

Machine Learning Does It and Does It Better: Unearthing Primordial Dark-Matter Velocities from the Matter Power Spectrum

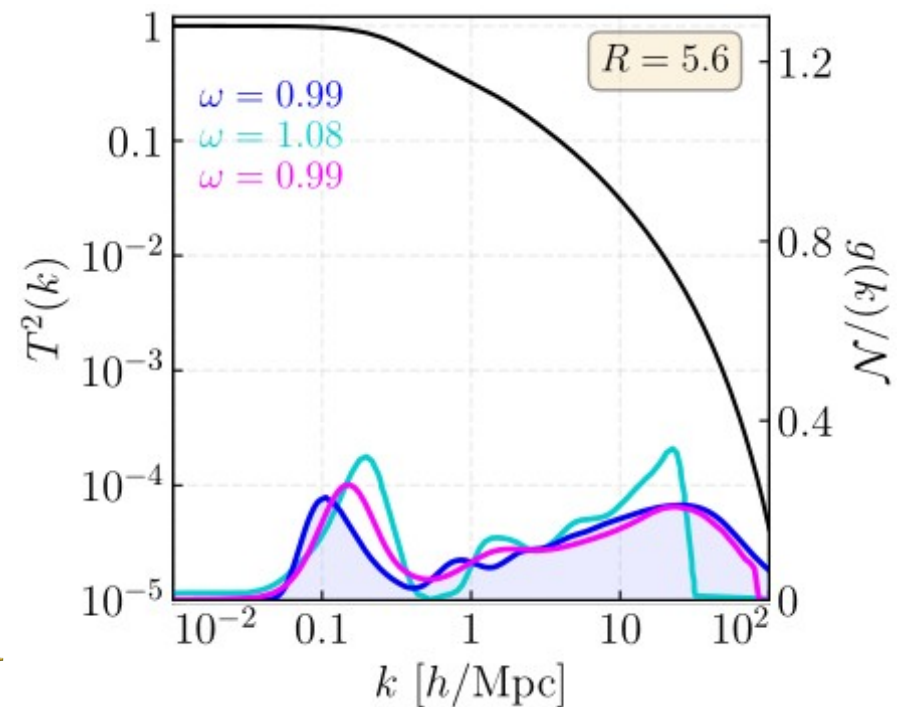
Brooks Thomas

LAFAYETTE
COLLEGE

**Based on work done
in collaboration with:**

• Keith Dienes, Jessica Howard, Fei Huang, Yuanzhen Li [arXiv:2606.13527]

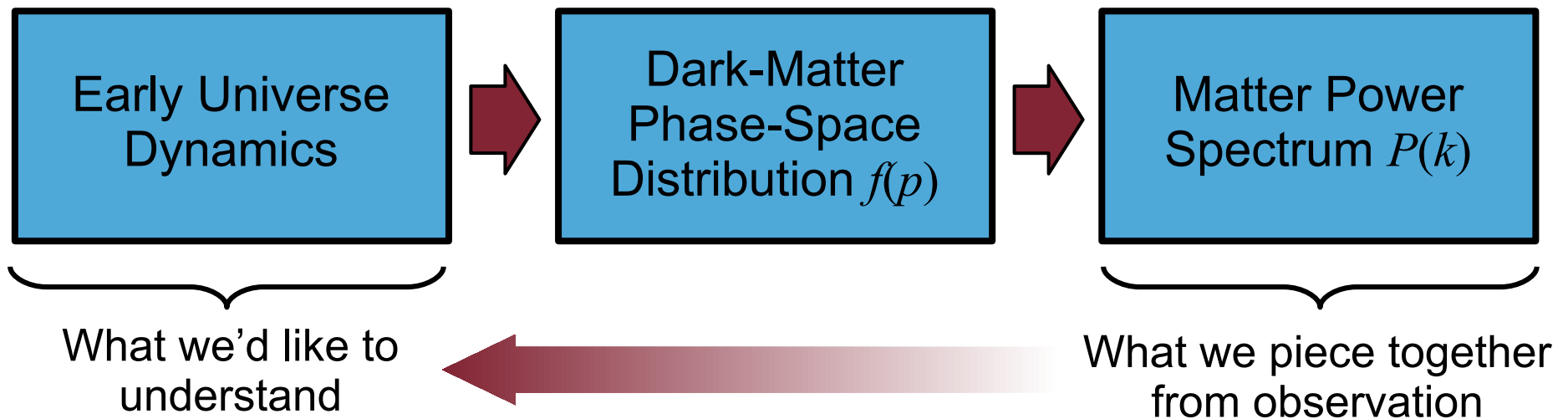
This research is supported in part by 



CETUP* Dark-Matter Workshop 2026, June 30th, 2026

The Basic Question

- The early-universe dynamics which produces the dark matter gives rise to a particular dark-matter phase-space distribution $f(p)$. This, in turn, affects the shape of the matter power spectrum $P(k)$.



To what extent can we work backwards and **reconstruct** the properties of $f(p)$ – and the dynamics that gave rise to it – from information encoded in $P(k)$?

- While the maps from the underlying physics to $f(p)$, and from $f(p)$ to $P(k)$ are clearly not invertible, it is nevertheless possible to “work backwards” and obtain substantial information about the dark sector from information contained in the matter power spectrum.

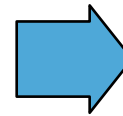
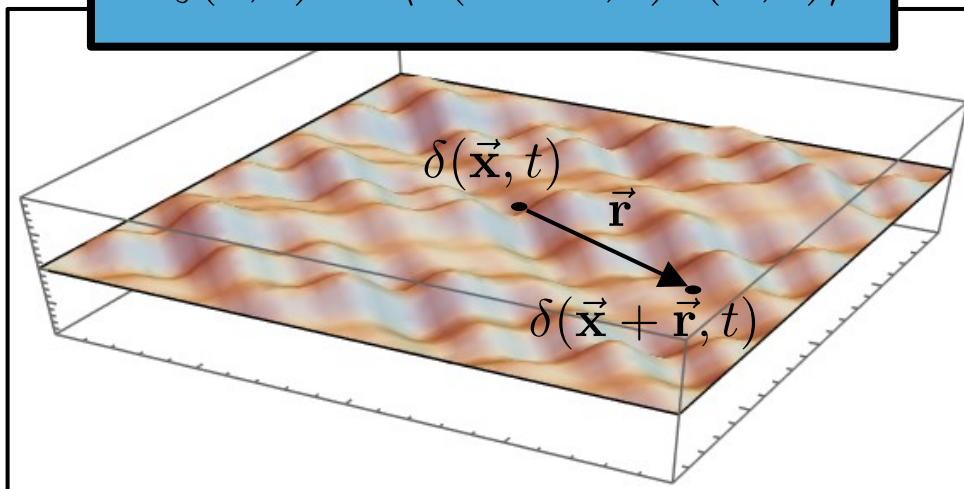
Matter Power Spectrum

- The **matter power spectrum** encapsulates information about the spatial distribution of matter in our universe.

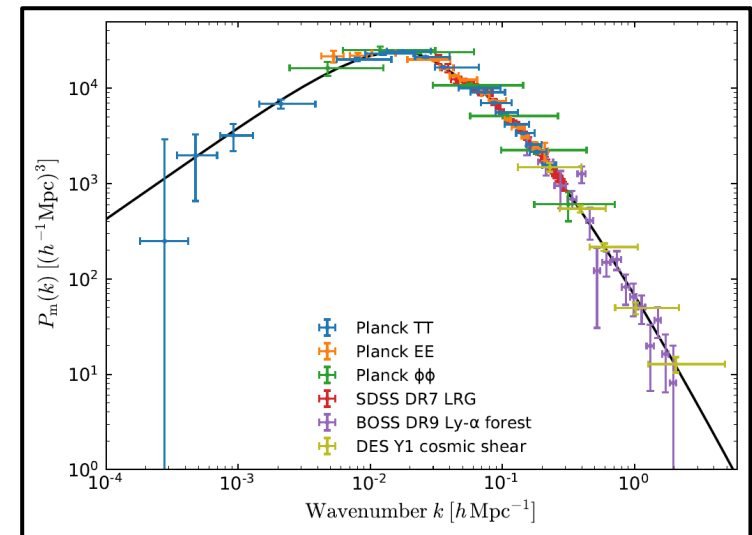
$$P(k, t) \equiv 4\pi \int dr r^2 \frac{\sin(kr)}{kr} \xi(r, t)$$

Two-point correlation function for the fractional matter overdensity

$$\xi(\vec{r}, t) = \langle \delta(\vec{x} + \vec{r}, t) \delta(\vec{x}, t) \rangle$$



Linear Matter Power Spectrum

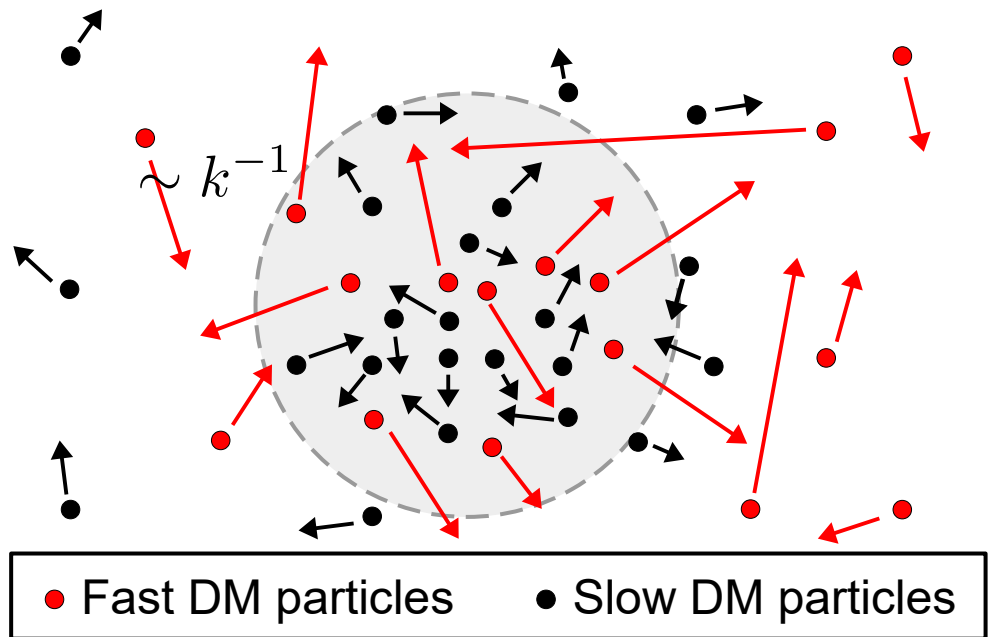
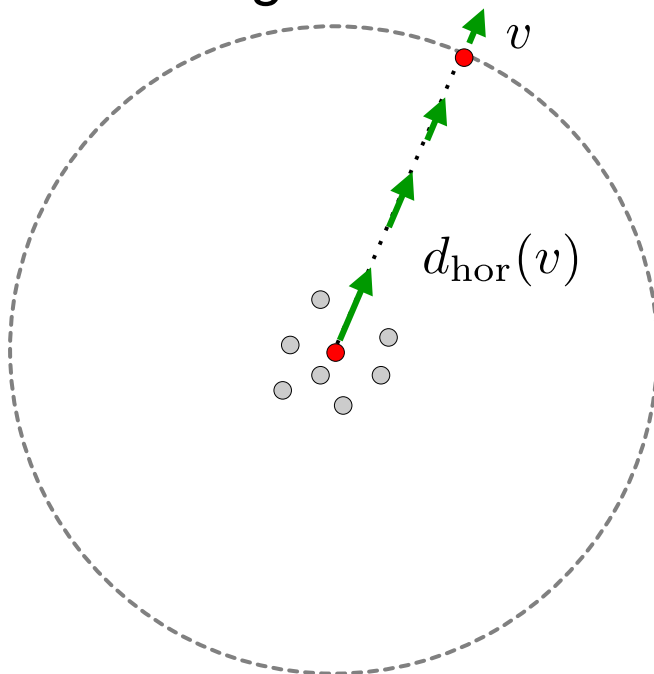


- Not directly observable, but can be probed using CMB data, Lyman- α -forest data, 21-cm forest, etc., up to $k \sim \mathcal{O}(100) \text{ Mpc}^{-1}$.
- Robust predictions** for $P(k)$ can be reliably obtained – at least within the linear regime – over a broad range of redshifts through use of numerical tools like CLASS.

Free Streaming and Dark-Matter Speeds

- The properties of the dark matter can impact $P(k)$ in a variety of ways.
- Deviations from the shape that $P(k)$ takes relative to its shape $P_{\text{CDM}}(k)$ in the case of ultra-cold dark-matter with only gravitational interactions are parametrized by the **transfer function** $T(k)$.
- One of the most important of these is **free-streaming** due to **particle horizons** when the dark matter is not ultra-cold.
- Our focus going forward will be on the impact $f(p)$ has on $P(k)$ through free-streaming.

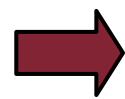
$$T^2(k) = \frac{P(k)}{P_{\text{CDM}}(k)}$$



Describing the Phase-Space Distribution

- We're going to find it useful to describe the DM phase-space distribution in a slightly atypical way.

$$\begin{aligned} x(t) &= x(t') \frac{a(t)}{a(t')} \\ p(t) &= p(t') \frac{a(t')}{a(t)} \end{aligned}$$



$$\frac{d \log(p)}{dt} = -H(t)$$

Number of internal degrees of freedom

- Physical number density:

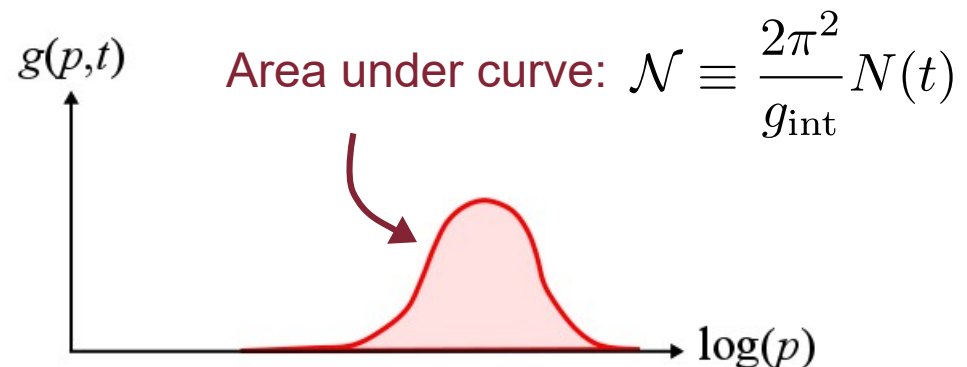
$$n(t) = \frac{g_{\text{int}}}{2\pi^2} \int dp p^2 f(p, t)$$

- Comoving number density:

$$N(t) = n(t) a^3(t) = \frac{g_{\text{int}}}{2\pi^2} \int d \log p \, p^3 a^3 f(p, t)$$

- This motivates us define the comoving “log-space” DM phase-space distribution $g(p, t)$:

$$g(p, t) = a^3(t) p^3 f(p, t)$$



The Cosmological Conveyor Belt

- In the absence of sources/sinks, the total number of particles $N(t') = N(t)$ is conserved. In this case, $g(p,t)$ evolves according to the relation

$$g(p(t'), t') = g(p(t), t)$$

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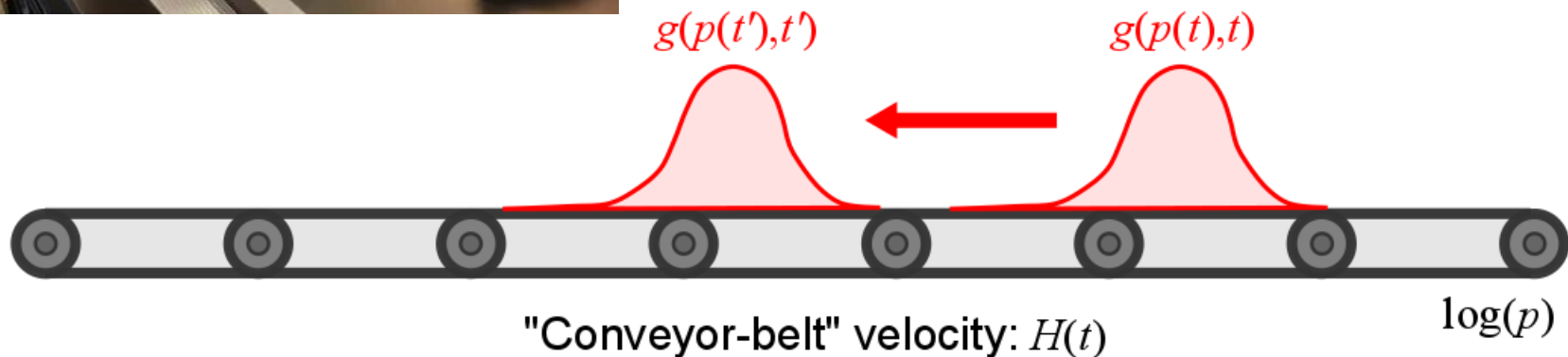
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- In other words, $g(p,t)$ is carried along like a cucumber on a **conveyor belt**, moving to lower and lower $\log(p)$ at speed $|d\log(p)/dt| = H(t)$, but retaining a fixed shape.



The Usual Approach

- The free-streaming horizon for a particle of mass m and present-day momentum p in an expanding universe is

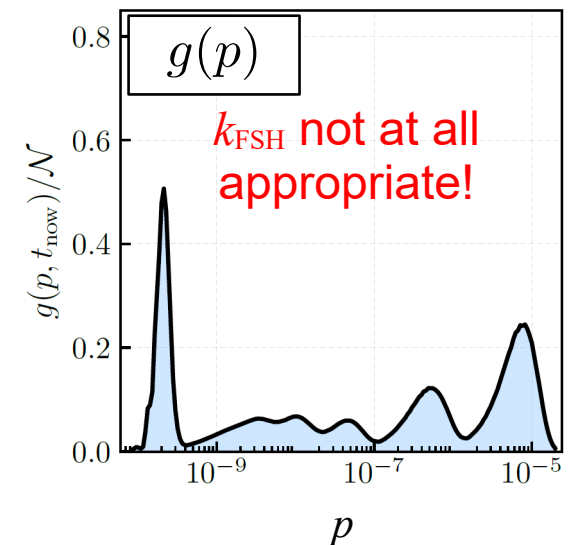
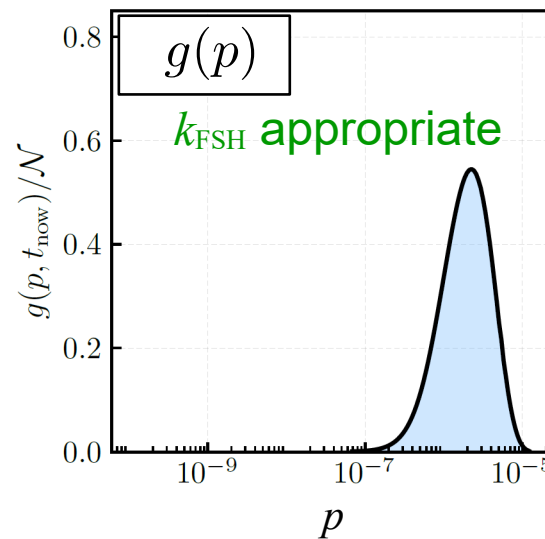
$$k_{\text{hor}}(p) \equiv \xi \left[\int_{t_{\text{prod}}}^t v(p, t) \frac{dt}{a(t)} \right]^{-1} = \xi \left[\int_{a_{\text{prod}}}^1 \frac{da}{Ha^2} \frac{p}{\sqrt{p^2 + m^2 a^2}} \right]^{-1}$$

$\mathcal{O}(1)$ constant

- The usual approach (e.g., for warm DM) is to define a single “free-streaming-horizon” scale k_{FSH} using the average DM velocity $\langle v(t) \rangle$:

$$k_{\text{FSH}} \sim \left[\int_{t_{\text{prod}}}^t \langle v(t) \rangle \frac{dt}{a(t)} \right]^{-1}$$

- This works reasonably well when $g(p)$ is unimodal and narrow, but not when $g(p)$ is multimodal and/or broad.



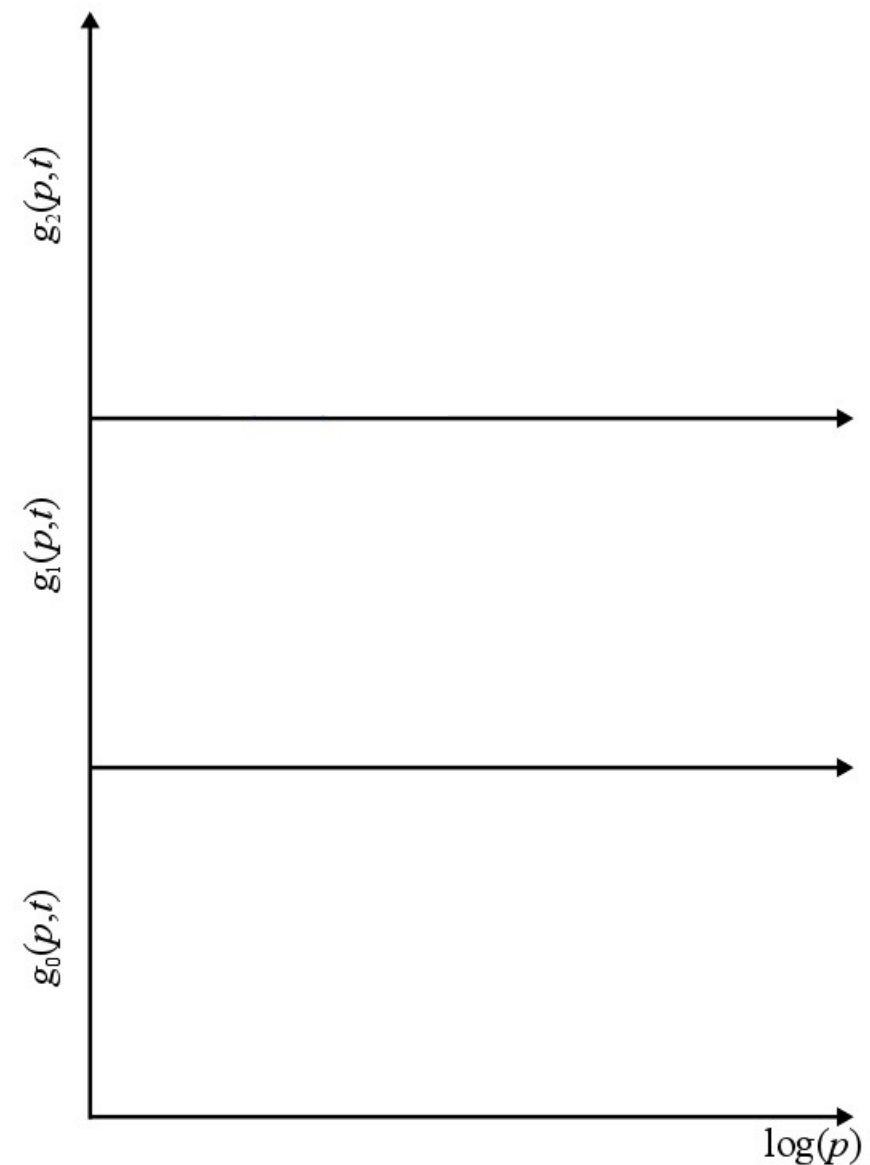
Dark-Sector Dynamics and Non-Trivial $g(p)$

- To motivate how more complicated $g(p)$ distributions might arise, we can consider a DM-production scenario involving *particle decays*.

Dark-Sector Dynamics and Non-Trivial $g(p)$

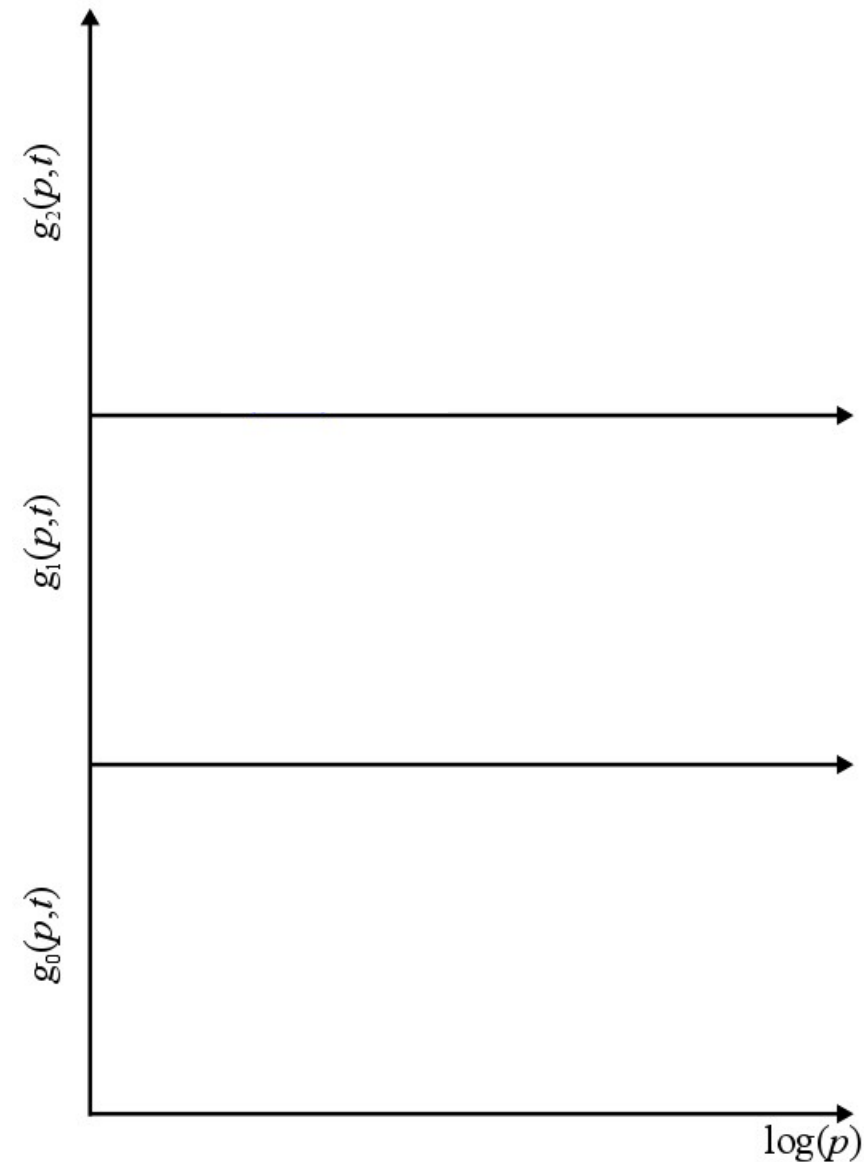
- To motivate how more complicated $g(p)$ distributions might arise, we can consider a DM-production scenario involving particle decays.

- As an example, let's consider a dark sector involving three particle species ϕ_0 , ϕ_1 , and ϕ_2 (all scalar fields) with similar quantum numbers and masses $m_2 > 2m_1 > 4m_0$.



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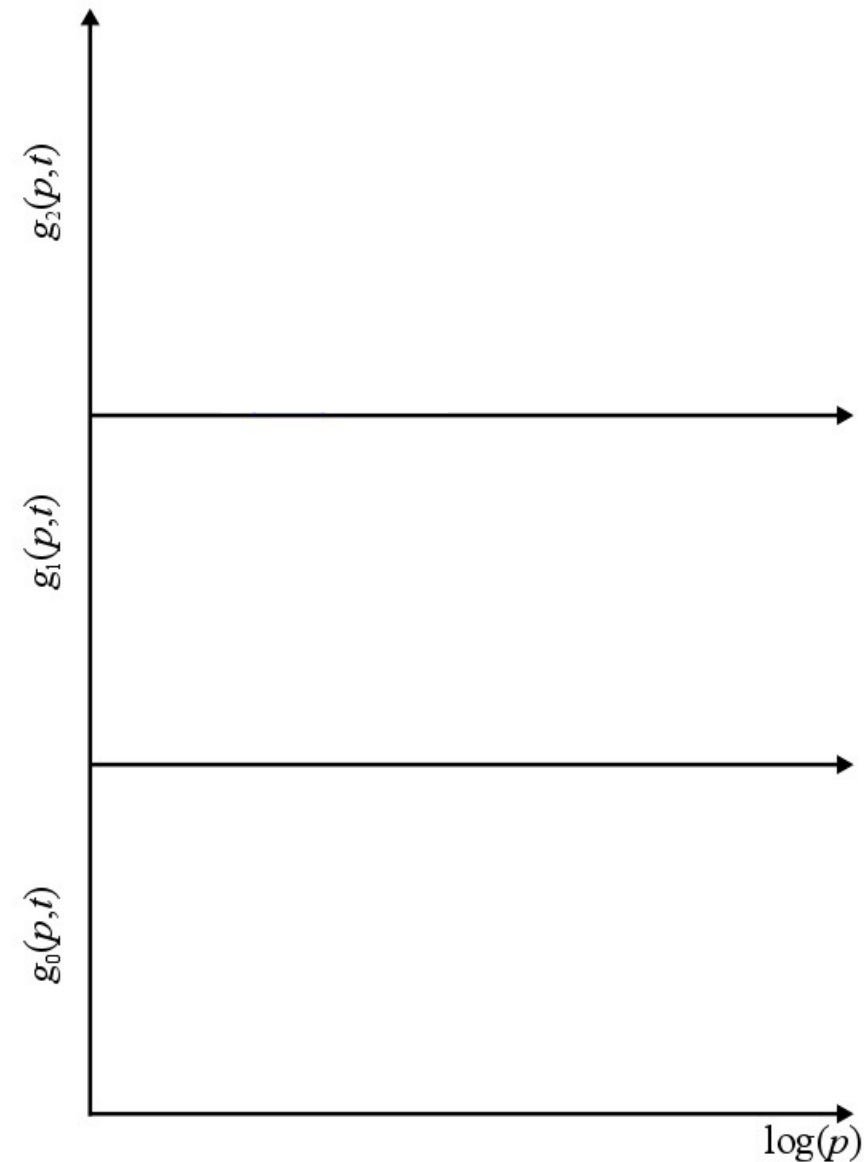
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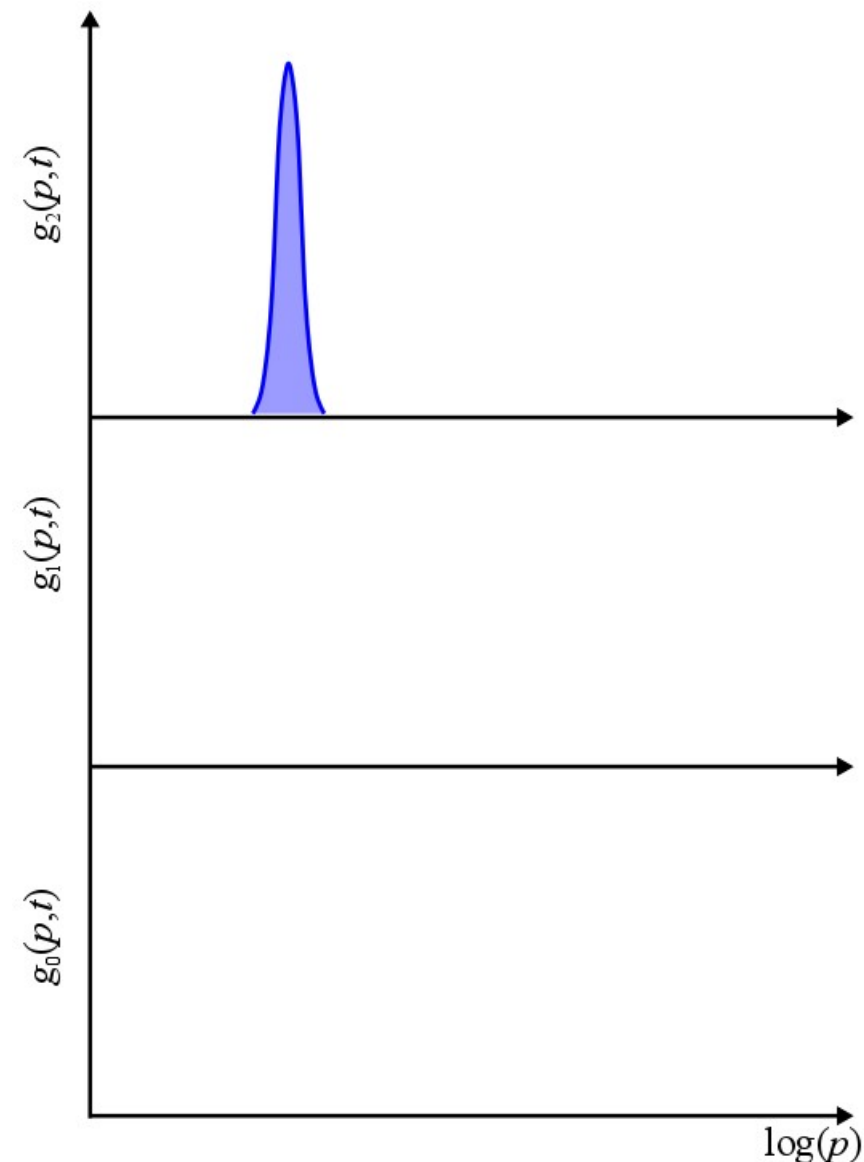
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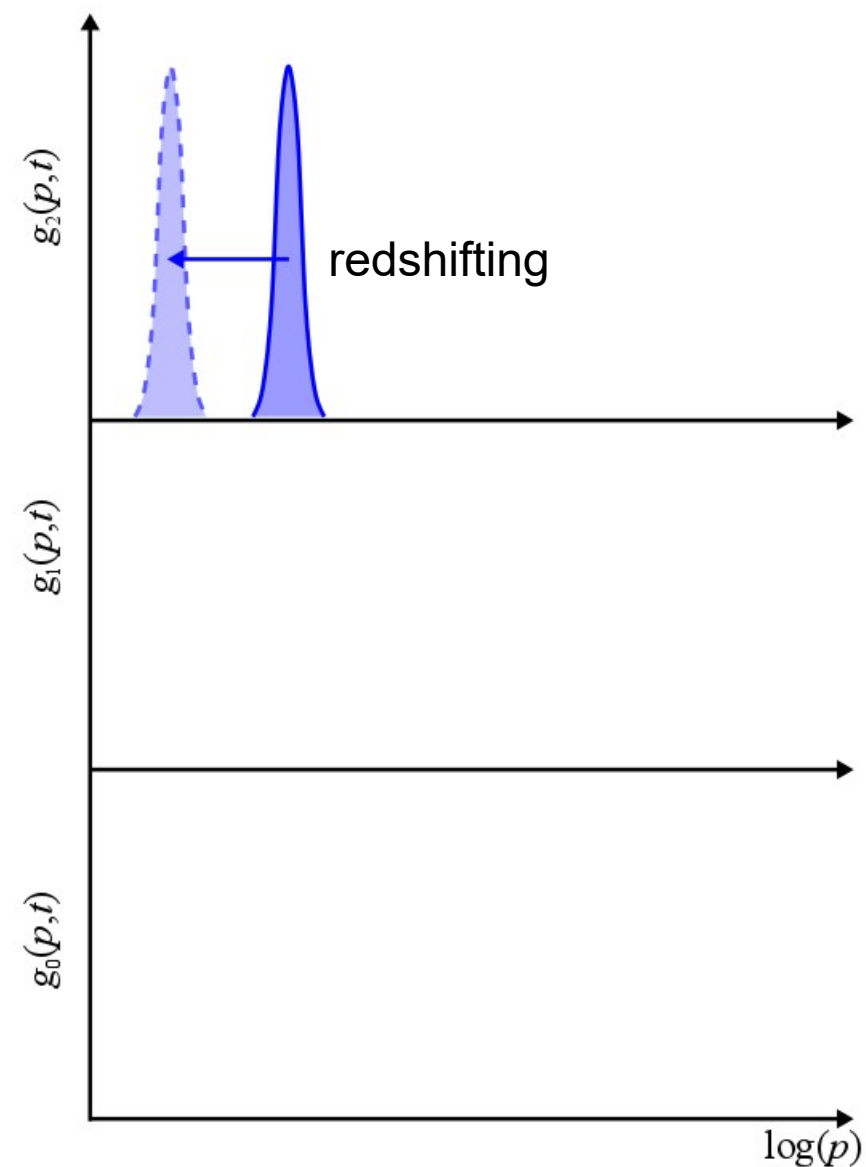
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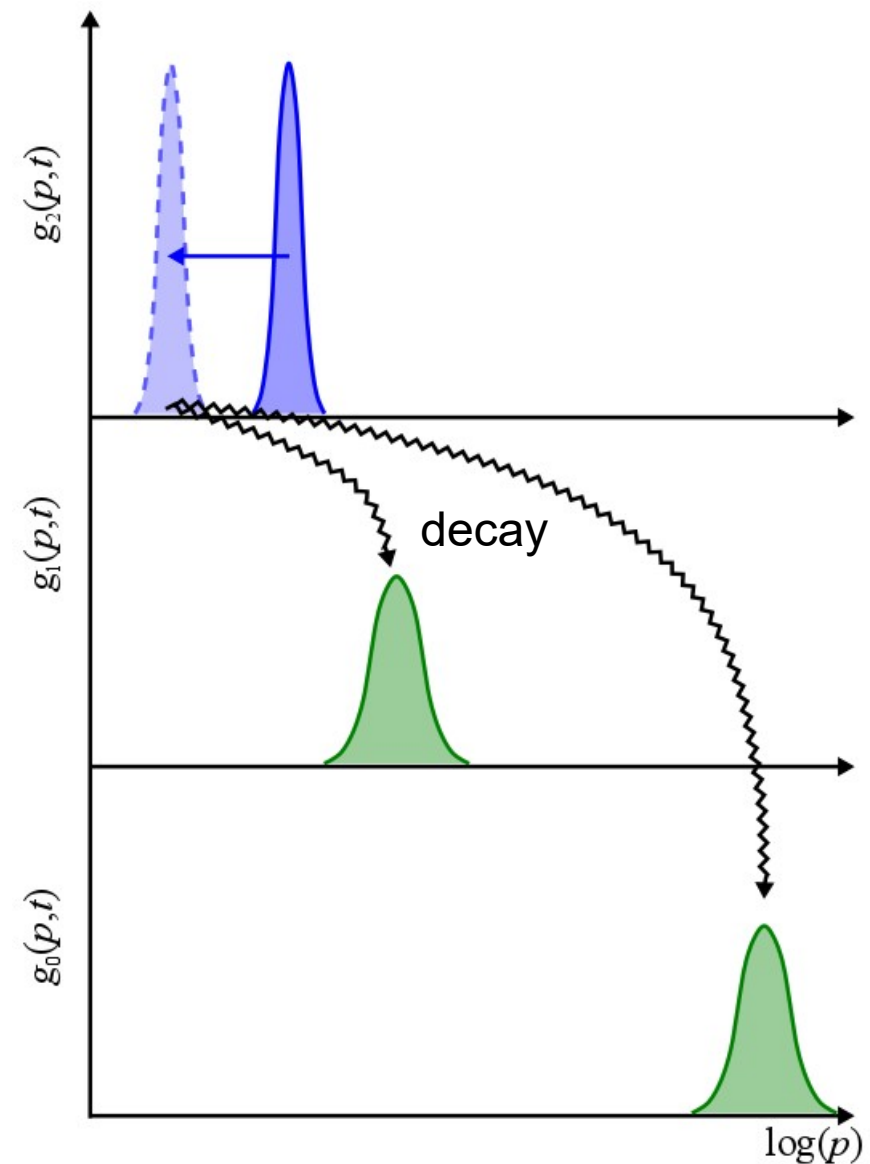
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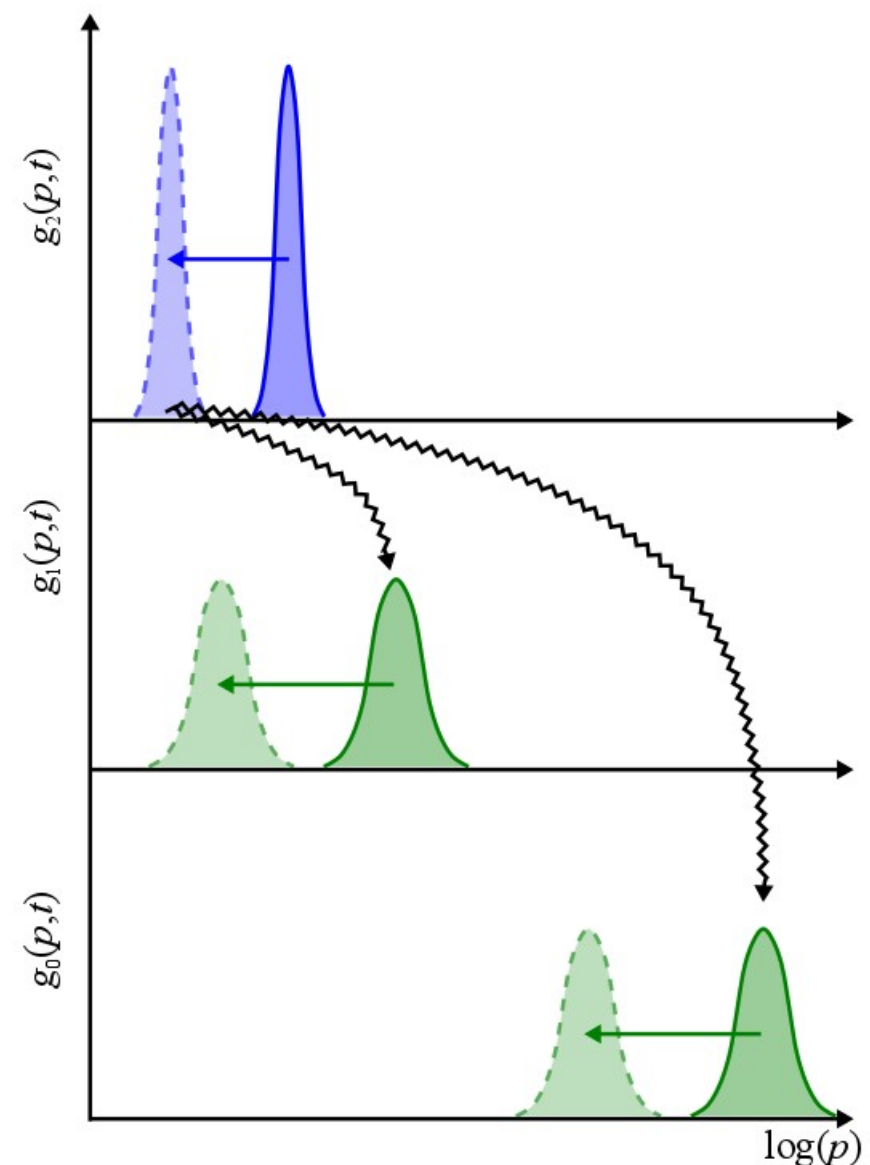
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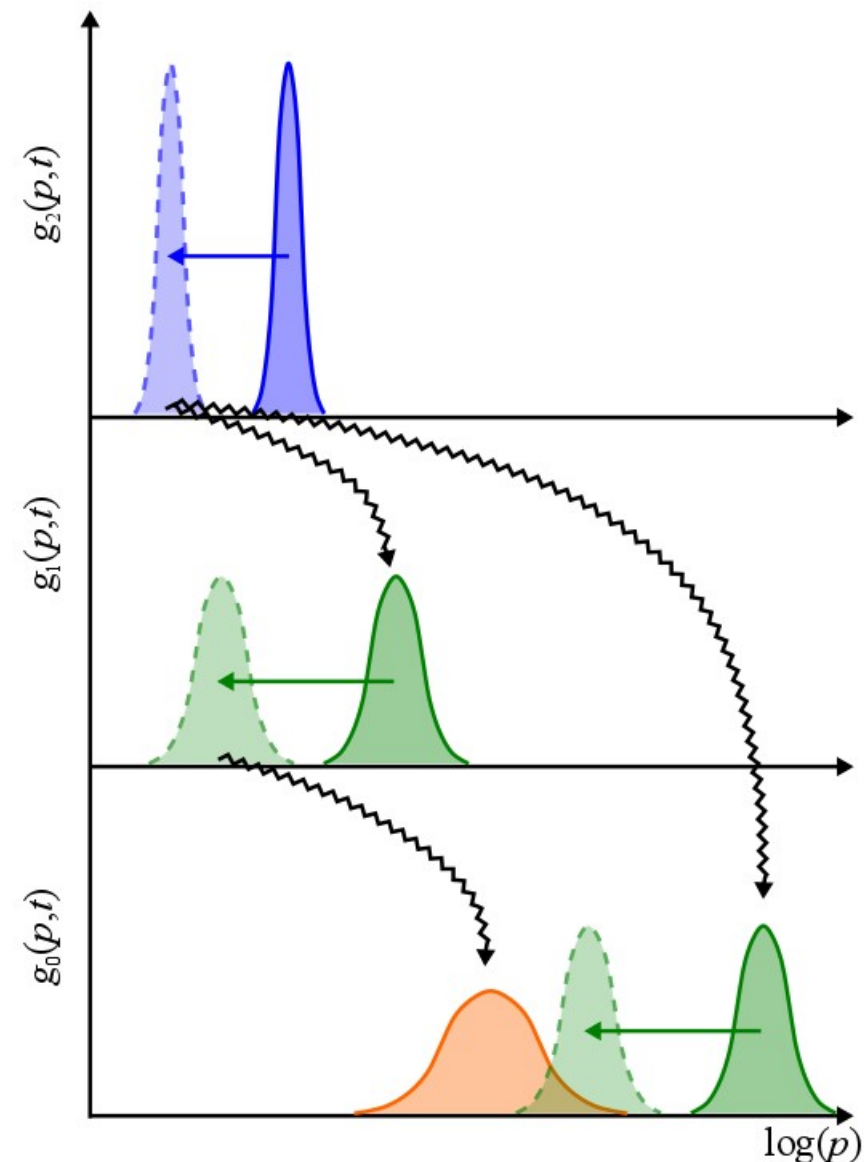
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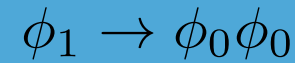
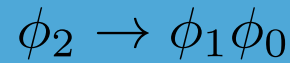
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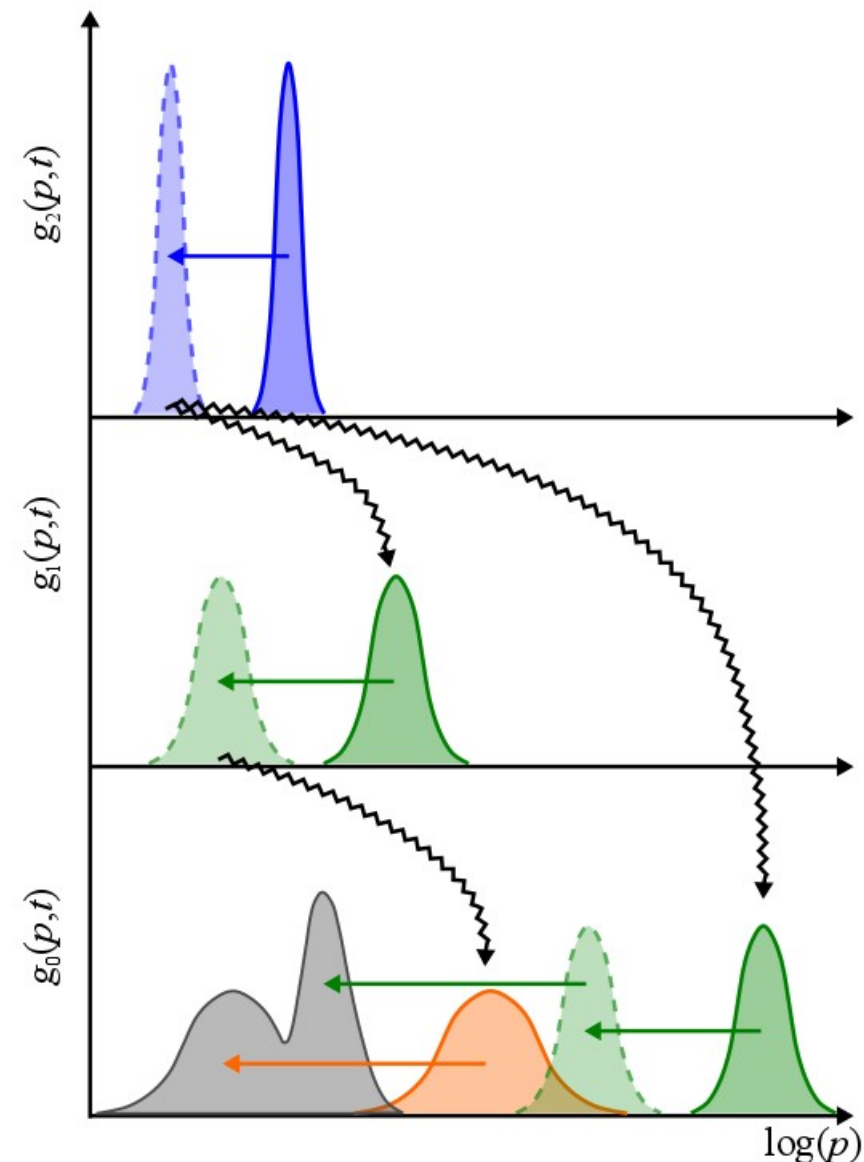
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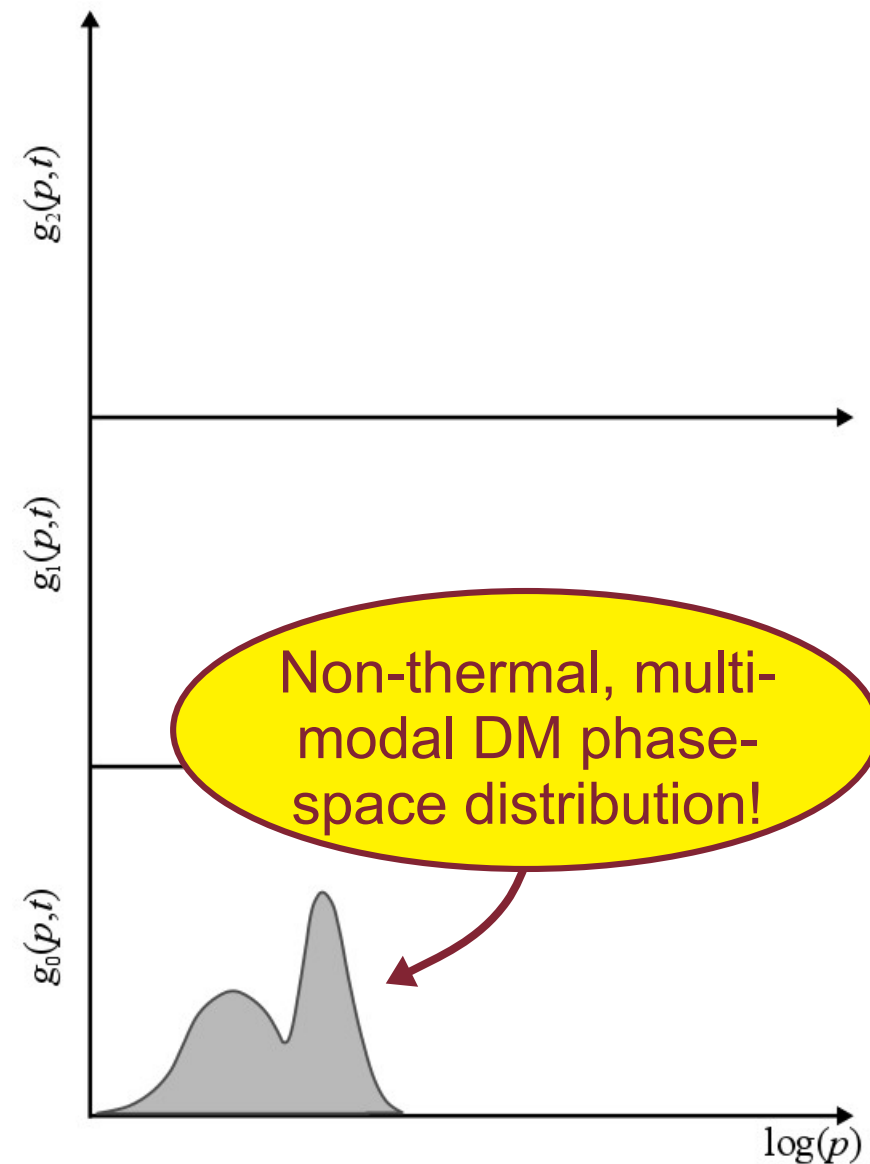
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An Alternative Approach

- By contrast, we shall consider a somewhat unorthodox procedure in which we regard $k_{\text{hor}}(p)$ as a **functional map** between p and k .

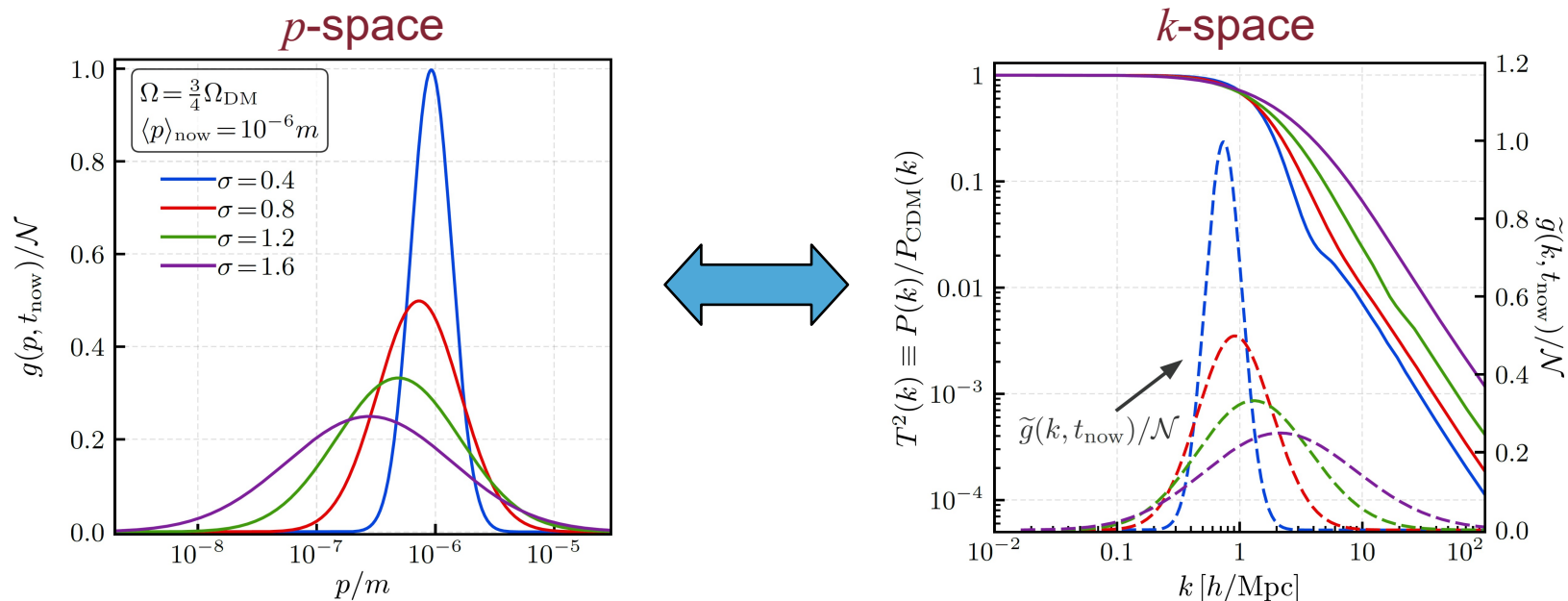
Dienes, Huang, Kost, Su, BT [arXiv:2001.02193]

- We can use this map to define a **phase-space distribution in k -space** which correspond to $g(p)$ in momentum space.

$$\tilde{g}(k) \equiv g(k_{\text{hor}}^{-1}(k)) \left| \frac{d \log p}{d \log k} \right|$$

Inverse of $k_{\text{hor}}(p)$ Jacobian

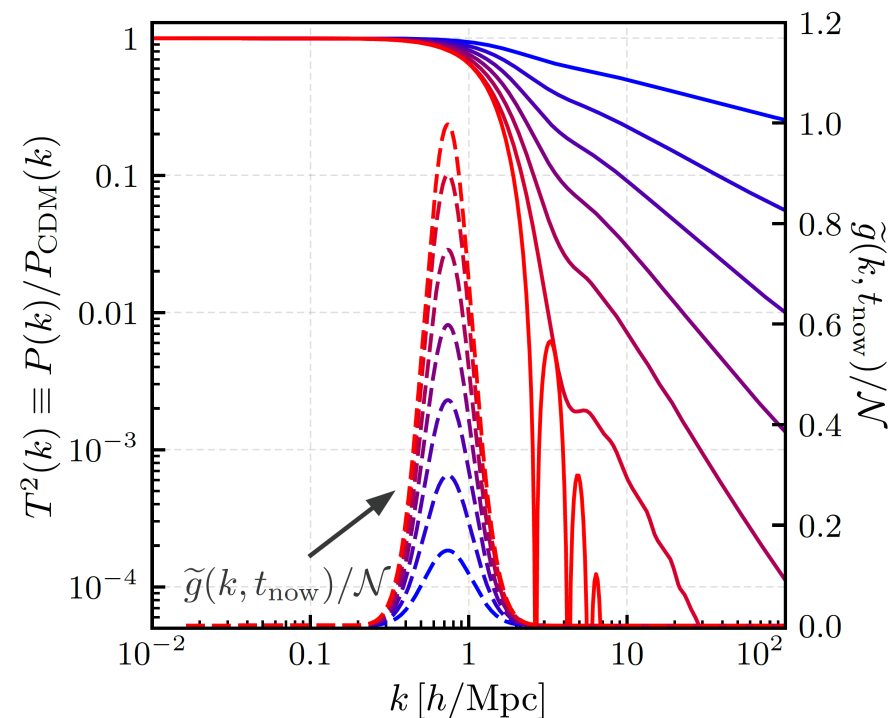
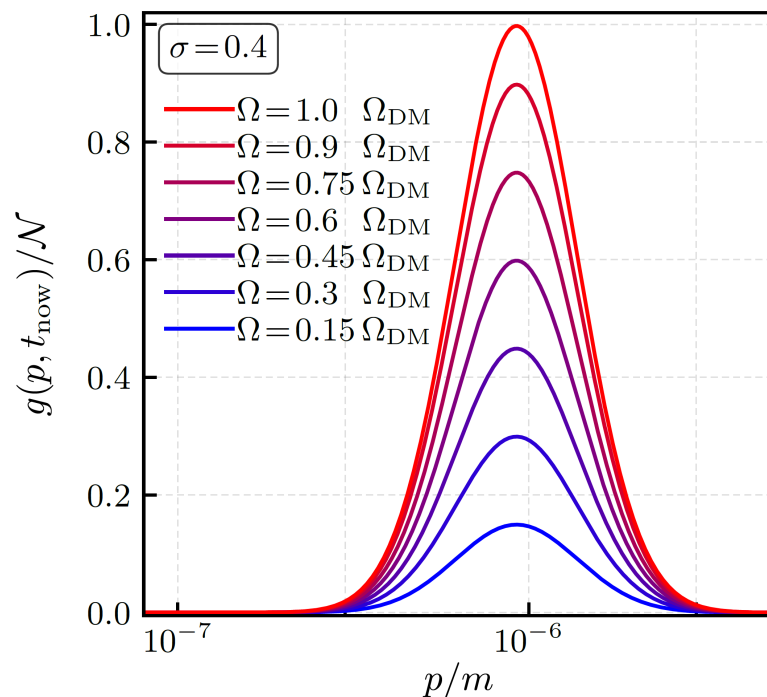
- This means that, in a sense, we can plot the dark-matter phase-space distribution and the matter power spectrum **on the same axis** and explore correlations between them.



Relating $g(p)$ to $T^2(k)$

- Let's first consider the case of a simple $g(p, t_{\text{now}})$ which consists of a single log-normal peak with average momentum $\langle p \rangle$ and width σ .
- We'll begin simply by fixing $\langle p \rangle$ and σ and **varying the normalization** of the peak, assuming that the rest of Ω_{DM} is made up by cold DM.
- Increasing the abundance Ω associated with the peak, we find...

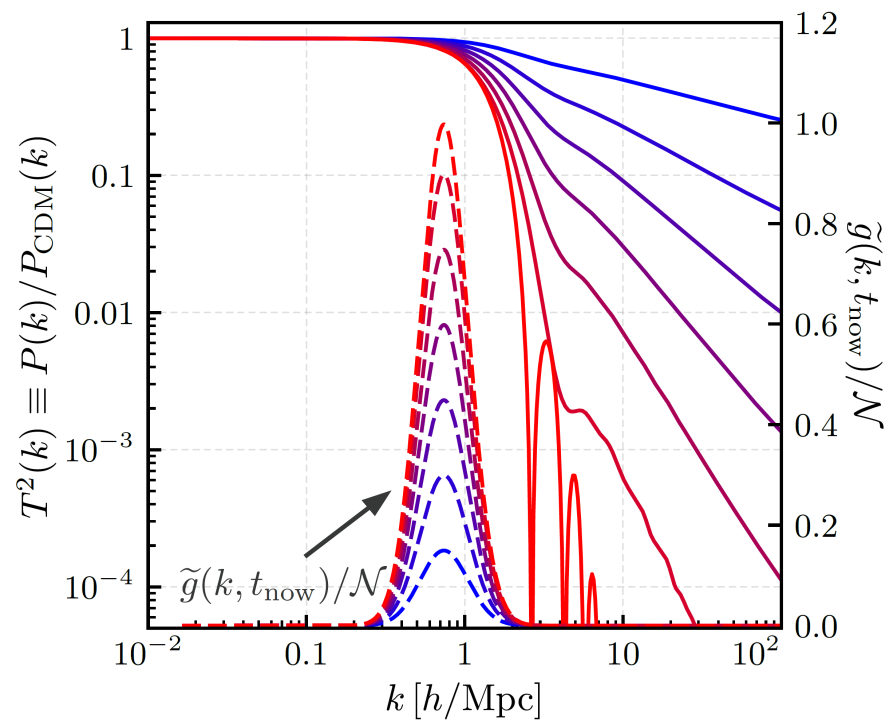
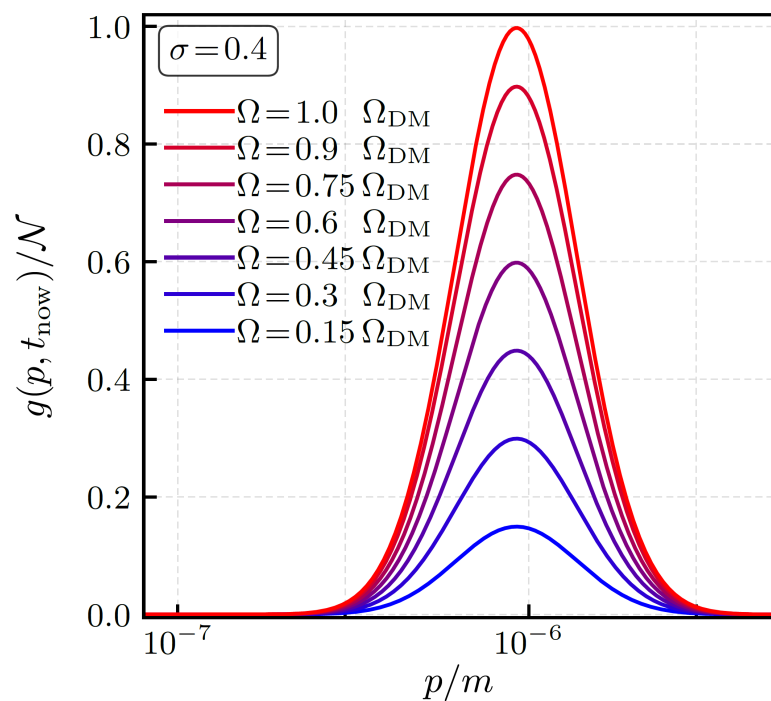
Correlations between $\tilde{g}(k, t_{\text{now}})$ and $T^2(k)$ are **local**: features in $\tilde{g}(k, t_{\text{now}})$ are correlated with features in $T^2(k)$ that appear at/around the same k .



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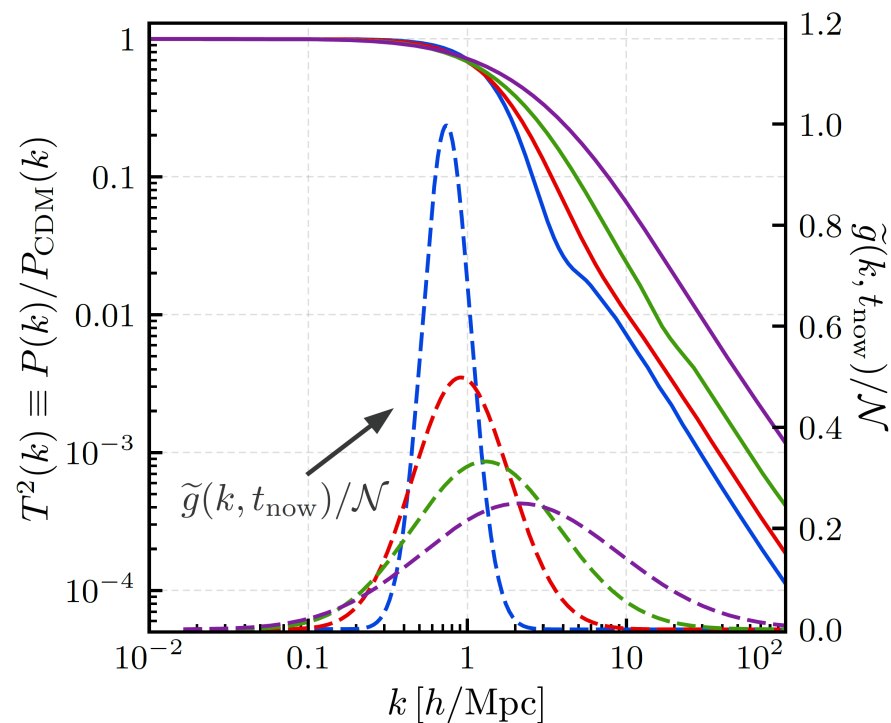
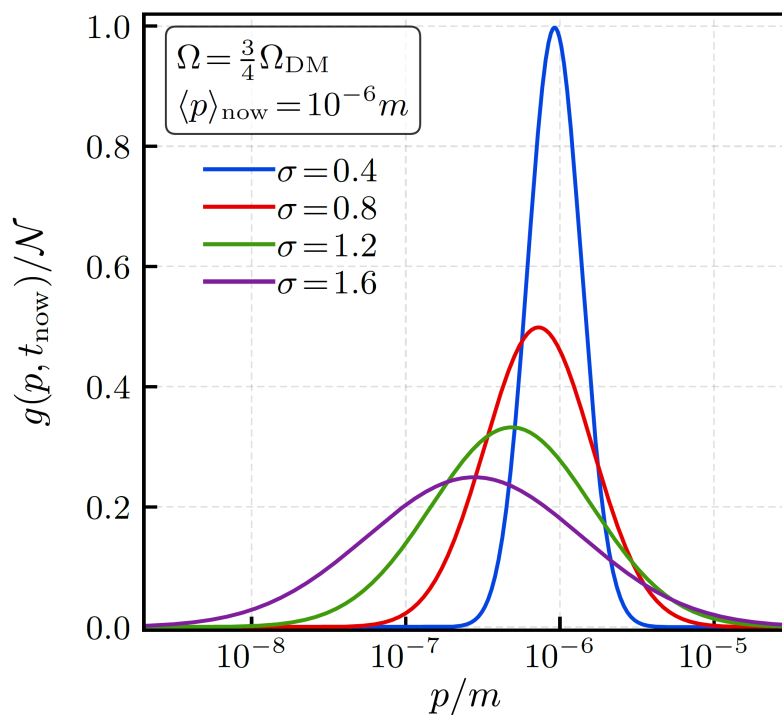
The abundance associated with a peak in $\tilde{g}(k, t_{\text{now}})$ is correlated with the **change in the slope** of $T^2(k)$.



Relating $g(p)$ to $T^2(k)$

- Now let's hold Ω and $\langle p \rangle$ fixed and **vary the width** σ of the peak.
- Different values of σ lead to different amounts of suppression in $T^2(k)$ for k above the peak in $\tilde{g}(k, t_{\text{now}})$, but essentially **identical slopes!**

Once again, the abundance associated with a peak in $\tilde{g}(k, t_{\text{now}})$ correlates *not* with suppression in $T^2(k)$, but rather with the change in its slope.

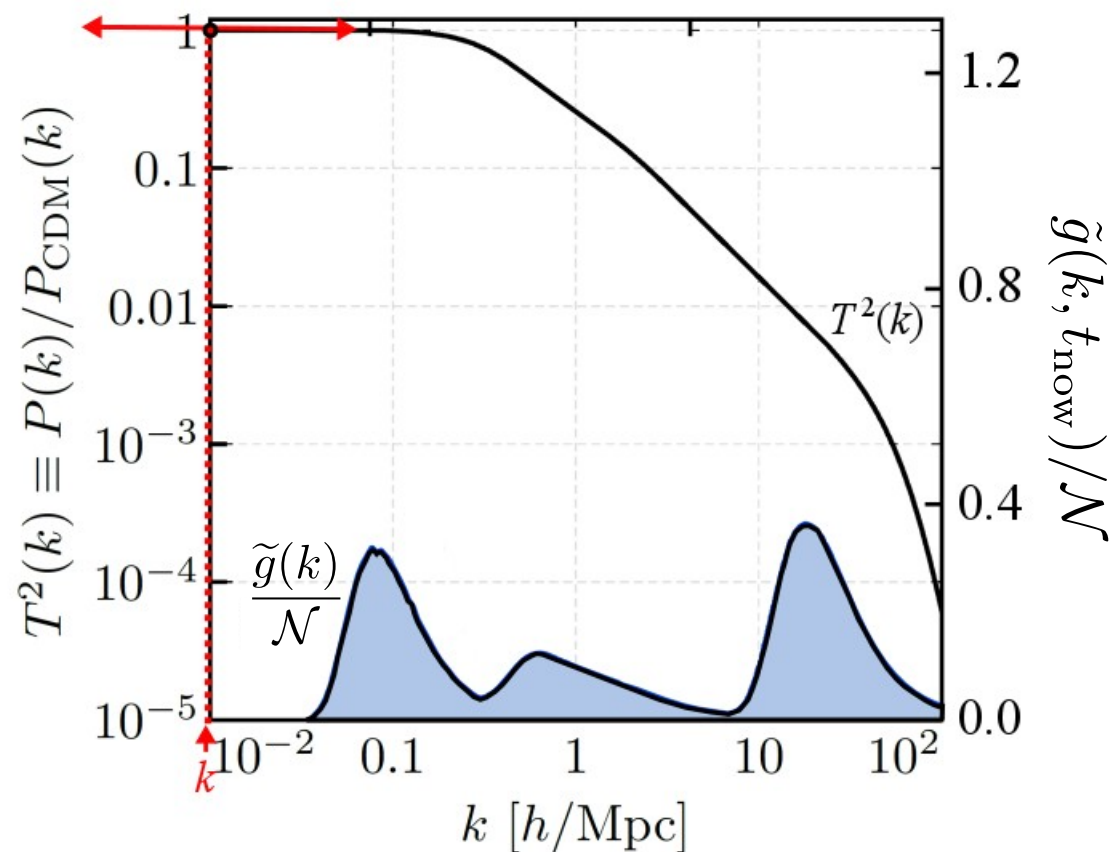
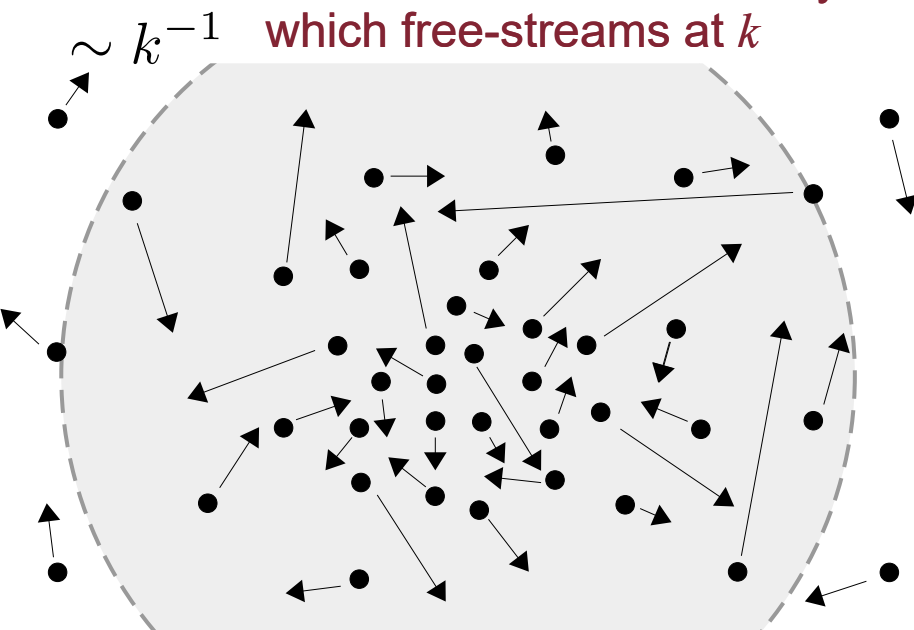


The Hot-Fraction Function

- The slope of the transfer function at a given value of k seems to correlate with the the total number density of particles which can free-stream at that value of k – particles with momenta $p > k_{\text{hor}}^{-1}(k)$.
- Motivated by these empirical findings, let us define the “hot-fraction function” $F(k)$ as follows:

$$F(k) = \frac{\int_{-\infty}^{\log k} \tilde{g}(k) d \log k'}{\int_{-\infty}^{\infty} \tilde{g}(k) d \log k'}$$

Fraction of DM number density
which free-streams at k

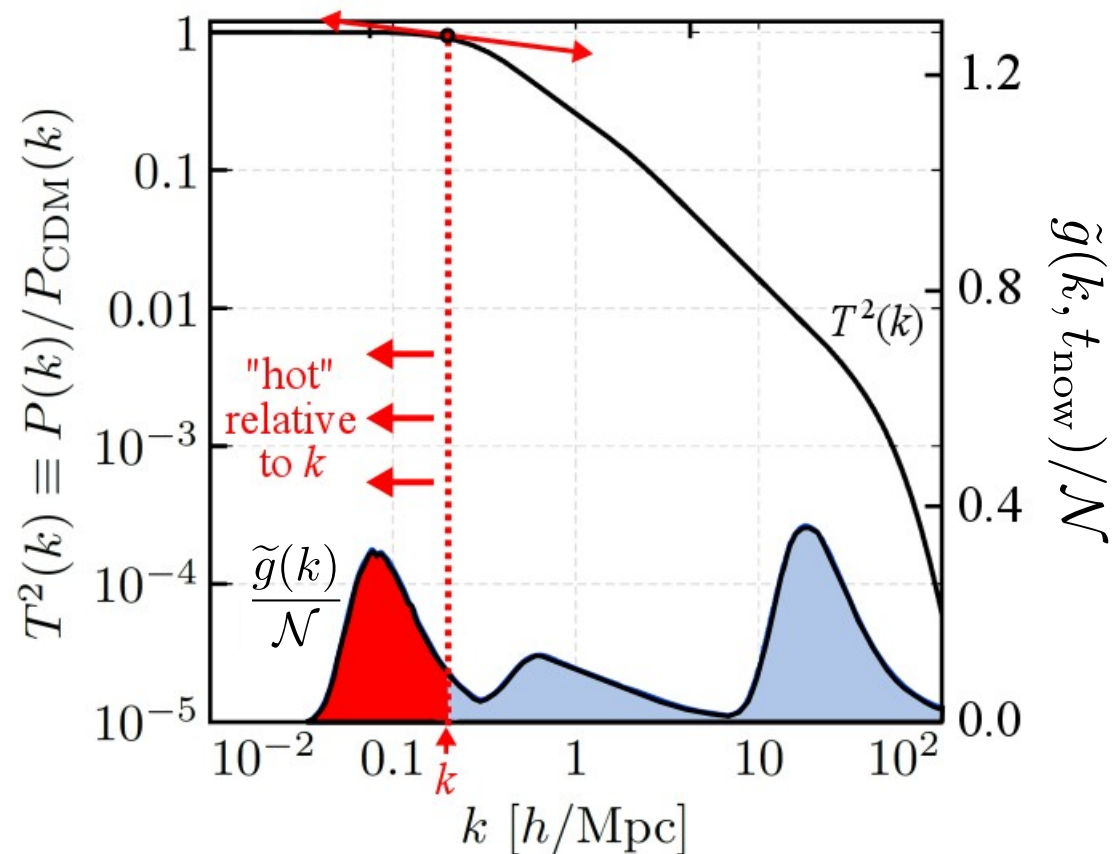
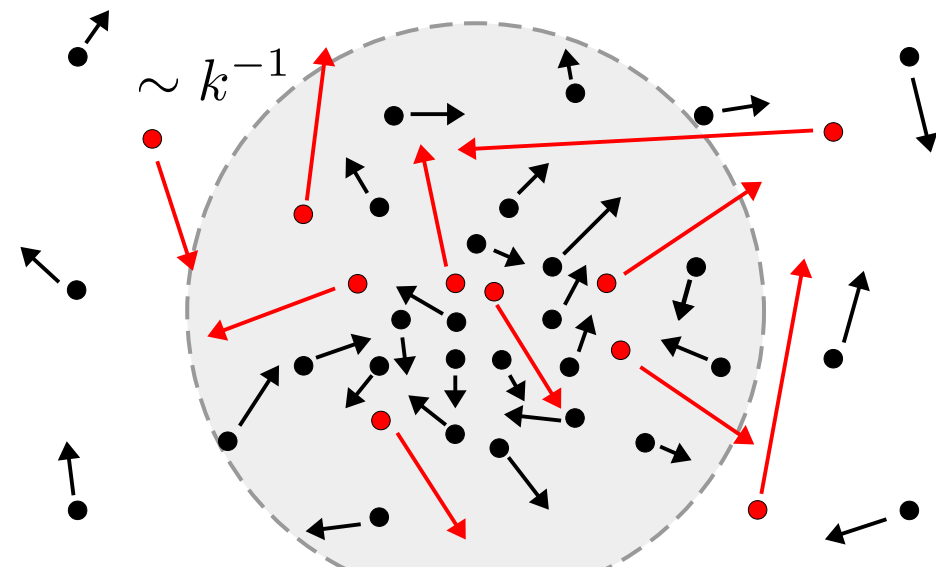


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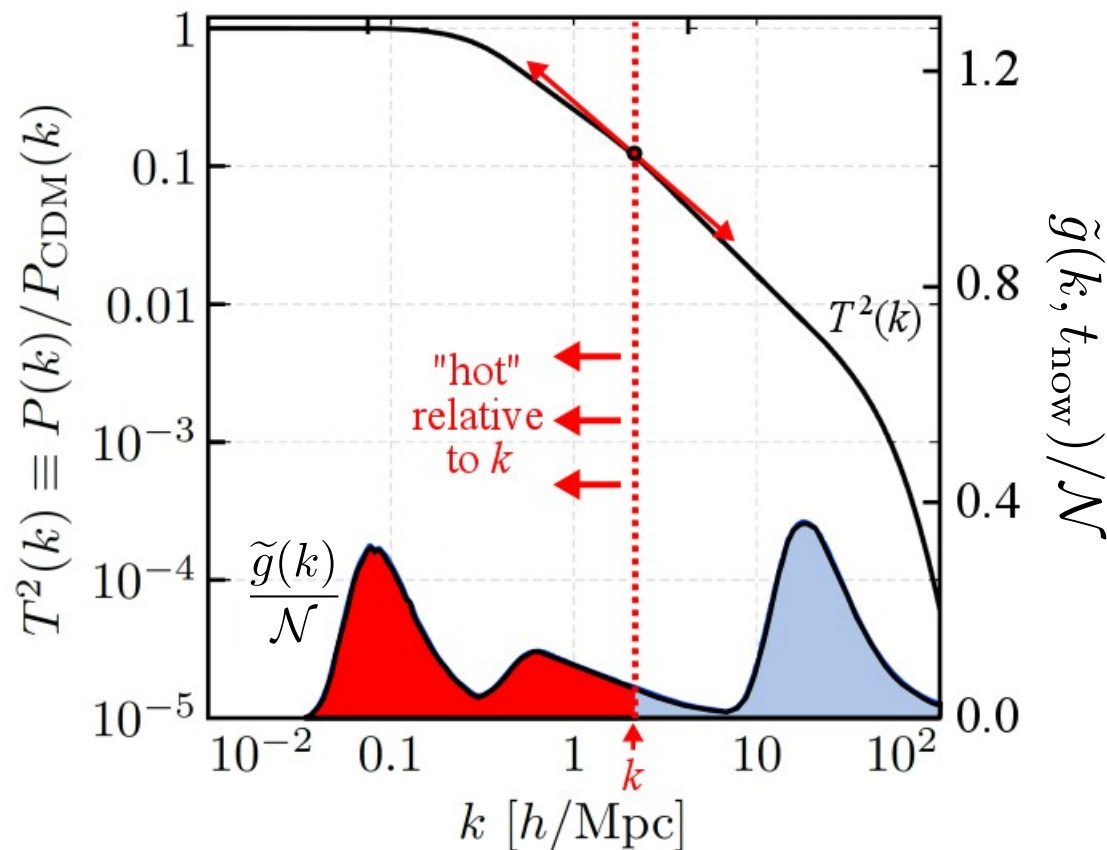
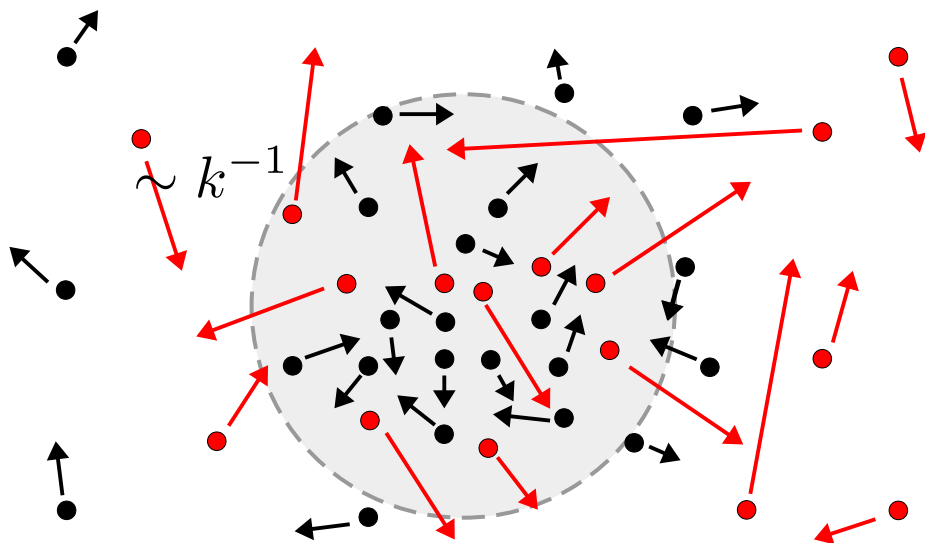


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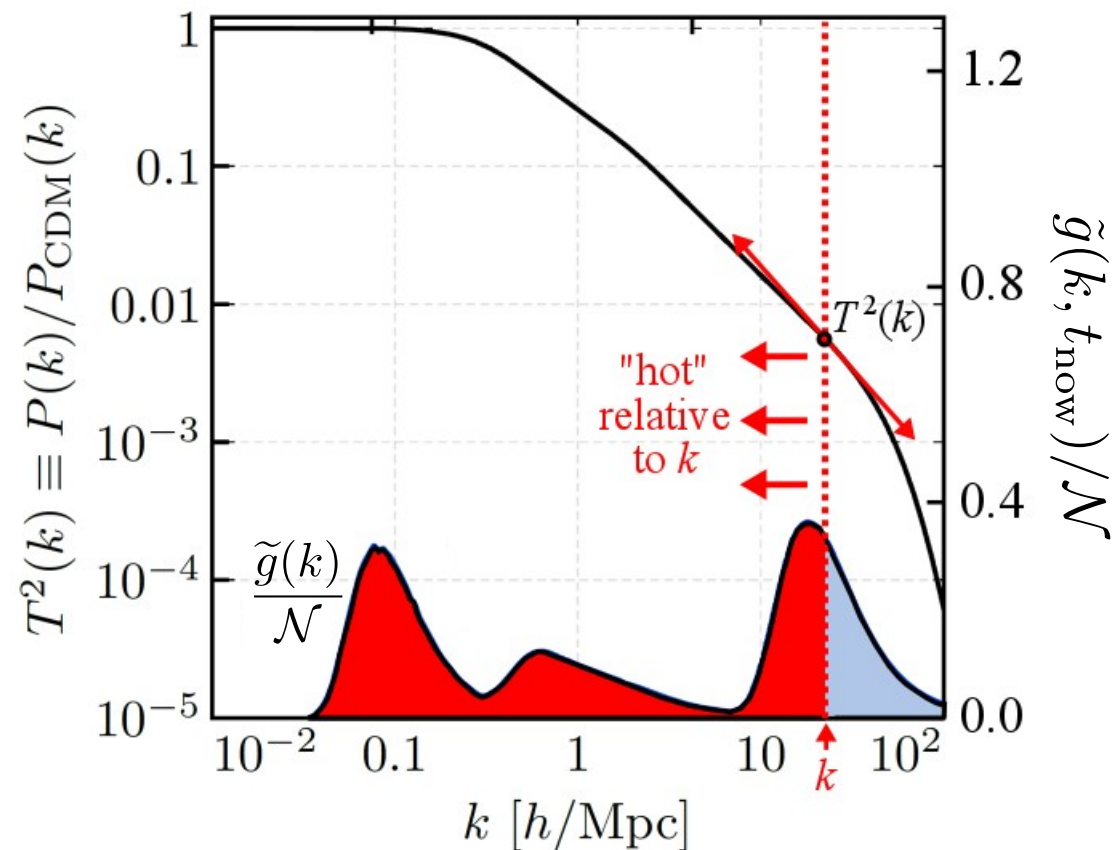
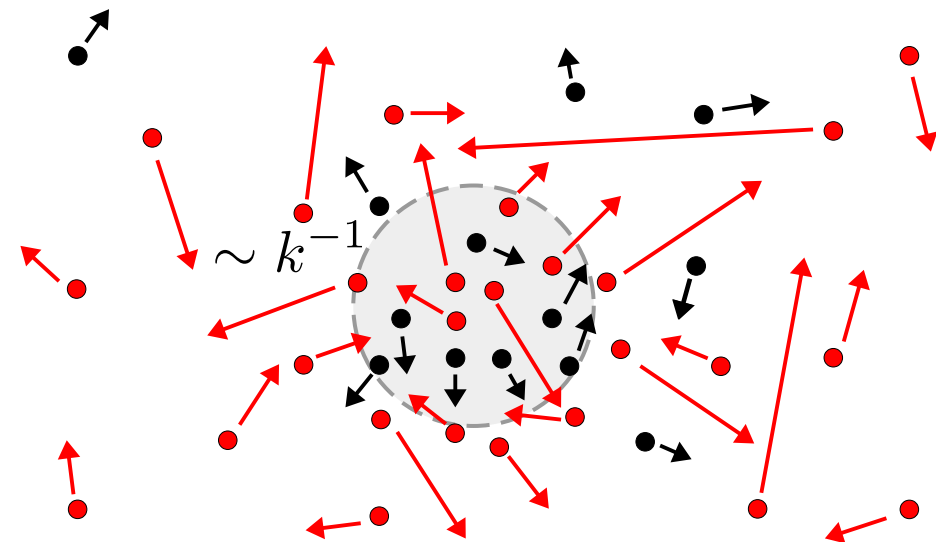


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$$F(k) = \frac{\int_{-\infty}^{\log k} \tilde{g}(k) d \log k'}{\int_{-\infty}^{\infty} \tilde{g}(k) d \log k'}$$

Fraction of DM number density which free-streams at k

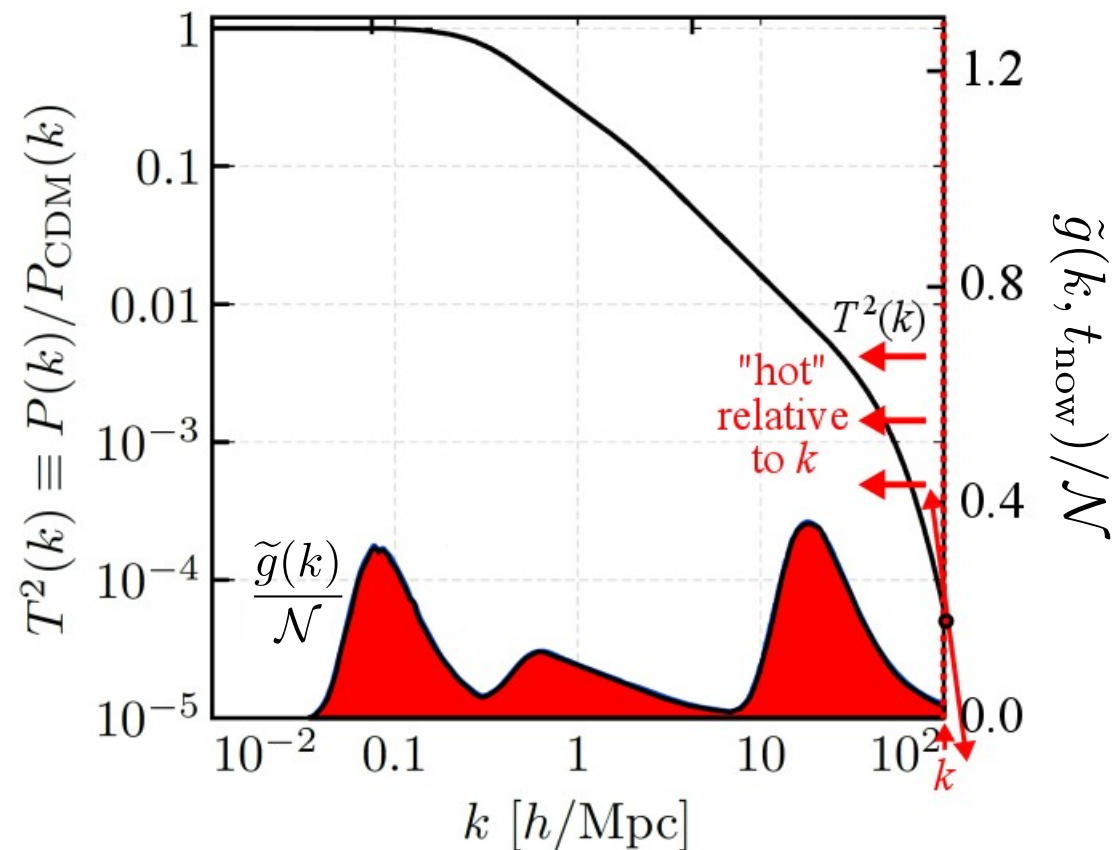
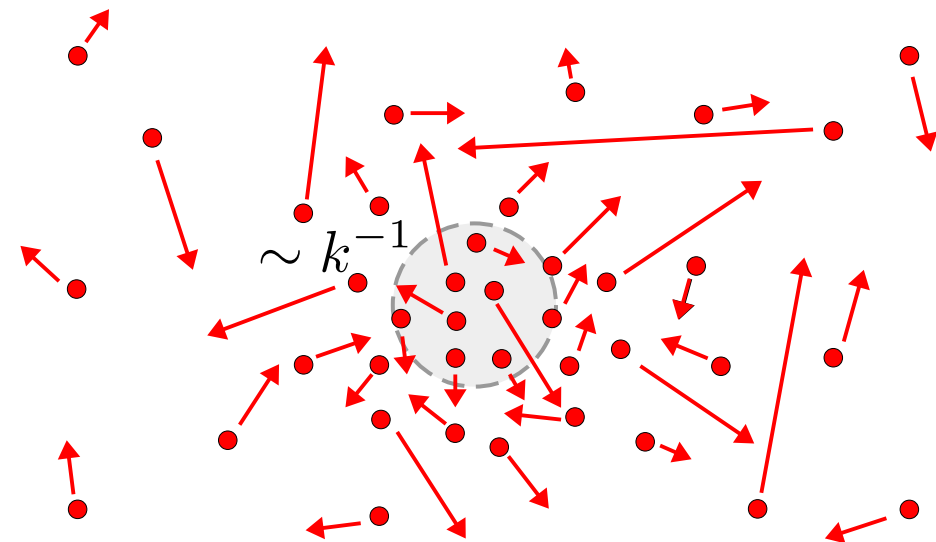


The Hot-Fraction Function

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A Reconstruction Conjecture

- Our conjecture, then, is that there exists some *invertible functional relationship* between $F(k)$ and $T^2(k)$.
- Empirically, from numerical investigations (using CLASS) of the relationship between these two quantities, we find that

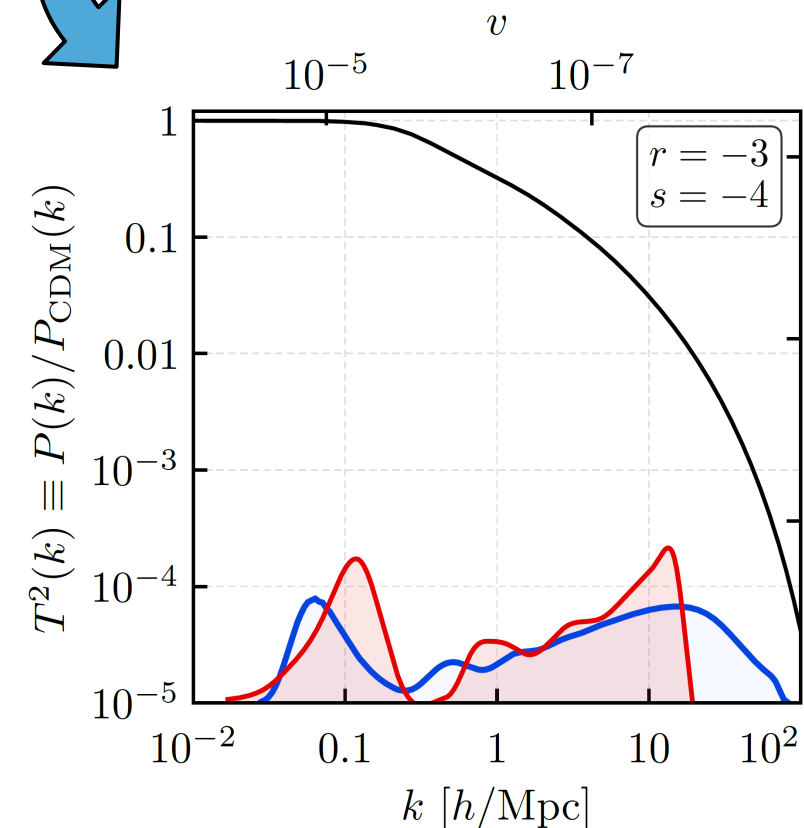
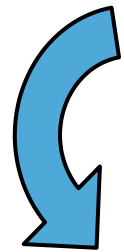
$$\left| \frac{d \log T^2(k)}{d \log k} \right| \approx F^2(k) + \frac{3}{2} F(k)$$

- Taking the derivative of both sides, we obtain an approximate analytic expression for reconstructing $\tilde{g}(k)$ from $T^2(k)$.

$$\frac{\tilde{g}(k)}{\mathcal{N}} \approx \frac{1}{2} \left(\frac{9}{16} + \left| \frac{\log T^2(k)}{\log k} \right| \right)^{-1/2} \left| \frac{d^2 \log T^2(k)}{(d \log k)^2} \right|$$

How Well Does This Work in Practice?

- We can assess how well this reconstruction conjecture works in practice by applying it to the $g(p)$ distributions that emerge from concrete example models.
- One class of models which can give rise to highly trivial, multi-modal $g(p)$ distributions is that involving **multi-step decay chains** within an extended dark sector.



Upshot: It Works Surprisingly Well!

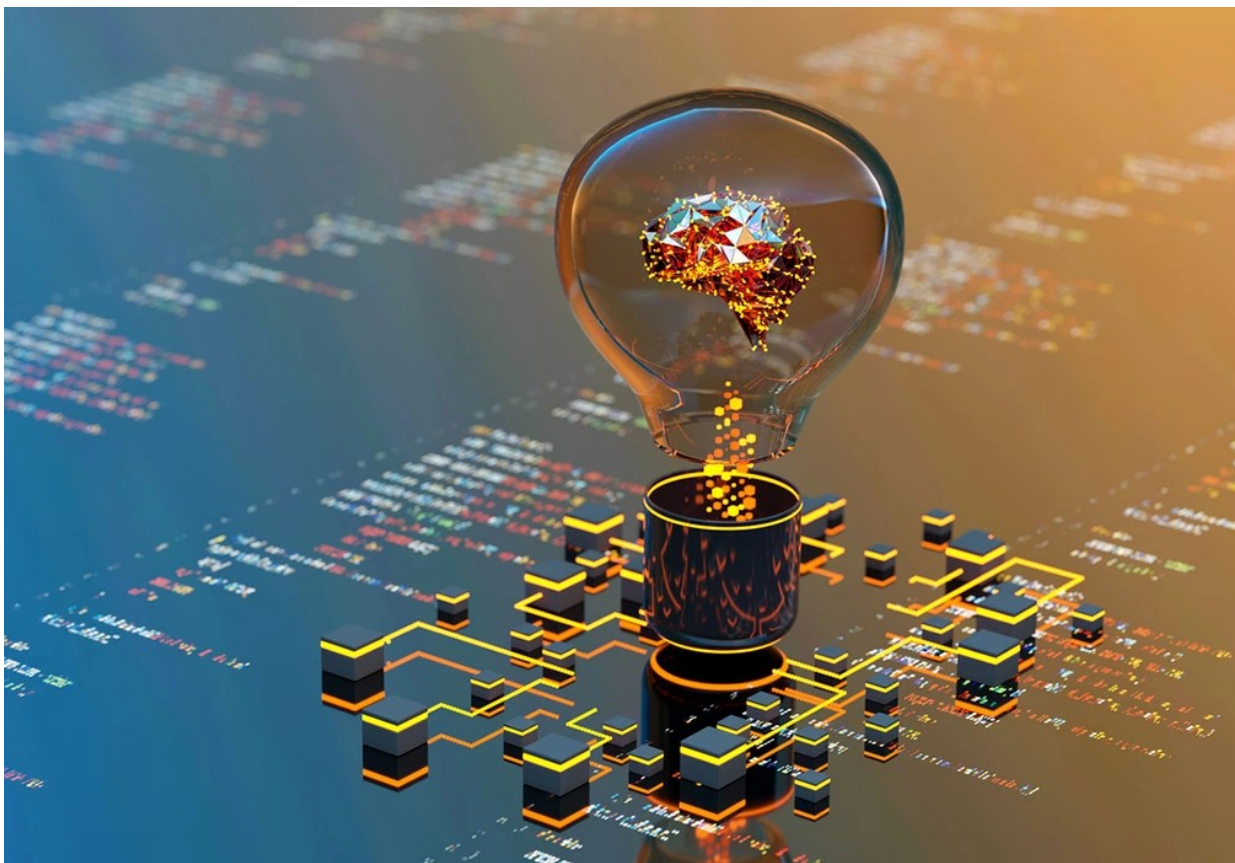
- We find that our reconstruction conjecture reproduces the broad-brush features of the DM velocity distribution quite robustly in all cases.
- However, the accuracy of the reconstruction could be improved... and fortunately there's a straightforward way of accomplishing that.

Blue: actual $\tilde{g}(k)$ distribution for the model in question

Red: reconstructed $\tilde{g}(k)$ distribution using our procedure

Machine Learning

- Uncovering relationships between sets of distributions is a task that machine learning is particularly well suited for.



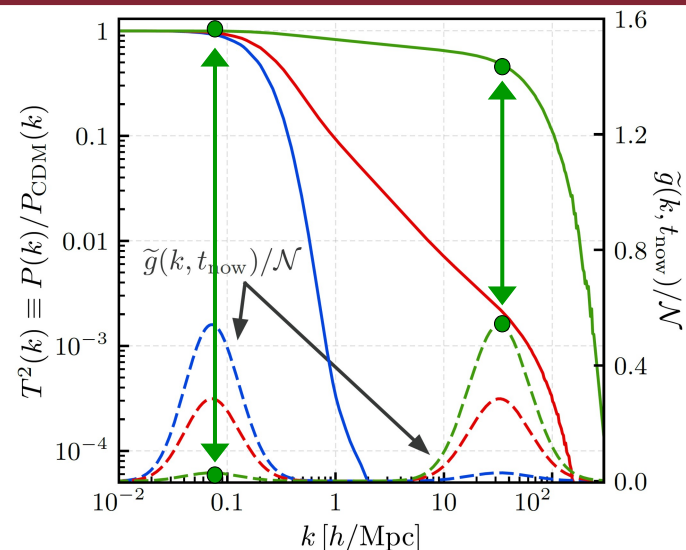
- The intuition that we've developed in deriving our empirical reconstruction conjecture will guide us in terms of network architecture, how we train the network, etc.

A Little Human Intuition

- In constructing and training our machine, we'll exploit the physical intuition we've developed – and in particular, **two guiding principles**:

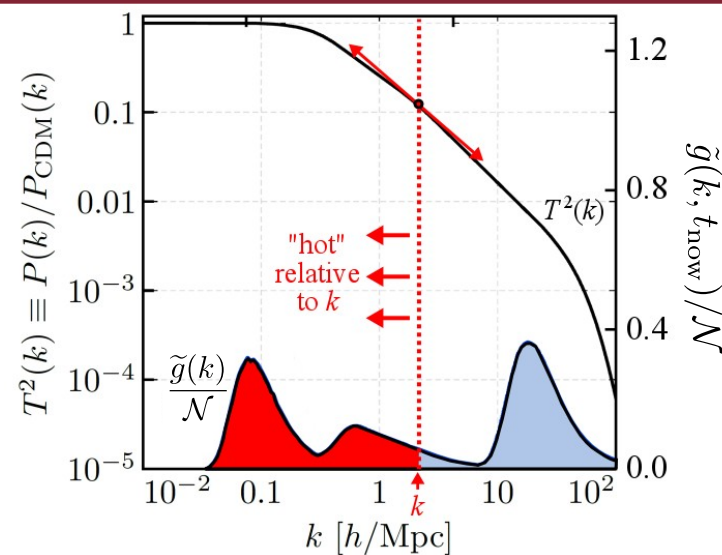
1 k -Locality

The reconstructed value of $g(k)$ at a given k should only depend on the properties of $T^2(k)$ at/around that same value of k .



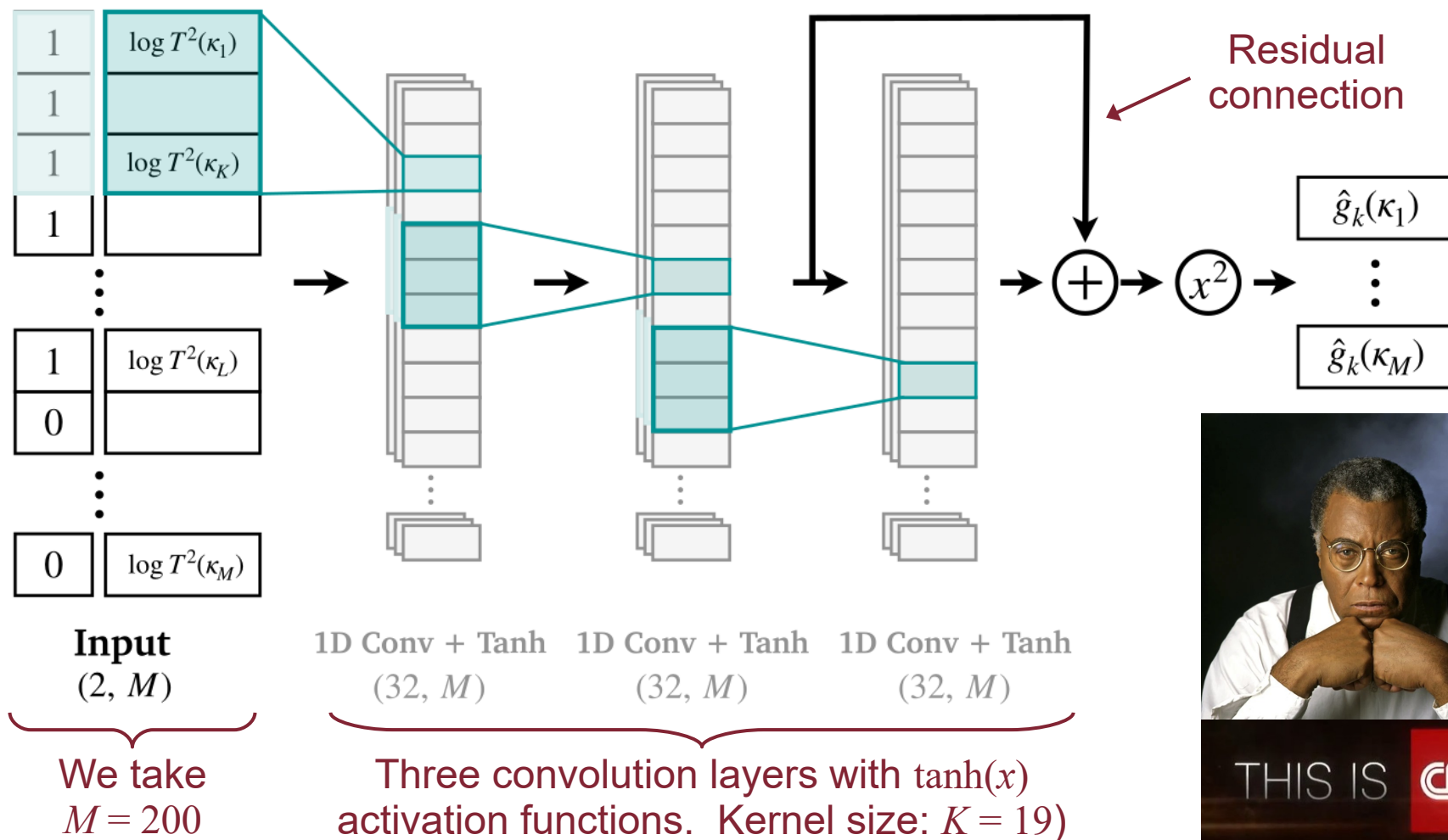
2 Horizon Thresholds

The value of $g(k)$ at a particular value of k should have no impact whatsoever on the shape of $T^2(k)$ anywhere below that value of k .



This in CNN: Reconstruction with ML

- We find that a **convolutional neural network** (CNN) provides the best performance out of a wide range of possible network architectures.



- Indeed, a CNN incorporates an inductive bias that **emphasizes local features** of $T^2(k)$ while still allowing for non-local connectivity.

Loss Function

- The **loss function** \mathcal{L} that we employ during the training process in order to establish a relationship between a reconstructed phase-space $\hat{g}(k)$ and the corresponding “true” $g(k)$ distributions is based on a simple mean-squared error (MSE) function:

$$\mathcal{L}_{\text{MSE}} = \frac{1}{M} \sum_{i=1}^M |\hat{g}(\kappa_i) - g(\kappa_i)|^2.$$

No. of pts.
sampled
($M = 200$)

- Our full loss function includes a curvature penalty in order to reduce the effect of numerical noise and fluctuations which can arise at large k .

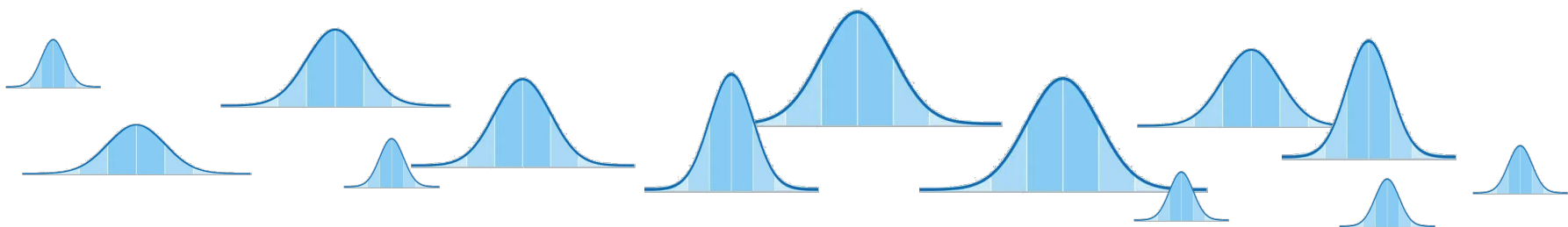
Smoothing hyperparameter

$$\mathcal{L} = \mathcal{L}_{\text{MSE}} + \frac{\lambda_s}{M} \sum_{i=2}^{M-1} |\hat{g}_k(k_{i+1}) - 2\hat{g}_k(k_i) + \hat{g}_k(k_{i-1}))|^2$$

- λ_s and other hyperparameters optimized using the Optuna framework.

Training Data and Truncation

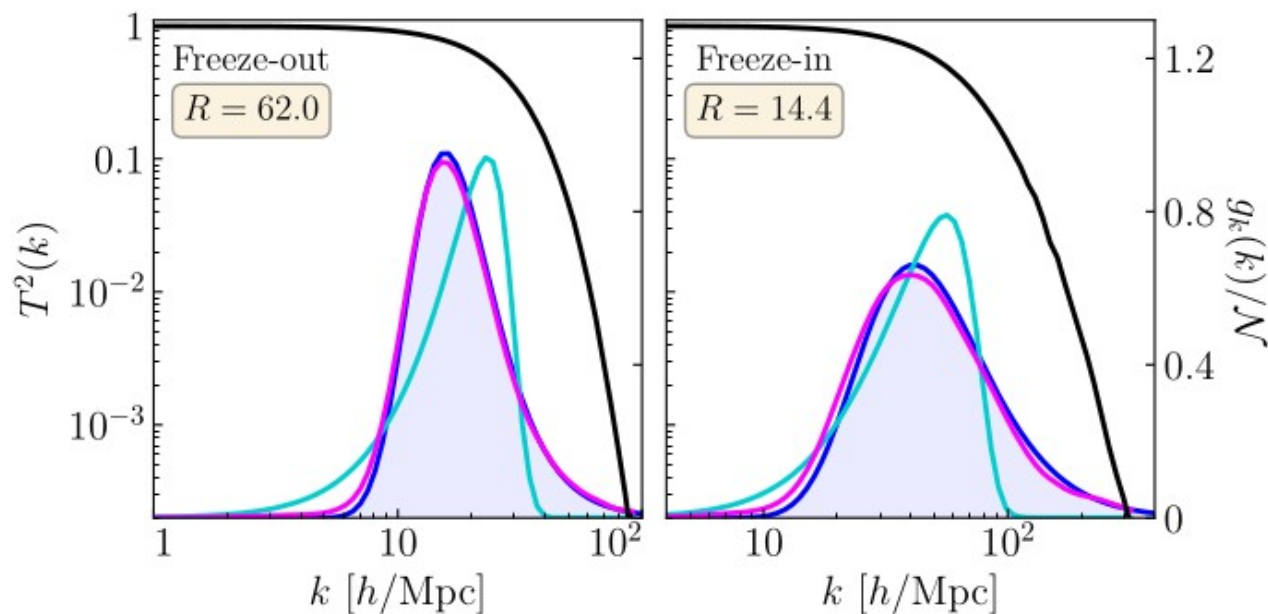
- Our core training data consists of $g(k)$ created by combining $N = 30$ or $N = 80$ individual Gaussian distributions with randomly distributed means, widths, and amplitudes.



- We also include:
 - $g(k)$ distributions created by combining smaller numbers ($N = 1$, $N = 2$, and $N = 3$) of such Gaussians.
 - $g(k)$ distributions associated with DM freeze-in and freeze-out.
- While training, we implement a **truncation procedure** wherein we randomly select some k value k_L , truncate $\log T^2(k)$ for $\log k > \log k_L$, and forward-fill the truncated values.
- Training on these truncated distributions weakly encourages the CNN to learn something akin to our **horizon-threshold principle**.

Machine Learning Does it Better

- We begin by examining the trained network's performance for transfer functions obtained from **simple, unimodal** $g(k)$ distributions.
- In particular, we apply them to $g(k)$ distributions obtained from DM freeze-in and freeze-out.
- We assess the accuracy of $\hat{g}(k)$ via our (MSE) function and use the ratio $R \equiv \mathcal{L}_{\text{MSE}}^{(\text{emp})} / \mathcal{L}_{\text{MSE}}^{(\text{ML})}$ to provide a measure for comparing the accuracy of empirical and ML reconstructions.



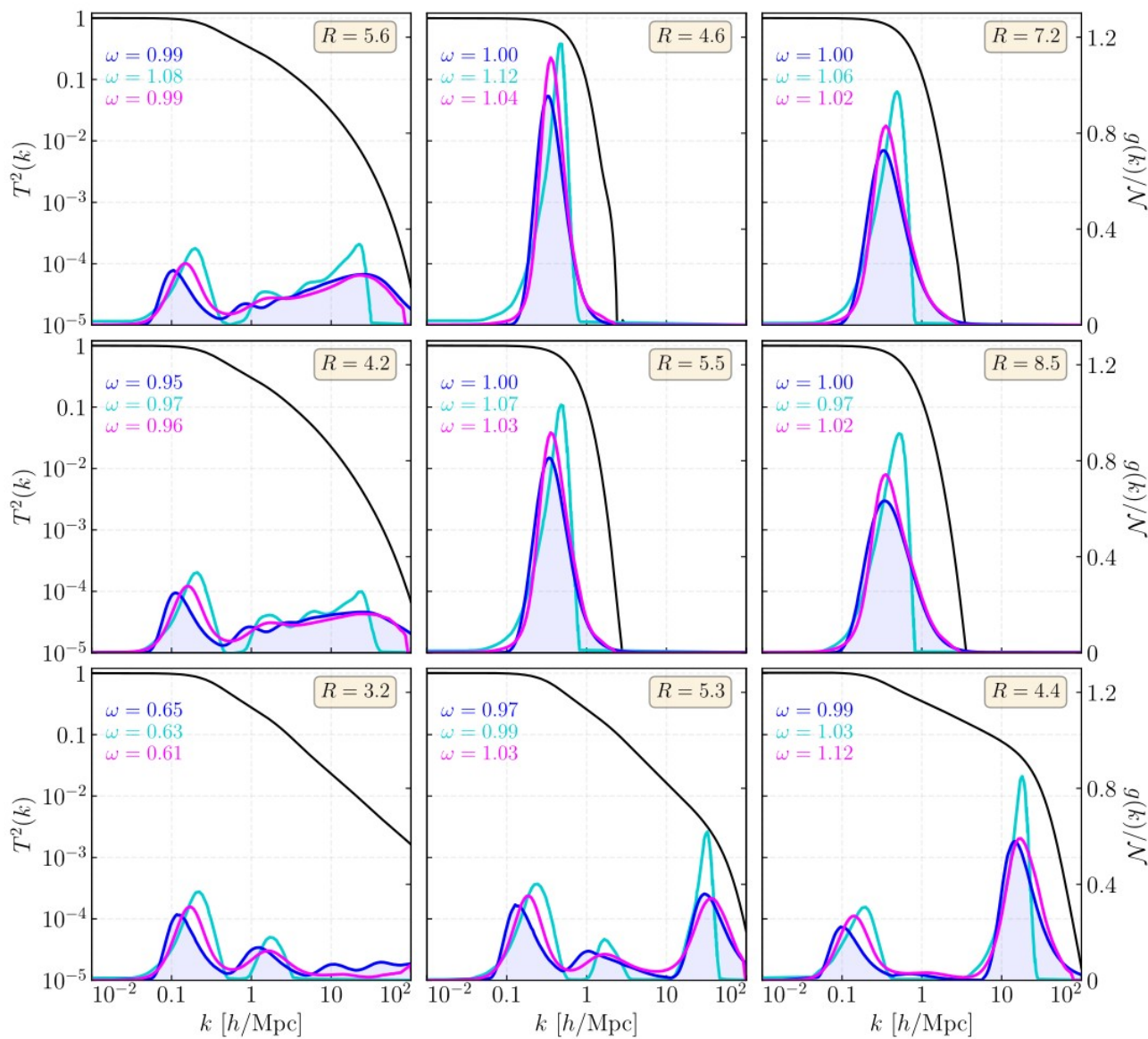
Example: $m = 50$ keV

- “Truth” $g(k)$ distribution
- Analytic reconstruction
- ML reconstruction

- In both cases, the CNN generically **outperforms** our empirical reconstruction conjecture by an order of magnitude!

Machine Learning Does it Better

- We also examine the trained network's performance for transfer functions obtained from **complicated, multi-modal** $g(k)$ distributions.
- We use the CNN to reconstruct $\hat{g}(k)$ distributions obtained from cascade-decay models.
- Once again, the CNN **outperforms** our empirical reconstruction conjecture by a significant margin.



— “Truth” $g(k)$ distribution
 — Analytic reconstruction
 — ML reconstruction

Stability of the Solutions

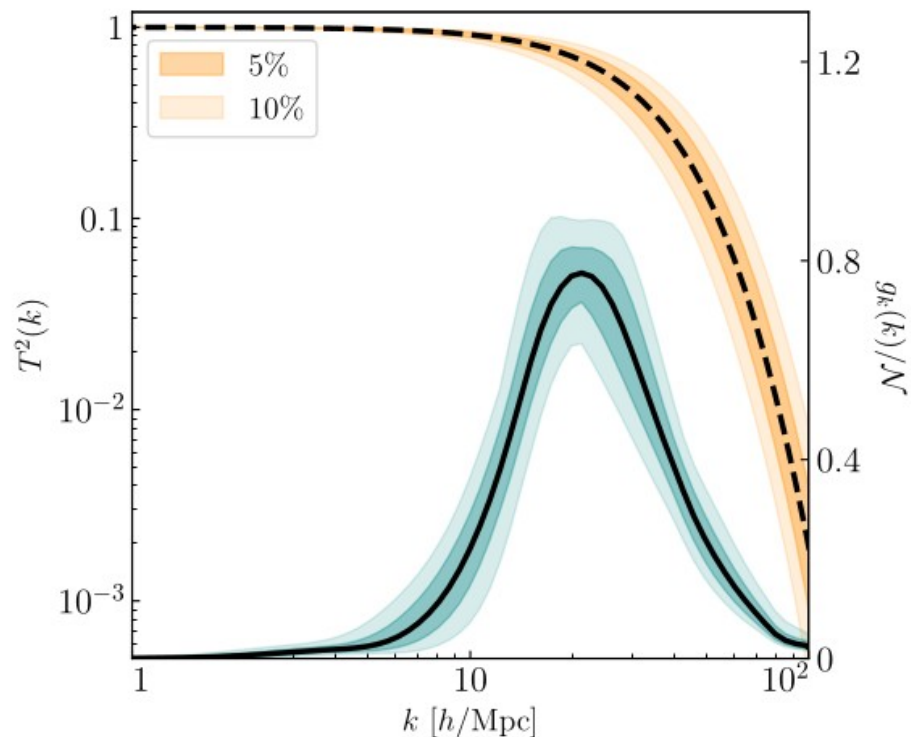
- We can test the stability of the solutions by perturbing $T^2(k)$ in a controlled way and examining the effect on the corresponding reconstructed $\hat{g}(k)$ distribution.

Unimodal

$$T^2(k) = [1 + (\alpha k)^\beta]^{2\gamma}$$

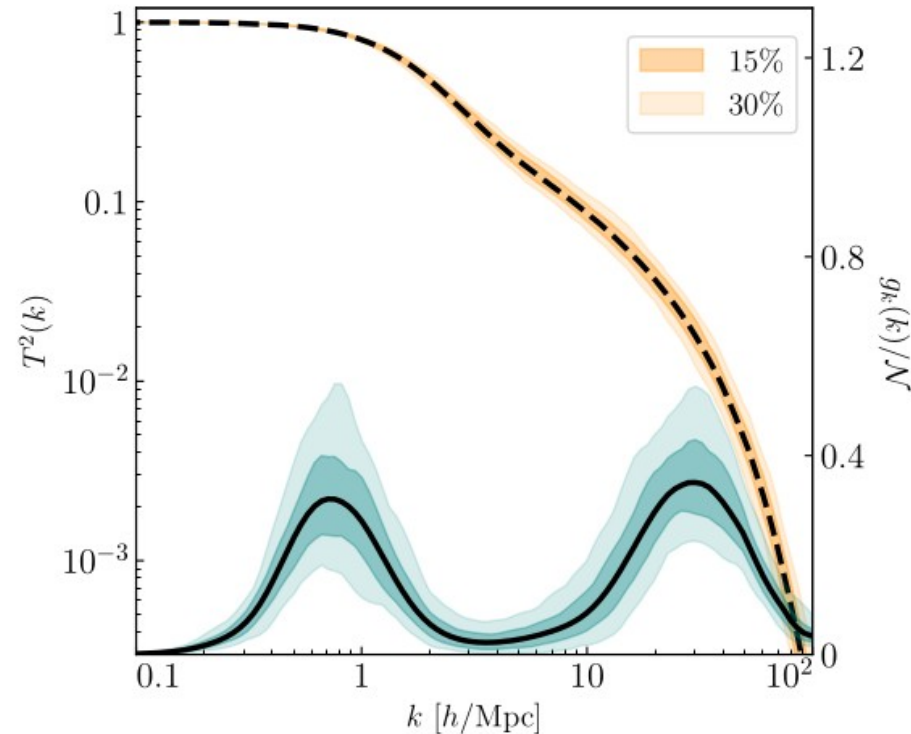
[Murgia et al., 1704.07838]

Vary $\{\alpha, \beta, \gamma\}$ within a specified range.



Bimodal

Perturb difference $\Delta \log T_0^2(k_i)$ between $\log T_0^2(k_i)$ values at adjacent grid points by a specified percentage.



Summary

- Non-trivial dynamics in the early universe can lead to a complicated – and even multi-modal – DM velocity distribution, which in turn affects the shape of the matter power spectrum.
- In an effort to work backwards, we have studied the relationship between $P(k)$ and the DM velocity distribution and found that the **slope of the transfer function** at a given k is related to the **fraction of the DM number density which can free-stream** on the scale k .
- Motivated by these results, we have formulated a conjecture for **reconstructing the primordial dark-matter velocity distribution** from the shape of the matter power spectrum.
- Moreover, we have seen that **machine learning** can significantly improve the accuracy of such reconstruction efforts.

