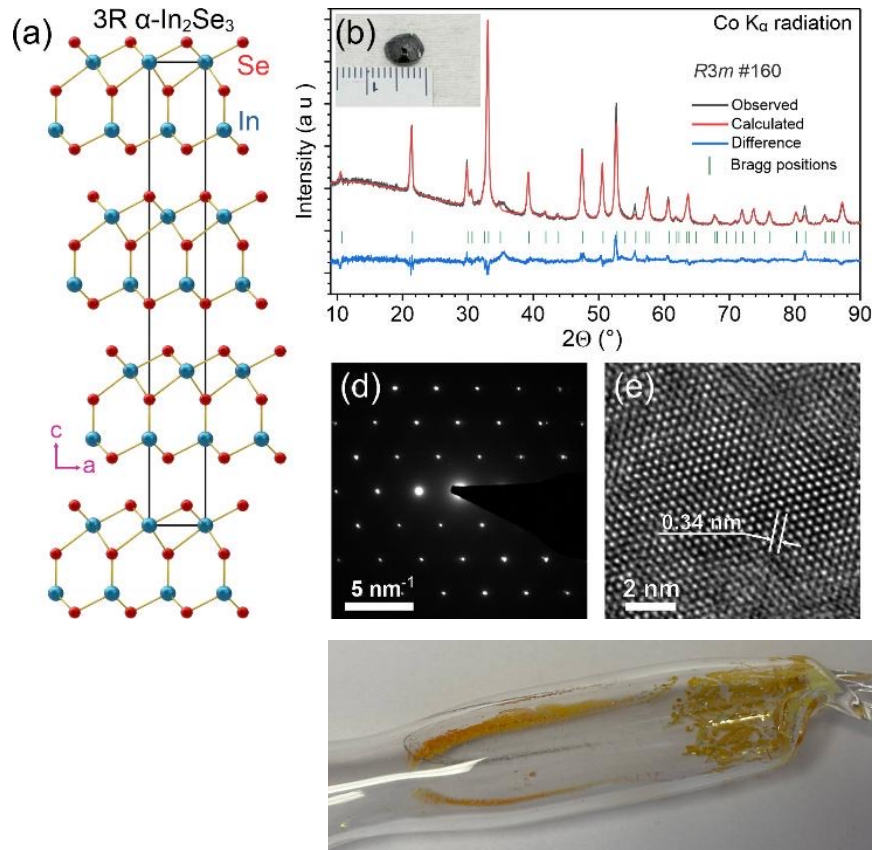
⇒ Perovskite layered materials

2D non-centrosymmetric materials synthesis

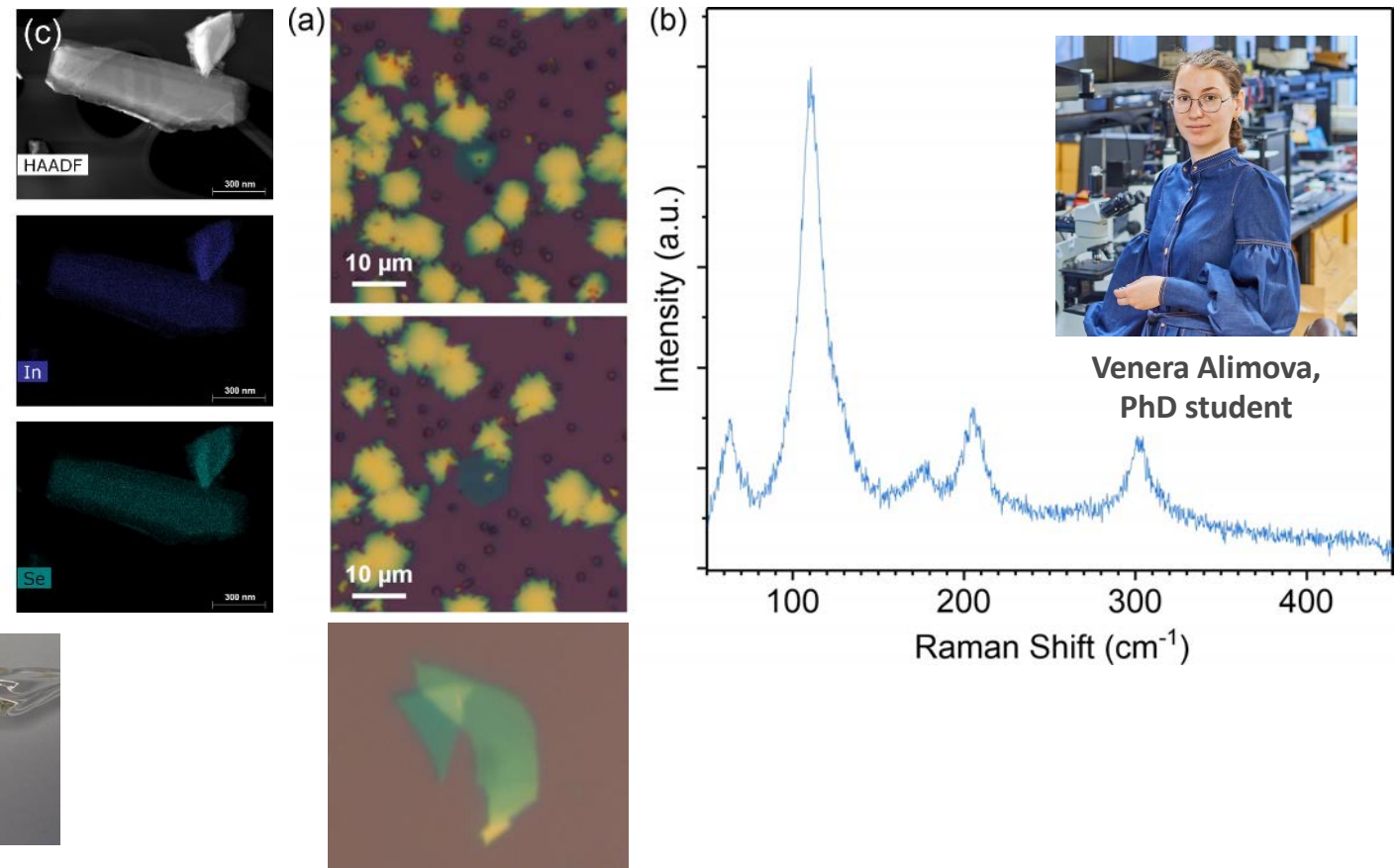
Synthesis of 2D materials (α - In_2Se_3 , β - In_2Se_3 , CIPS)

CVT method

CVD method



CIPS crystals in an ampoule



$\text{MoS}_2/\text{In}_2\text{Se}_3$ heterostructure

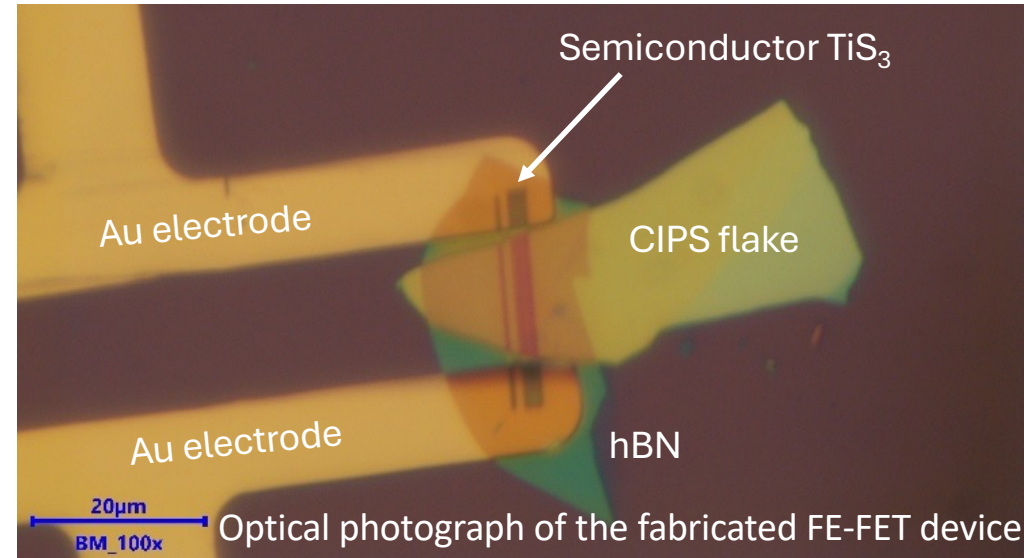


Venera Alimova,
PhD student

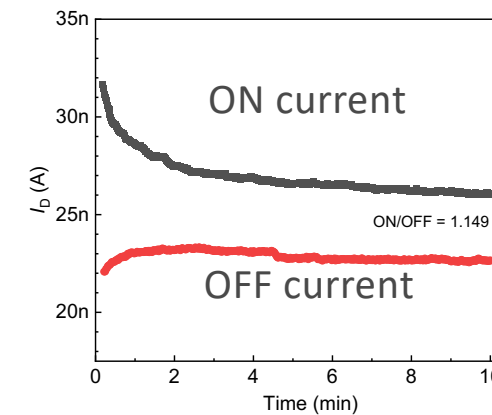
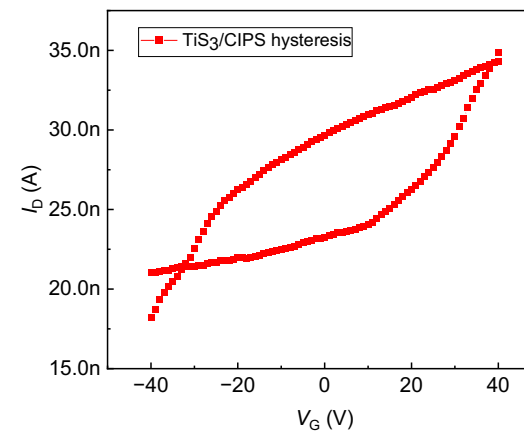
2D heterostructures and devices fabrication



Photo of a flake transfer setup



Ilya Mikhailov,
PhD student



Multiphoton Imaging of In_2Se_3 (Lipatov)



Arik
Ahmed

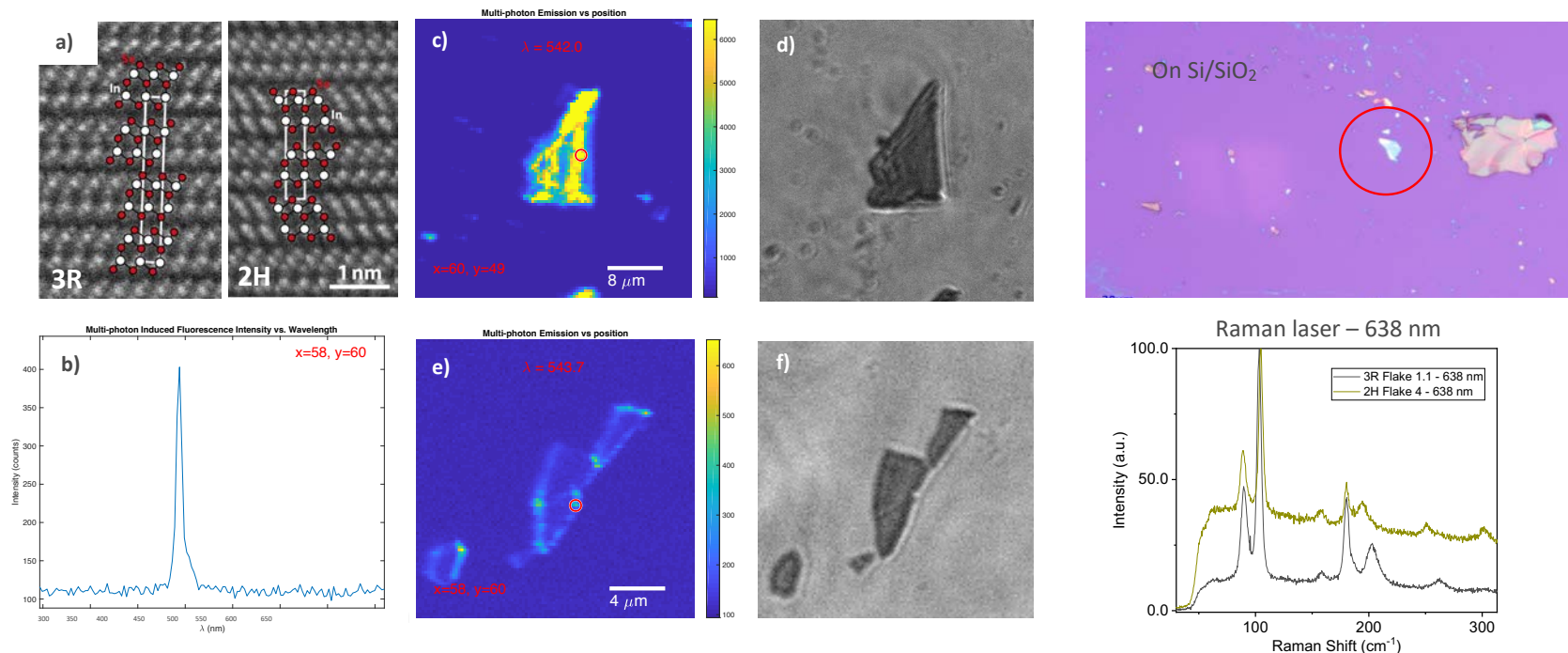


Figure 4: (a) High-resolution high-angle annular dark-field scanning transmission electron microscopy (HAADF-STEM) Z-contrast images of 2H and 3R In_2Se_3 together with the structural models¹. (b) SHG spectrum of In_2Se_3 (c) Spatially resolved SHG from 2H stacked In_2Se_3 (d) White light image of 2H stacked In_2Se_3 (e) Spatially resolved SHG from 3R stacked In_2Se_3 (f) White light image of 3R stacked In_2Se_3

- Predicted to have high $\chi_{ijk}^{(2)}$ and sensitivity to interlayer coupling
- Variation in intensity observed, SHG (3R) 10X SHG (2H)

1. Küpers, M., Konze, P. M., Meledin, A., Mayer, J., Englert, U., Wuttig, M., & Dronskowski, R. (2018). Controlled crystal growth of indium selenide, In_2Se_3 , and the crystal structures of $\alpha\text{-In}_2\text{Se}_3$. *Inorganic chemistry*, 57(18), 11775-11781.

⇒ Imaged SHG in 3R and 2H In_2Se_3

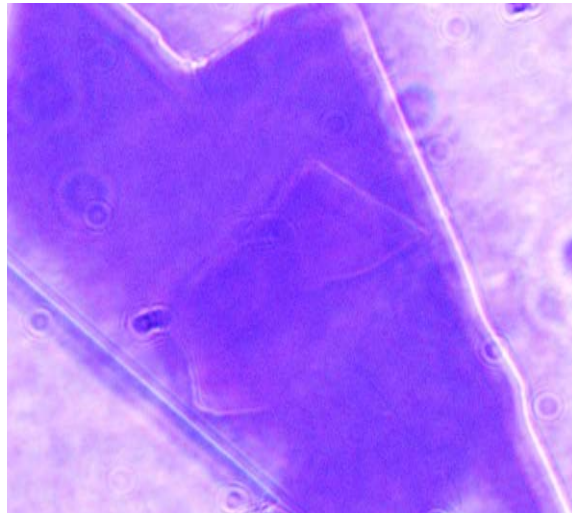
⇒ Edges highlighted, suppressed in 2H

⇒ Stacking determined by Raman

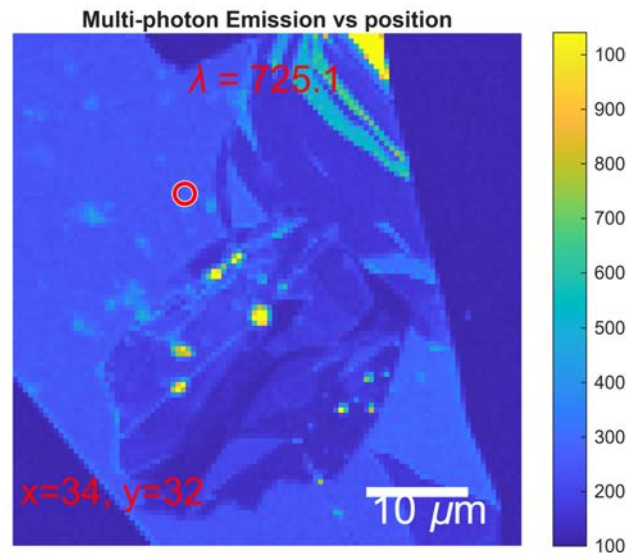
SHG Imaging in CIPS/MoS₂ heterostructure (Lipatov)



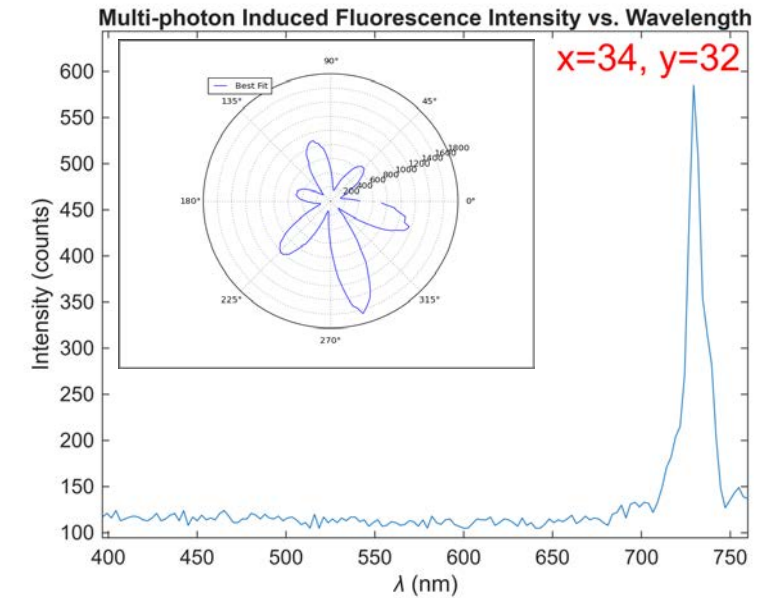
Arik
Ahmed



⇒ CIPS/MoS₂ widefield image



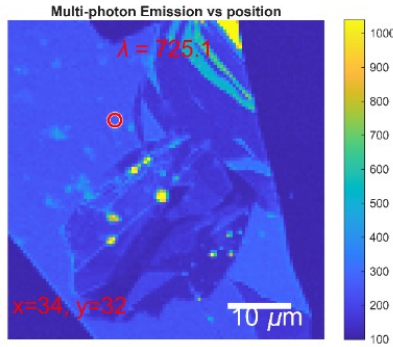
⇒ CIPS/MoS₂ SHG image



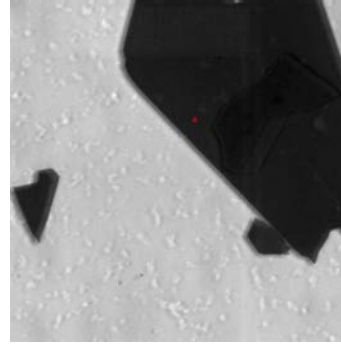
⇒ SHG spectra, and angular dependence

Polarized SHG in CIPS and fits

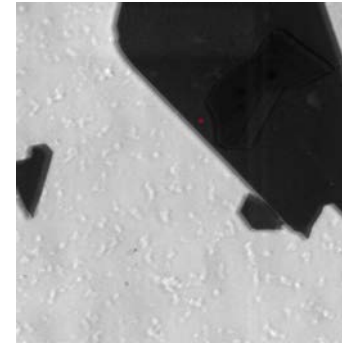
SHG intensity map



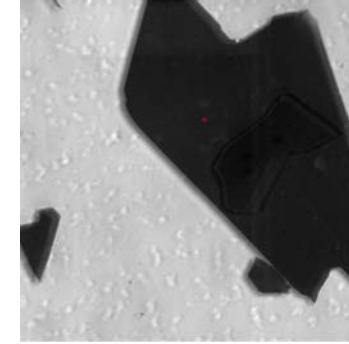
Region 1



Region 2



Region 3



Putting new tensor elements into the formula above, we could get strain-dependent SHG intensity:

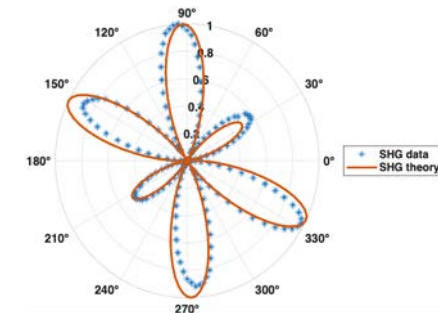
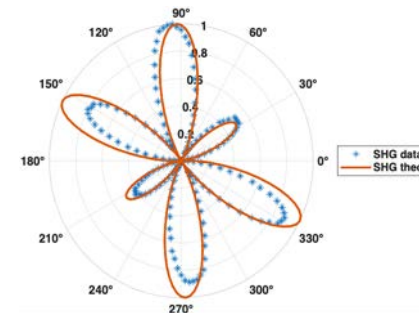
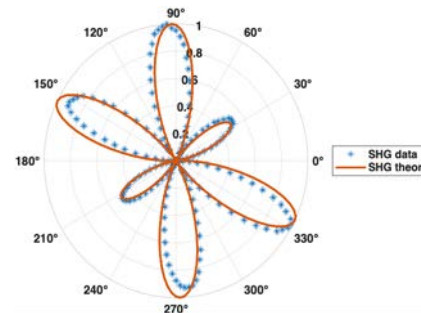
$$I_{\parallel}^{(C_{2v})} = \left[d_{22}^{(D_{3h})} (\cos 3\theta + \epsilon_a (a_1 \cos^3 \theta - b_1 \sin^2 \theta \cos \theta - 2c_1 \sin^2 \theta \cos \theta)) \right]^2$$

$$I_{\perp}^{(C_{2v})} = \left[d_{22}^{(D_{3h})} (\sin 3\theta + \epsilon_a (a_1 \sin \theta \cos^2 \theta - b_1 \sin^3 \theta + 2c_1 \sin \theta \cos^2 \theta)) \right]^2 \quad (6)$$

where θ is the included angle between unique armchair crystal orientation which remains a C_2 axis. Under ϵ_z , we would obtain the same formula shown above with ϵ_a , a_1 , b_1 , c_1 replaced by ϵ_z , a_2 , b_2 , c_2 respectively.

S9. Parameters used to characterize strain-dependent $\vec{d}$.

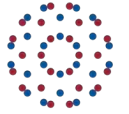
Table S1 Parameters used to characterize strain magnitude			
	a_i	b_i	c_i
$i = 1$	-0.31	-0.19	-0.17
$i = 2$	-0.12	-0.26	-0.25



Using the parallel I_{SHG} formula from the supp. info of Ref.1 and inputting the same a_1 , b_1 and c_1 , an offset of 33 degrees, and an ϵ_a value of 1.5 (i.e. 1.5% strain). The formula assumes the strain is aligned with the armchair axis.

1. Liang, J., Zhang, J., Li, Z., Hong, H., Wang, J., Zhang, Z., ... & Yu, D. (2017). Monitoring local strain vector in atomic-layered MoSe2 by second-harmonic generation. *Nano letters*, 17(12), 7539-7543.

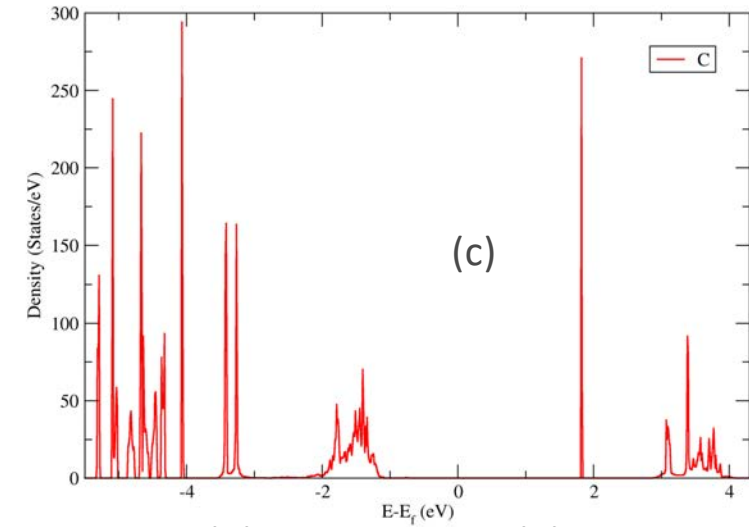
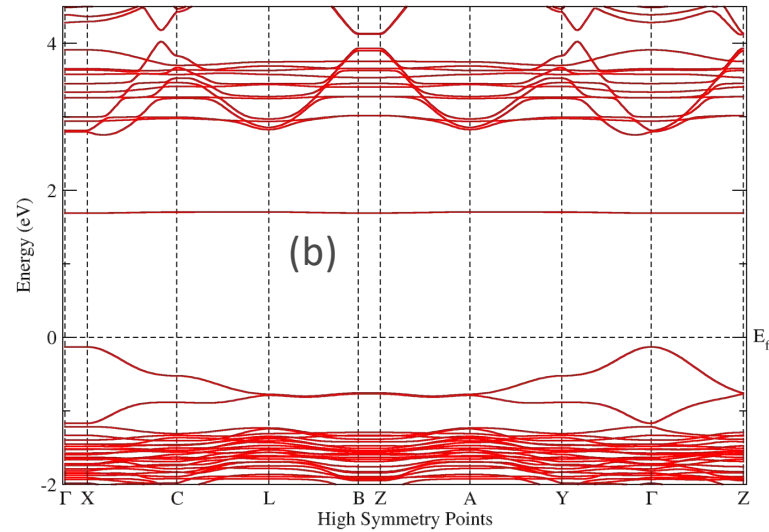
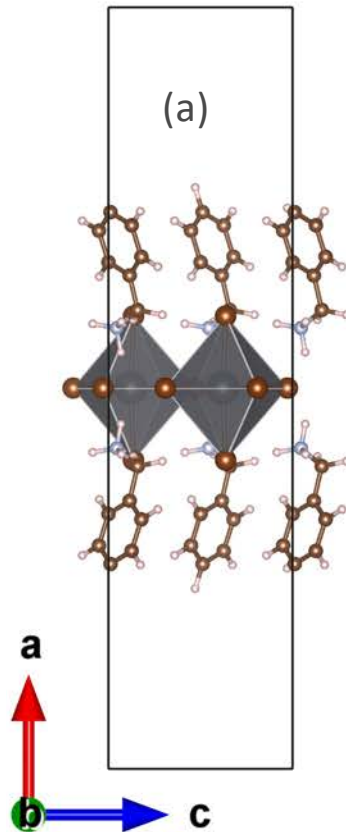
Band structure of monolayer 2D (*Benzylammonium*)₂PbBr₄ Perovskite (Paudel)



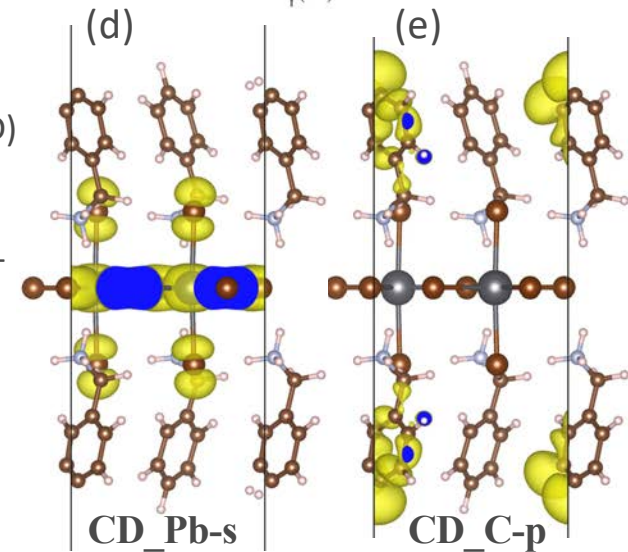
MonArk
Quantum Foundry



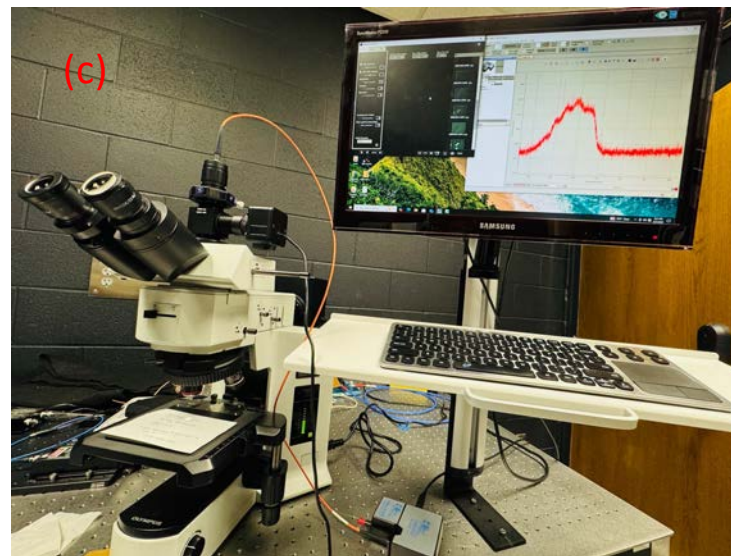
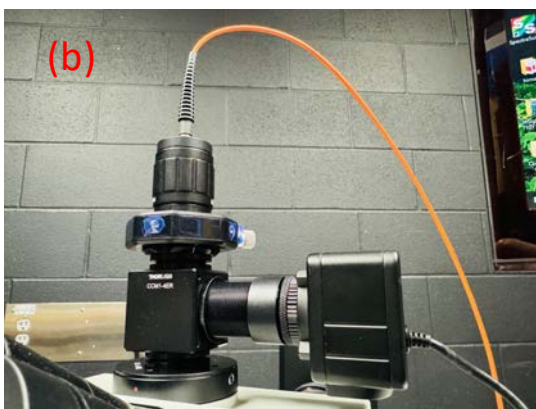
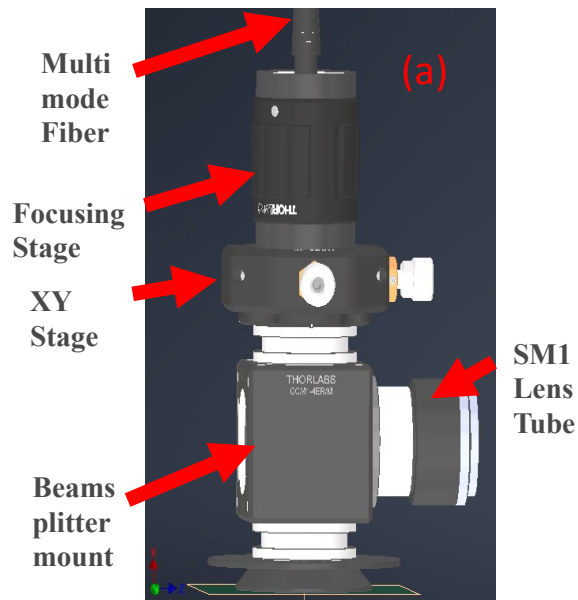
Himali
Oli



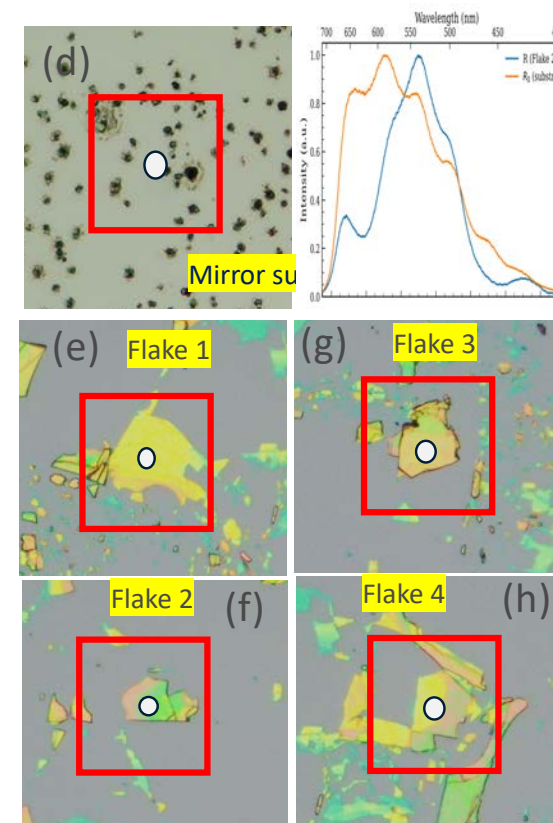
- Fig. (a) represents the monolayer crystal structure
- Fig. (b), (c), (d), and (e) show the DFT results: band, atom-resolved density of states on C-atom, charge densities (CD) of Pb-s and C-p orbitals resp. calculated using VASP
- Results identify the presence of optically inactive surface state in monolayer slab, which are attributed to surface C-atoms p-orbitals that are separated by a large distance (> 10 Å) in real space and do not overlap with Pb-s/p states forming the valence bands resulting in the absence of an optical signal in the linear regime



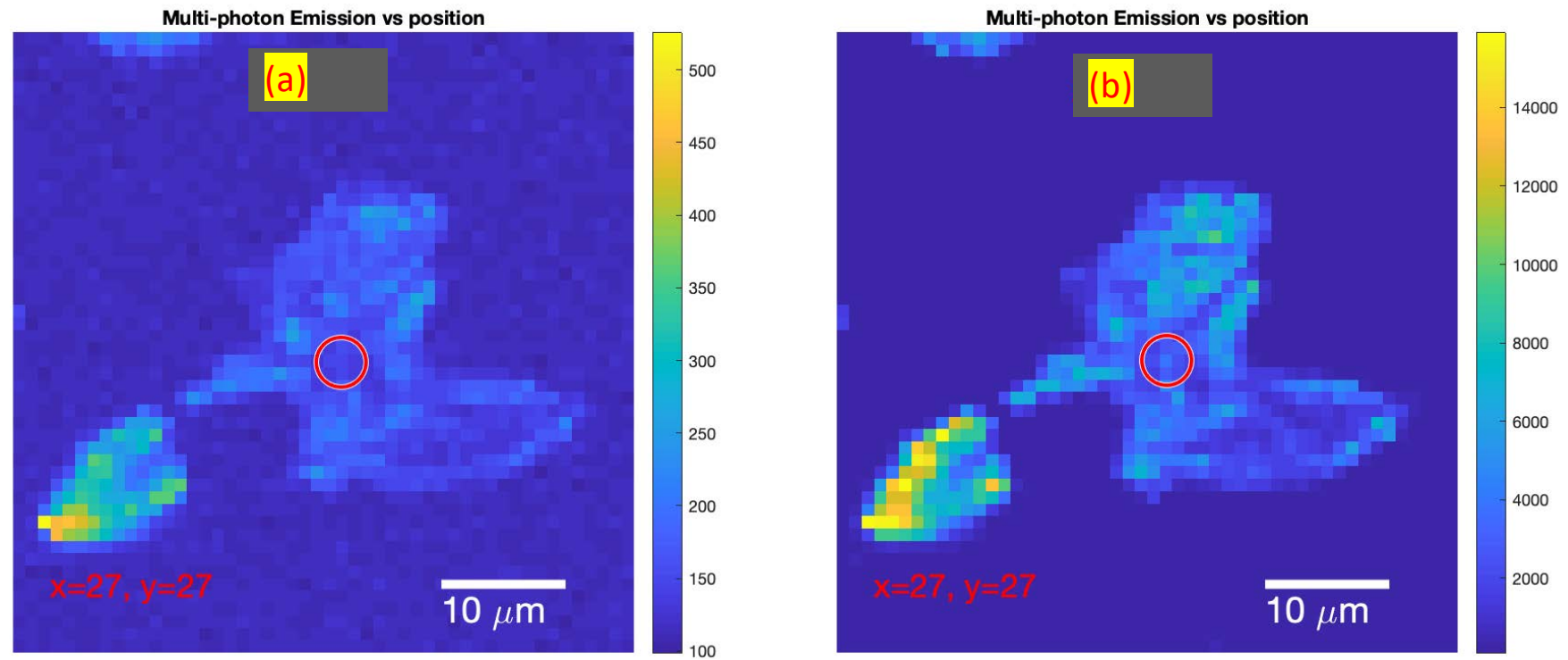
Reflectance lab set up and optical microscope images



- Fig. (a), (b), and (c) represent setup designed in Autodesk Inventor, setup after assembling the parts, and the overall experimental lab setup respectively
- Fig. (d) represents the optical microscope image of mirror substrate
- Fig. (e), (f), (g), and (h) represent the mechanically exfoliated optical microscope image of different flakes of 2D $(\text{Benzylammonium})_2 \text{PbBr}_4$ perovskite



SHG in 2D(*Benzylammonium*)₂PbBr₄ Perovskite



- Fig. (a) and (b) display a map of multi-photon emission vs position with & without grating respectively. It shows the spatial distribution of multi-photon emissions within the sample.

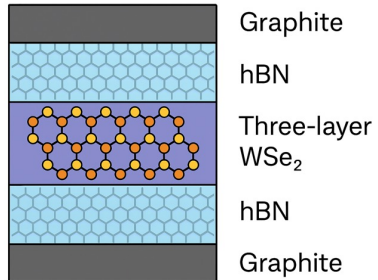
Tri-layer WSe₂ device fabricated at MonArk



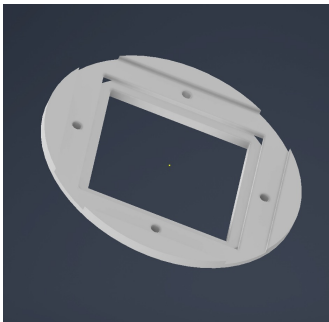
Arik
Ahmed

a

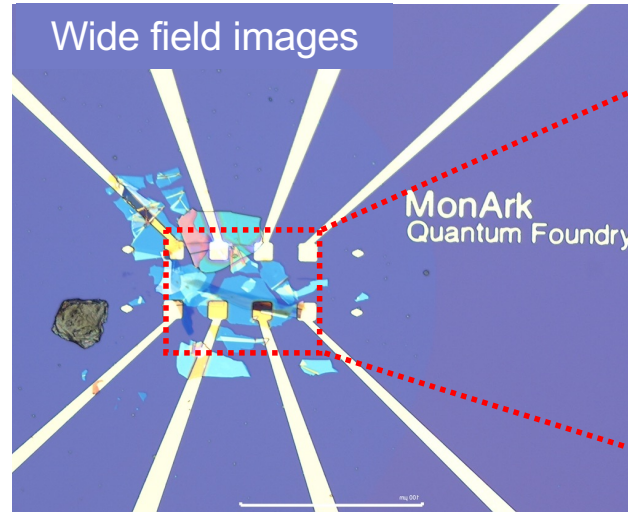
Schematic of
device



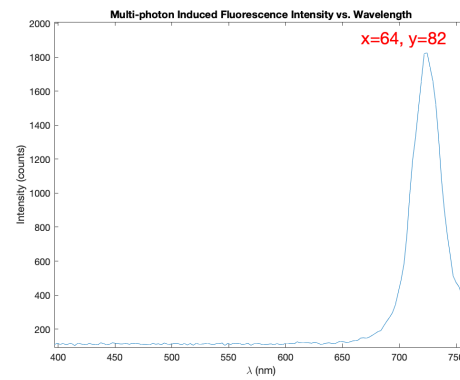
Sample holder



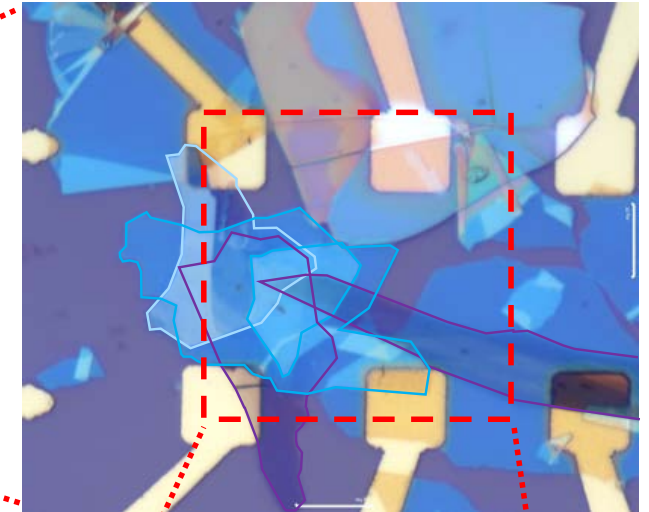
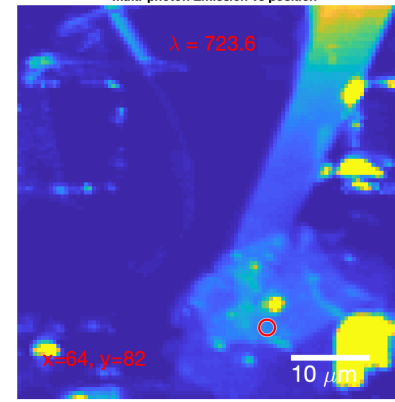
b



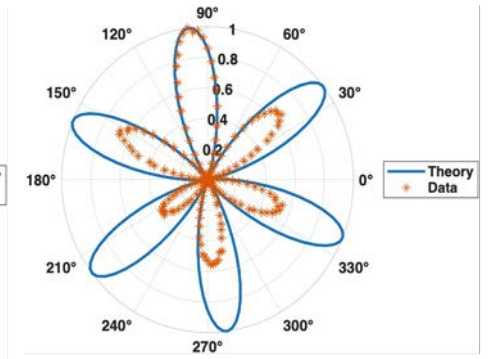
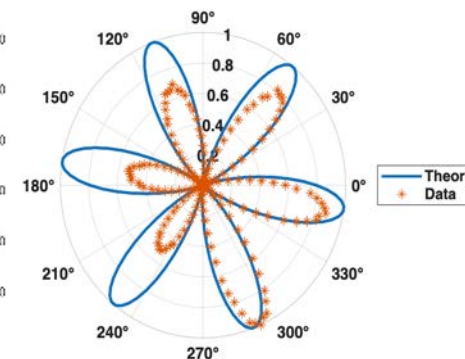
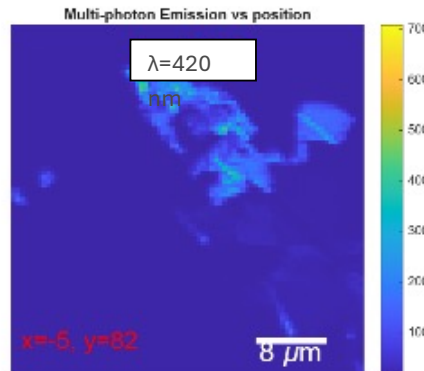
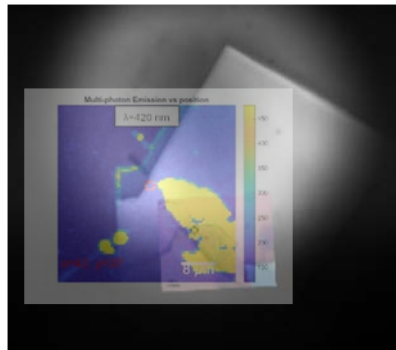
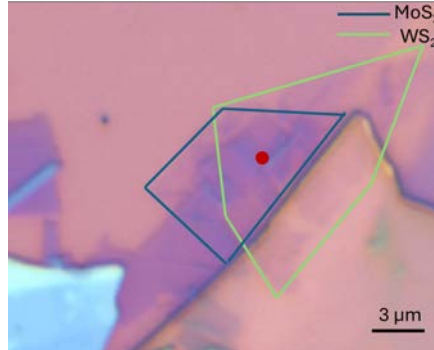
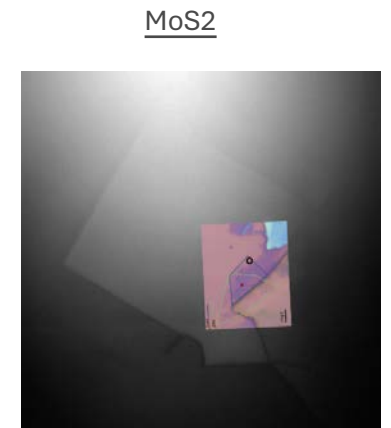
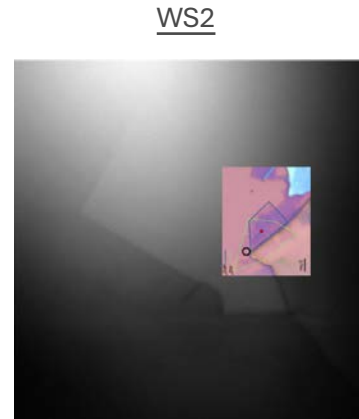
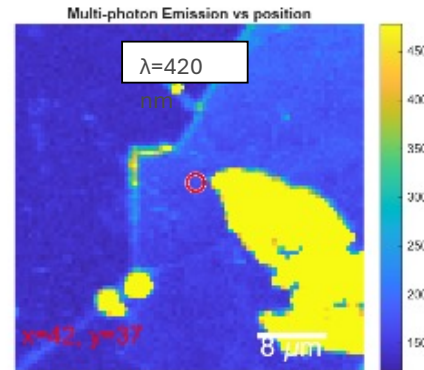
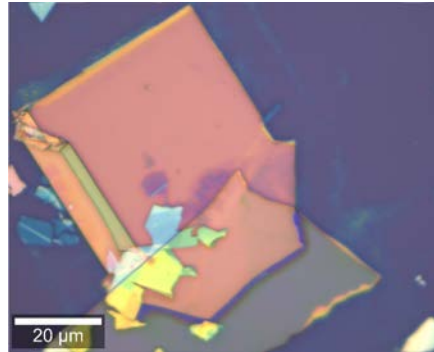
Multiphoton spectra



SHG image



Twist angle in MoS₂/WSe₂ heterojunction device (Behura)

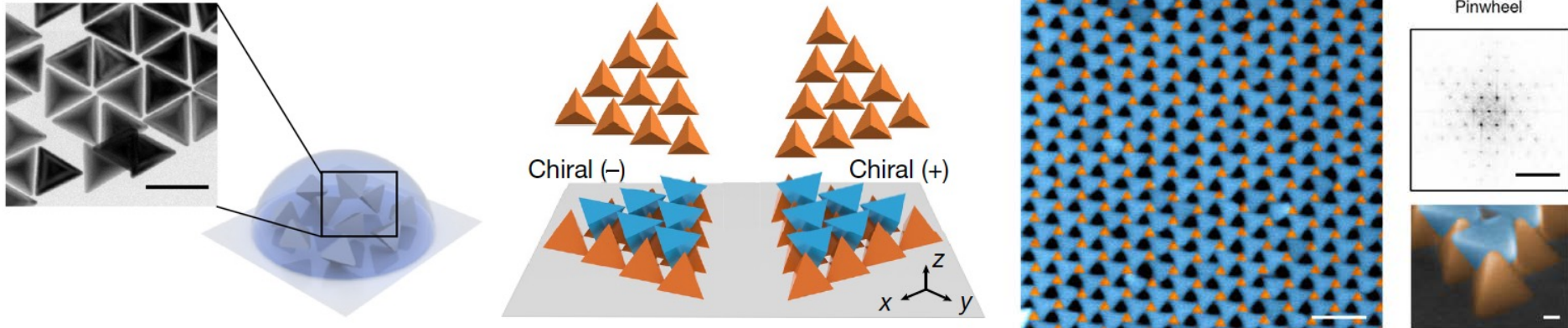


→ SHG spectroscopy on the MoS₂-WS₂ sample to determine twist angle between the MoS₂/WSe₂ bilayer

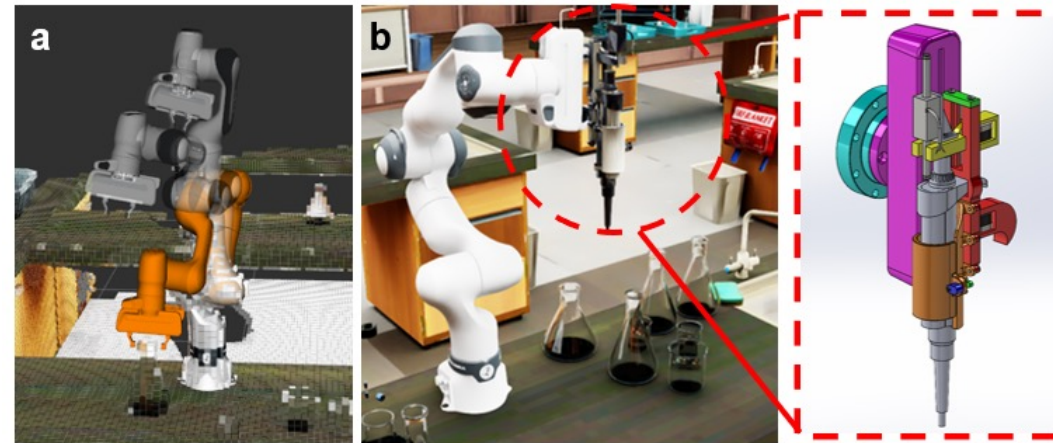
Self-assembled metasurfaces and Robotic Chemistry



Shan Zhou (2022)



Left to right: Colloidal self-assembled tetrahedra, chiral assembly via enantiomeric coupling and SEM image of chiral metasurface.



Left to right: Simulation of robotic arm, photo of arm learning chemistry and SEM CAD rendering of custom pipette actuator.

Infrastructure Improvements

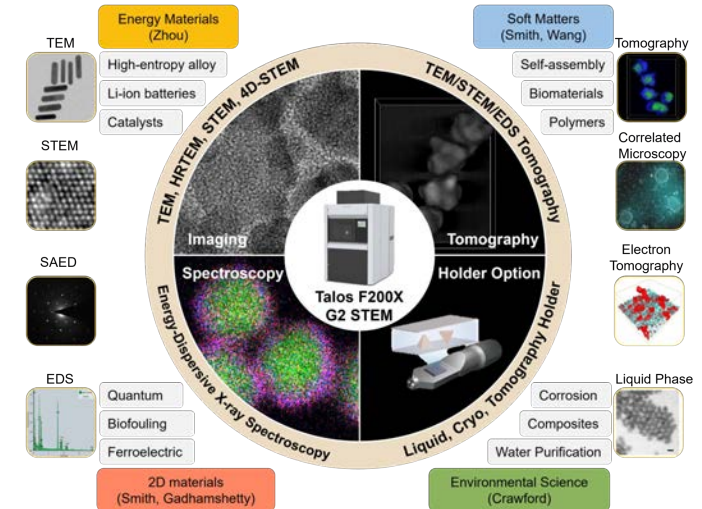
**9 Tesla Cryogen Free (2025)
Physical Property Measurement System**



**Nano-Frazor Photothermal
nano-Lithography (2025)**



TEM MRI (2025)



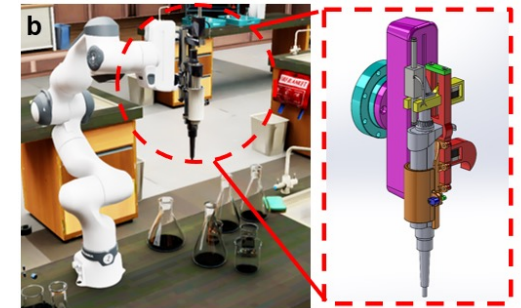
Quantum Mechanics Laboratory Kit (2024)



Quantum Cascade Laser and Near-field Microscope (2025)



6 DOF Robotic Manipulator (2026)



Conclusions and acknowledgements



Arik
Ahmed



Himal
Oli



Junming
Yue



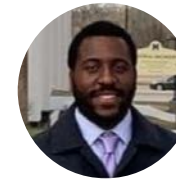
Tochukwu
Emeakaroha



Kim Yip
Chiok



Tolulope
Ajuwon



Yoseph
Loyd



Saif
Bijoy

- Spatially-resolved, second harmonic and multiphoton luminescence imaged in 2D materials coupled with theory and materials synthesis.
- Ongoing investigations in a palette of 2D materials, heterostructures and metasurfaces.
- Future work will focus on heterostructures, including meta-materials.



IONQ



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